



**NANYANG
TECHNOLOGICAL
UNIVERSITY**
SINGAPORE

Temporal-Spatial Coordination of Distributed Energy Resources (DERs) in Microgrids

Dr Yan Xu | Nanyang Assistant Professor
School of Electrical & Electronic Engineering
Nanyang Technological University (NTU)
Email: xuyan@ntu.edu.sg
Web: <https://eexuyan.github.io/soda/index.html>

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

1

REIDS Project

2

DER Control

- Islanded microgrid
- Grid-connected microgrid

3

DER Operation

- Energy dispatch
- Volt/Var regulation

4

Hierarchy Coordination

- Volt/Var control
- Active power balancing

5

DER Planning

- Distributed generation units
- Energy storage systems

Timescale

ms ~ seconds

mins ~ hours

ms ~ hours

years ~ decades



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- *Renewable Energy Integration Demonstrator – Singapore (REIDS)*



Energy Research Institute @ NTU

REIDS

Renewable Energy Integration Demonstrator - Singapore



REIDS is a Singapore-based RD&D platform dedicated to designing, demonstrating and testing solutions for sustainable multi-activity off-grid communities in Southeast Asia

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

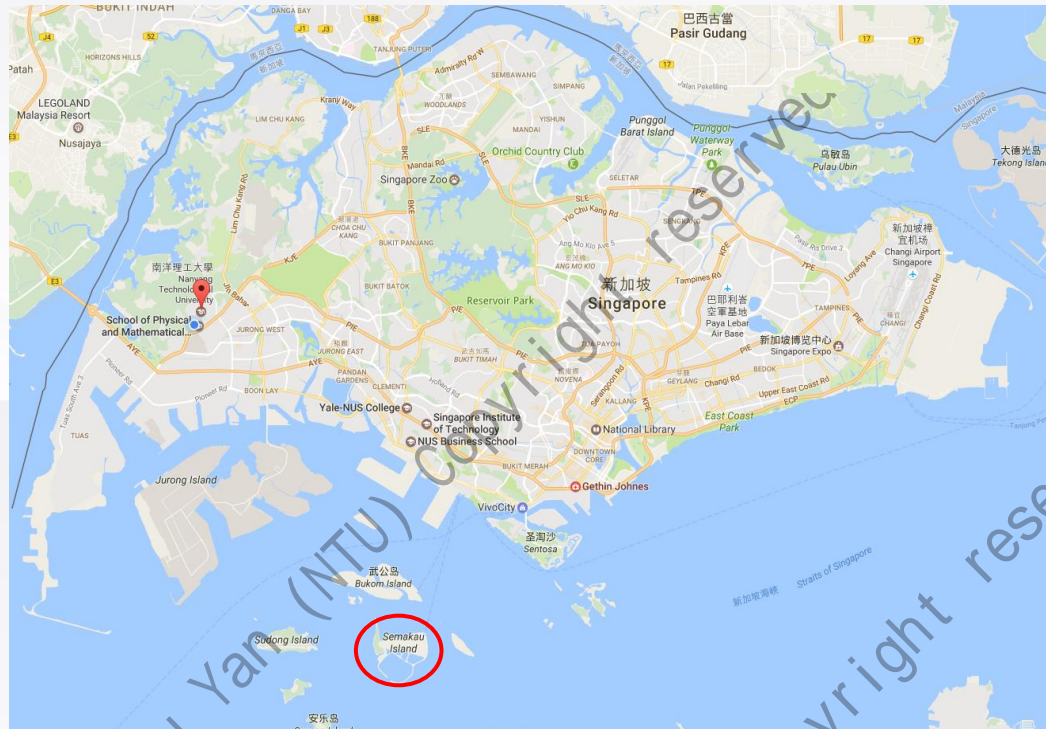
3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm



REIDS Partners



Research Leader



Supporting Agencies



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

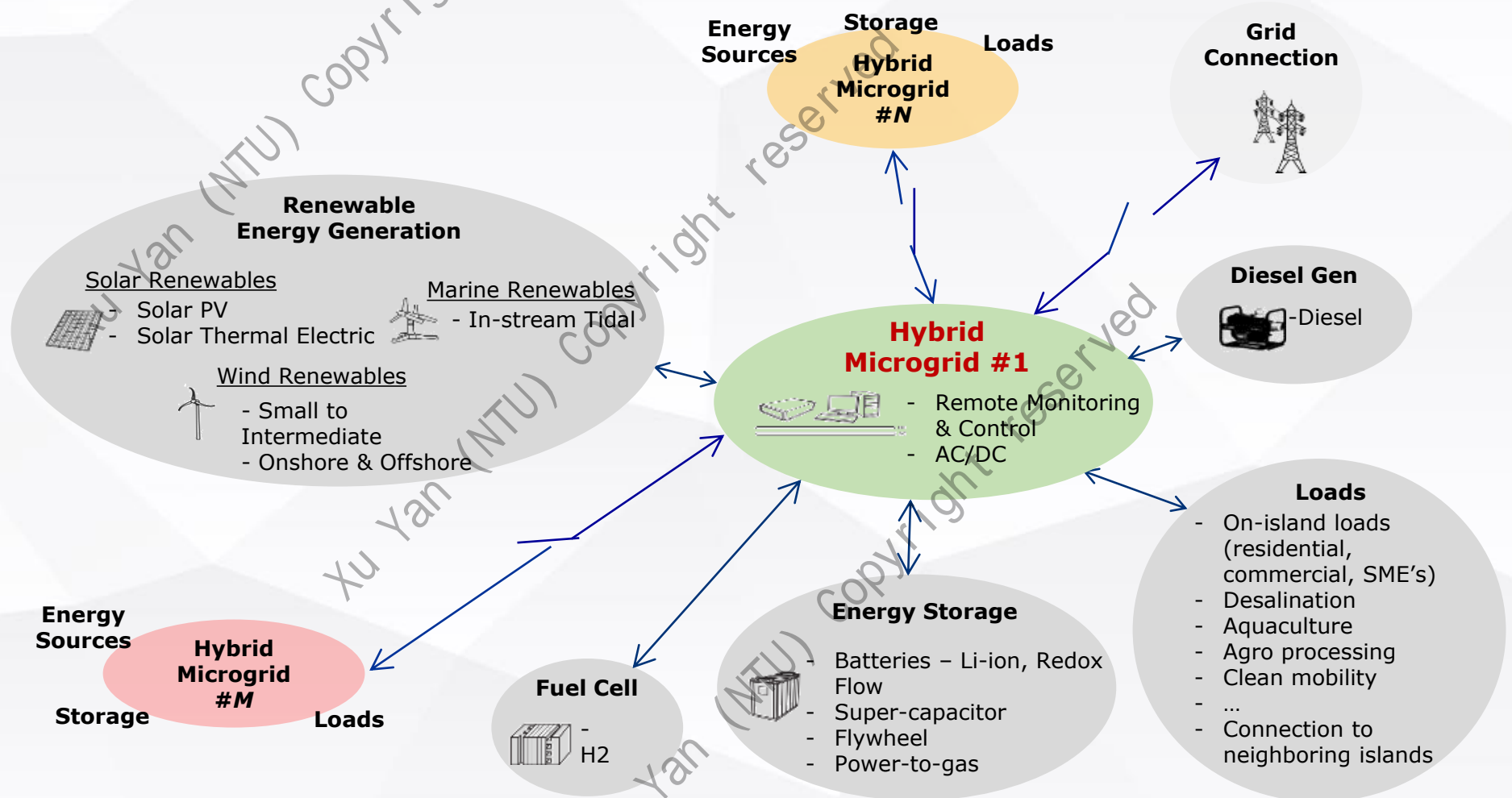
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

REIDS Roadmap and Framework

Phase I – 4 independent MGs (500kW-1MW each)

Phase II – 4 MGs in a cluster configuration (100kW-250kW each)



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

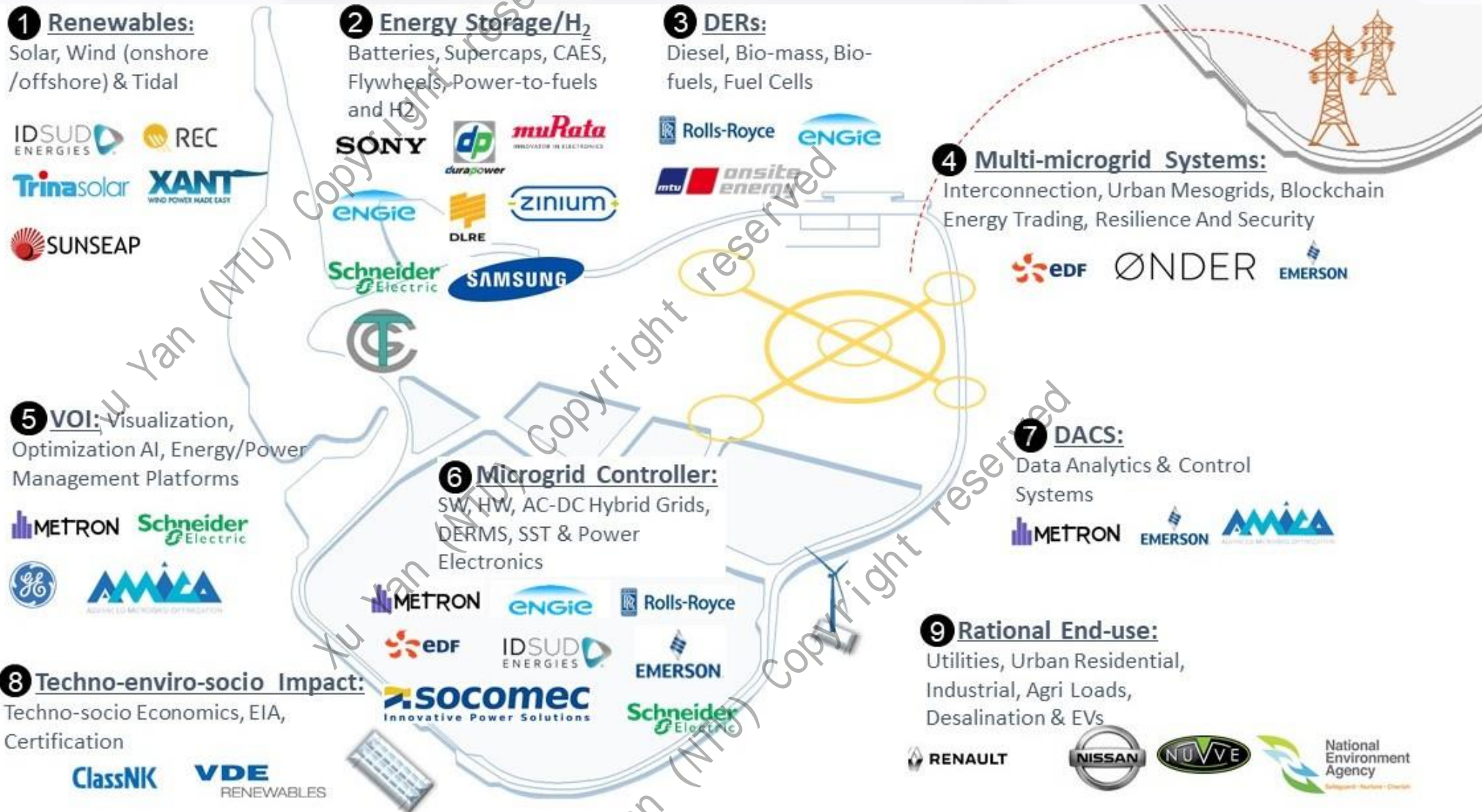
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Onboard Industry Collaborators



<http://erian.ntu.edu.sg/REIDS/Pages/AboutREIDS.aspx>

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

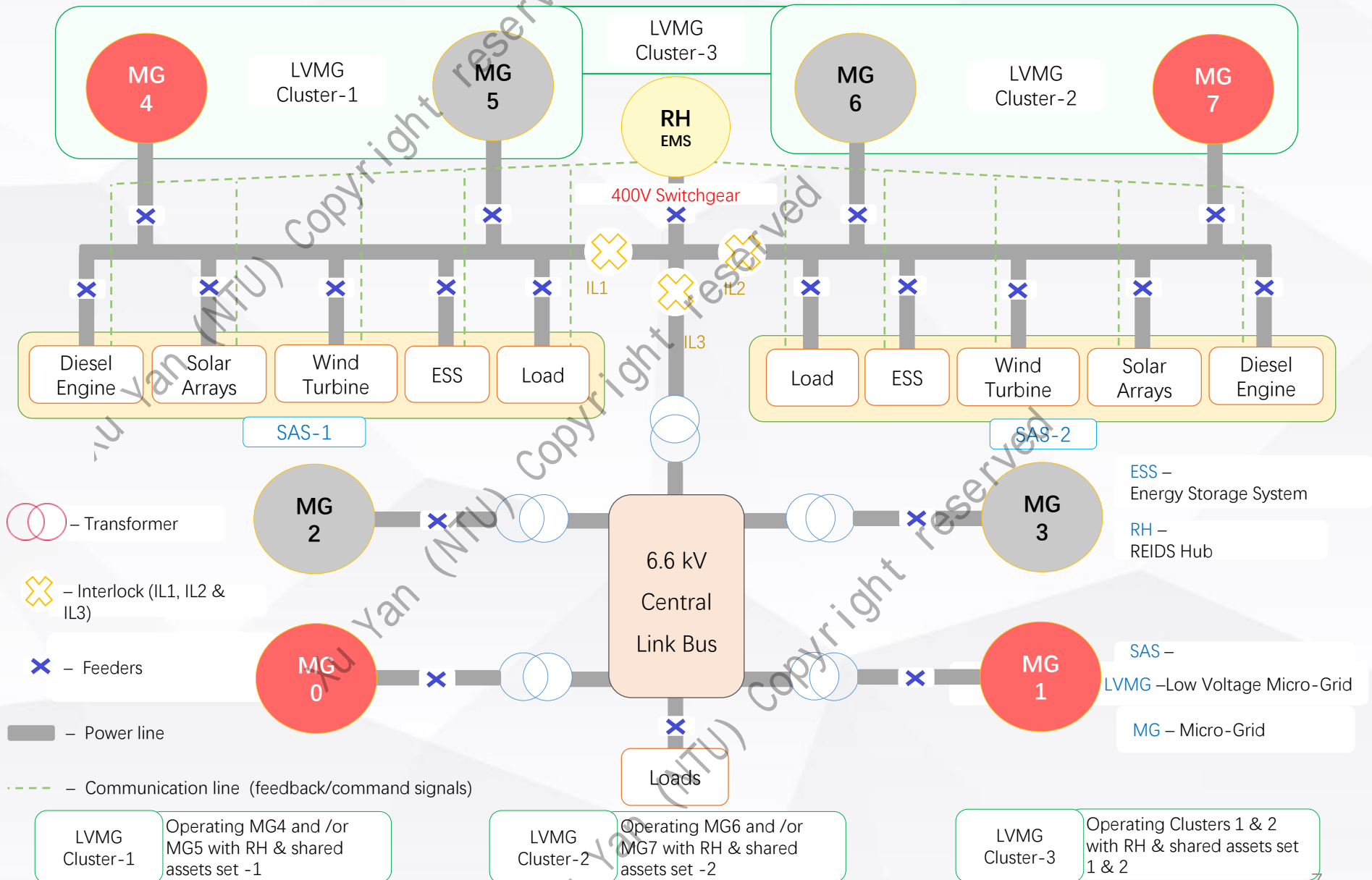
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

REIDS Electrical Structure



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Onsite pictures



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Onsite pictures



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

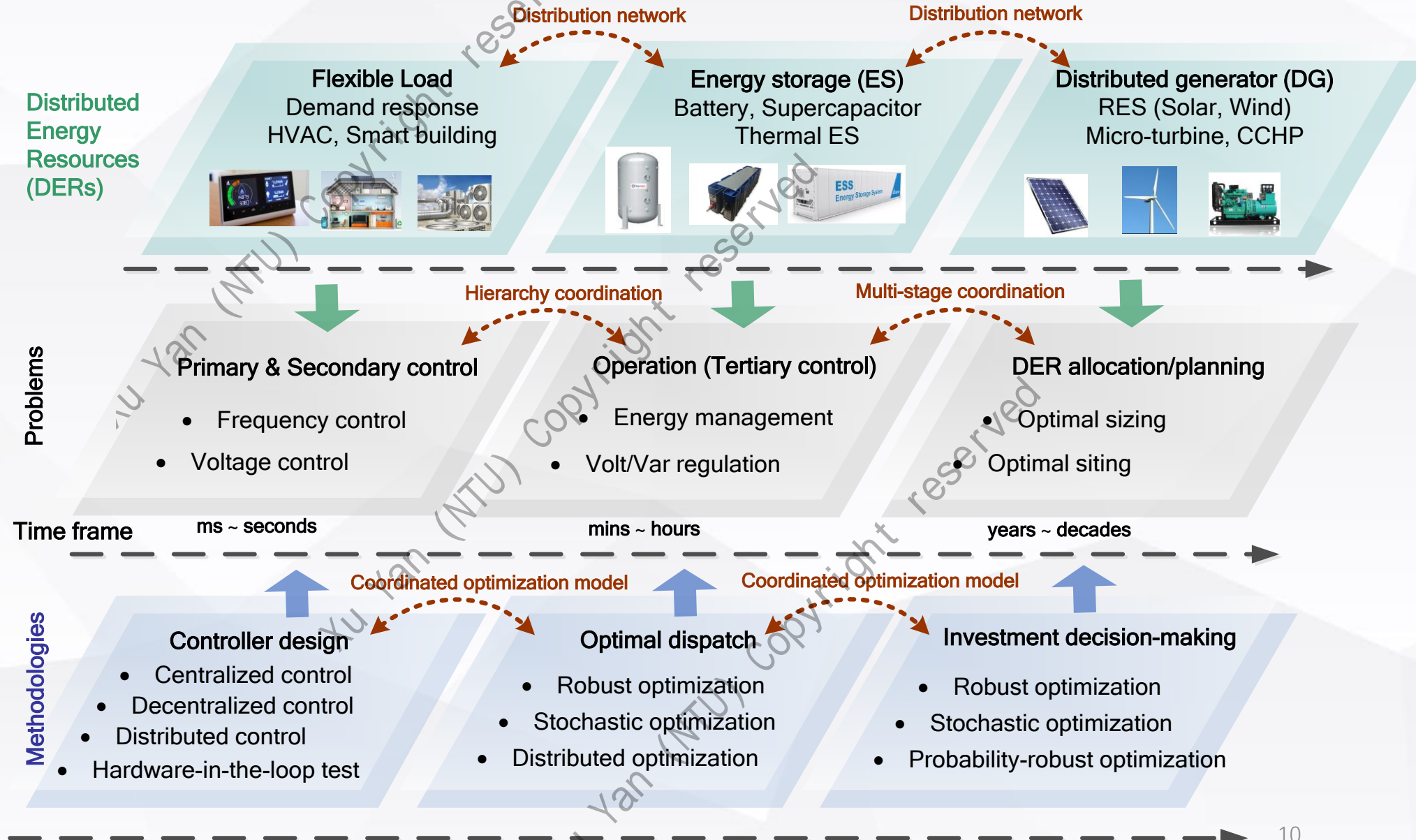
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Our research Framework: system-level coordination of DERs



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

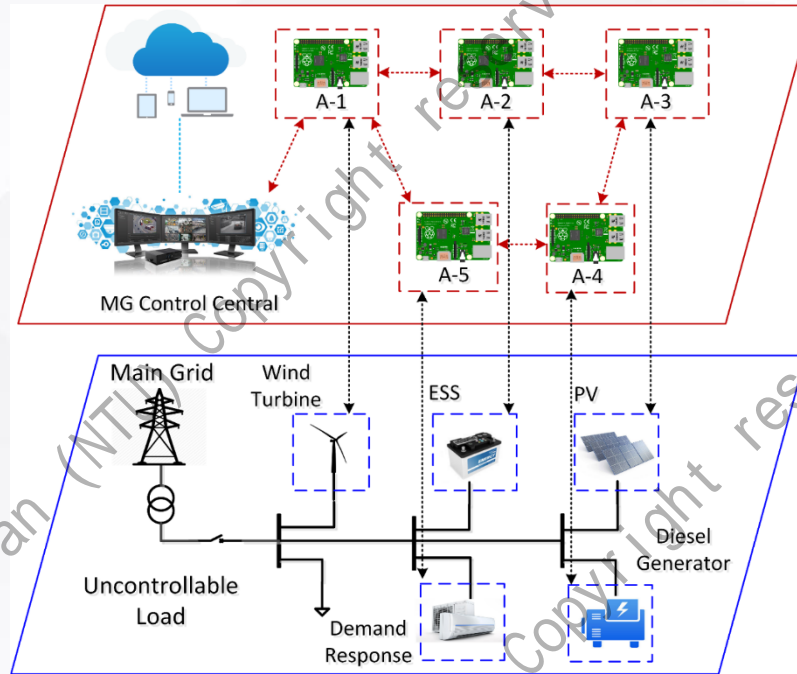
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Control of DERs in Microgrids

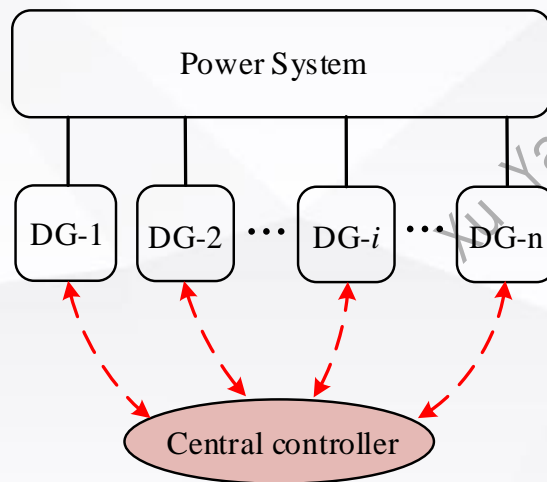


1. Islanded mode:

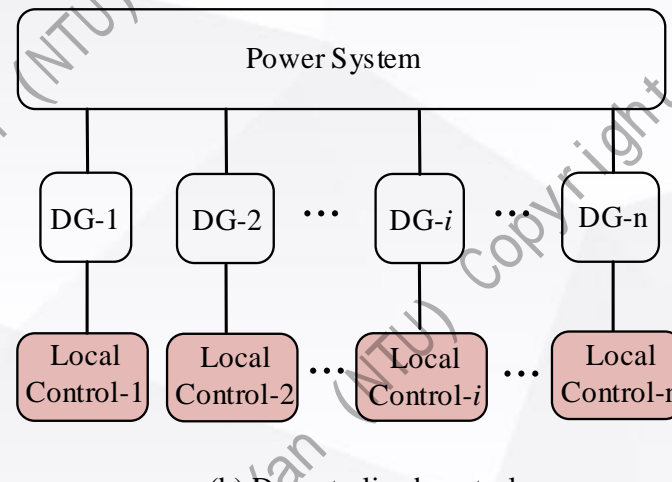
- Distributed control (event-triggered, finite-time)
- Hardware-in-the-Loop (Hil) validation

2. Grid-connected mode:

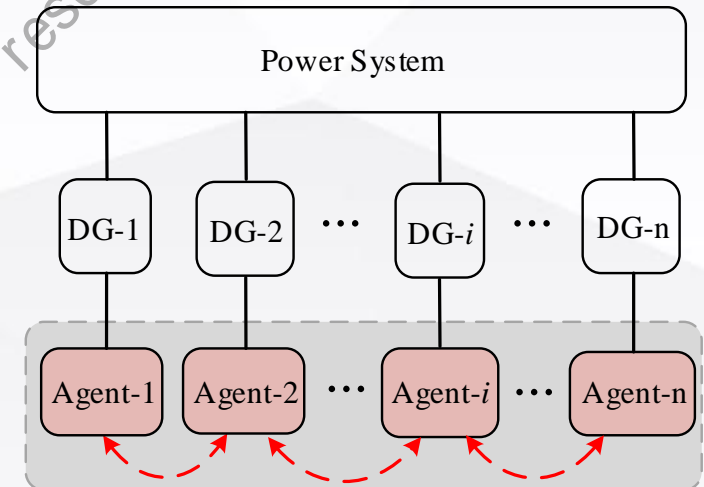
- DER for f support
- DER for V support



(a) Centralized control



(b) Decentralized control



(c) Distributed control

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

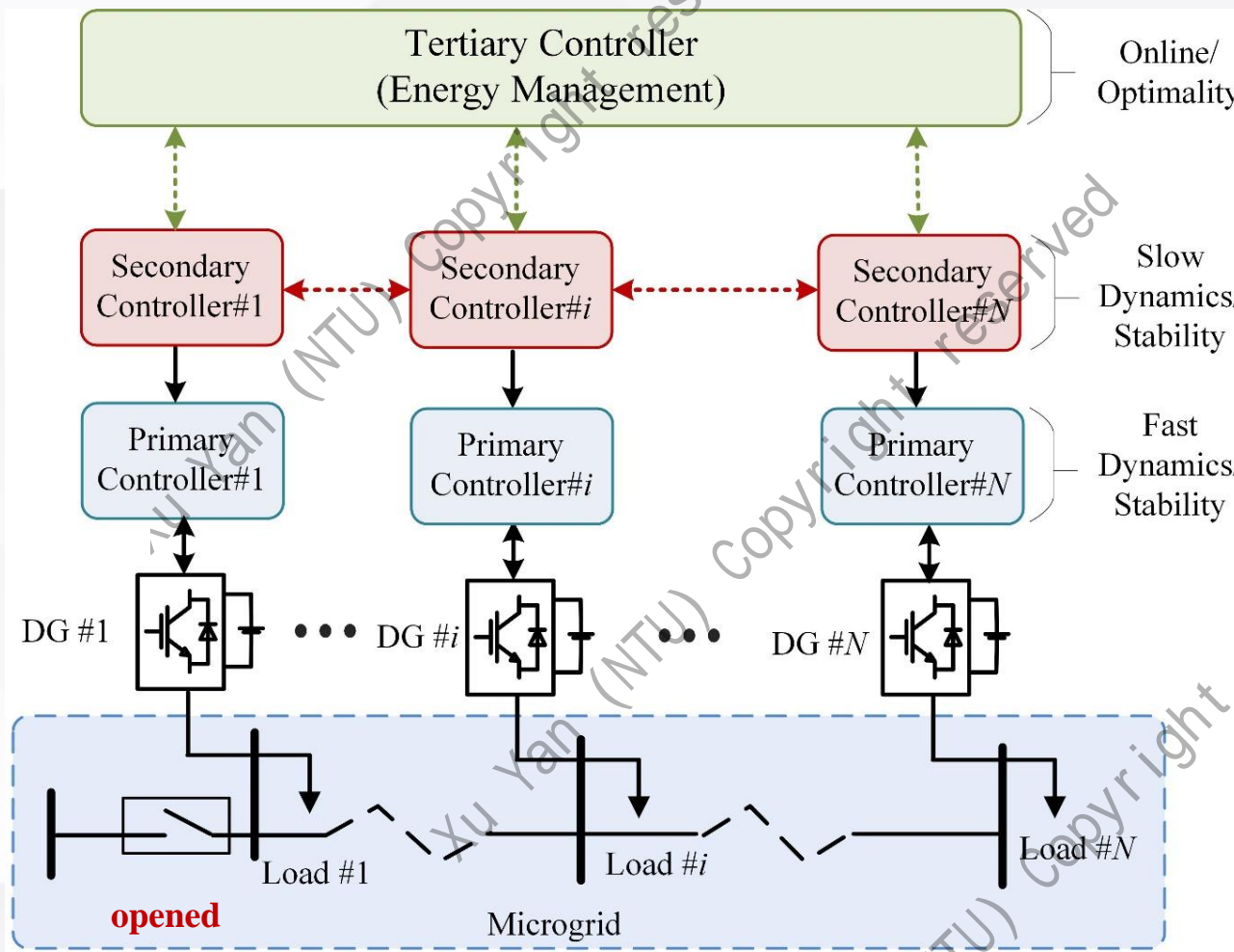
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

▪ Hierarchical control of an islanded microgrid



- **Tertiary control (centralized or distributed)**
 - Economic dispatch, optimal power flow.
- **Secondary control (centralized or distributed)**
 - V/f restoration and accurate power balancing
- **Primary control (decentralized)**
 - Inner control loops and droop control
 - Local V/f regulation and power sharing

Hierarchical control framework of islanded microgrids

0. Outline

1. REIDS Project

2. Control

1) Islanded mode

2) Grid-tied mode

3. Operation

1) Energy dispatch

2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

1) DG planning

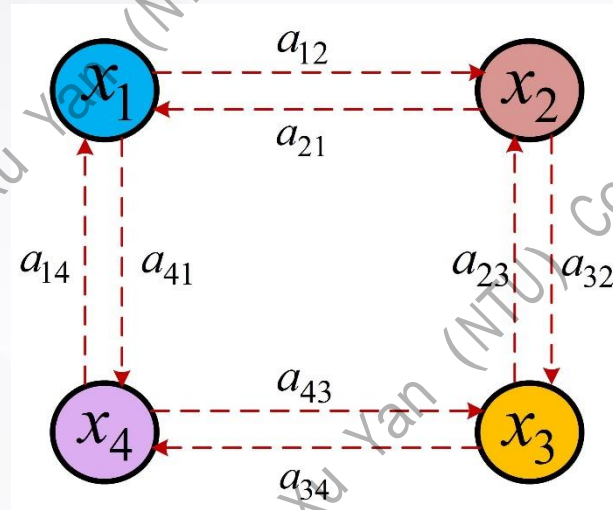
2) ESS planning

3) PRO algorithm

▪ Distributed Control – Spatial Coordination of DERs

- ✓ No need for a central controller
- ✓ One node only communicates with neighbouring nodes
- ✓ Share communication and computation burden among nodes
- ✓ Higher resilience, plug-and-play, scalability, data privacy

Example of communication graph



Adjacent matrix of the graph

$$A = \begin{bmatrix} 0 & a_{12} & 0 & a_{14} \\ a_{21} & 0 & a_{23} & 0 \\ 0 & a_{32} & 0 & a_{34} \\ a_{41} & 0 & a_{43} & 0 \end{bmatrix}$$

a) Average consensus control

$$\dot{x}_i(t) = \sum_{j \in N_i} a_{ij}(t)(x_j(t) - x_i(t))$$

$$\lim_{t \rightarrow \infty} \|x_i(t) - x_j(t)\| = 0$$

b) Leader-follower consensus control

$$\dot{x}_i(t) = \sum_{j=1}^n a_{ij}(t)(x_j(t) - x_i(t)) + g_i(x_0(t) - x_i(t)).$$

$$\lim_{t \rightarrow \infty} \|x_i(t) - x_0(t)\| = 0$$

0. Outline

1. REIDS Project

2. Control

1) Islanded mode

2) Grid-tied mode

3. Operation

1) Energy dispatch

2) Volt/Var regulation

4. Hierarchy coordination

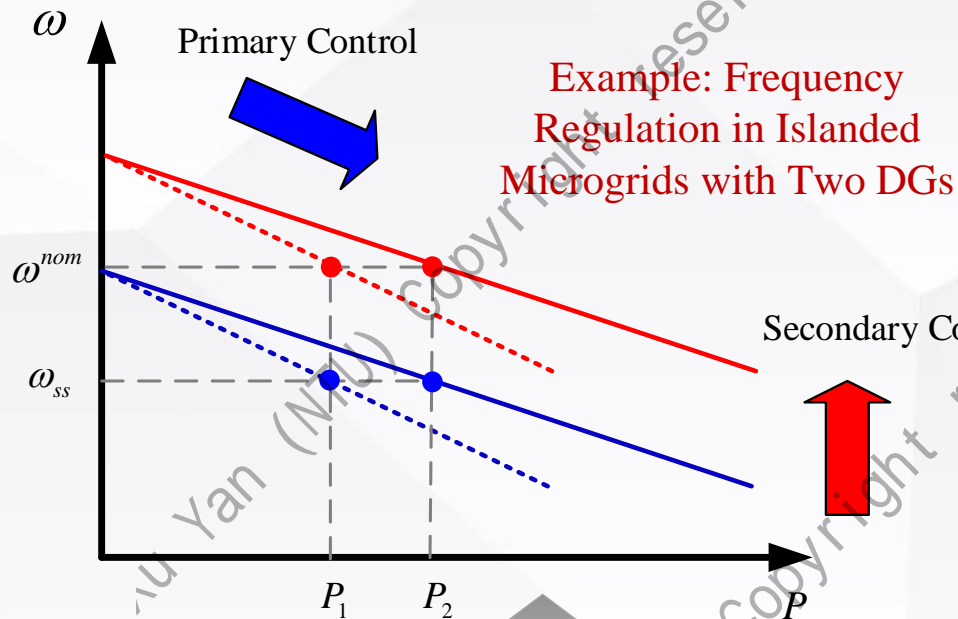
5. Planning

1) DG planning

2) ESS planning

3) PRO algorithm

Secondary Controller Design – Principle



Droop control

$$\omega_i = \omega_i^{\text{nom}} - m_i^P P_i$$

$$V_i = V_i^{\text{nom}} - m_i^Q Q_i$$

Taking Derivative

$$\dot{\omega}_i = \dot{\omega}_i^{\text{nom}} - m_i^P \dot{P}_i$$

$$\dot{V}_i = \dot{V}_i^{\text{nom}} - m_i^Q \dot{Q}_i$$

Problem formulation

$$\omega^{\text{nom}} = \int (\dot{\omega}_i + m_i^P \dot{P}_i) dt = \int (u_i^\omega + u_i^P) dt$$

$$V^{\text{nom}} = \int (\dot{V}_i + m_i^Q \dot{Q}_i) dt = \int (u_i^V + u_i^Q) dt$$

Apply consensus control rule

$$u_i^\omega = \sum_{j=1}^N a_{ij} (\omega_j - \omega_i) + g_i (\omega^{\text{ref}} - \omega_i)$$

$$u_i^P = \sum_{j=1}^N a_{ij} (m_j^P P_j - m_i^P P_i)$$

$$u_i^V = \sum_{j=1}^N a_{ij} (V_j - V_i) + g_i (V^{\text{ref}} - V_i)$$

$$u_i^Q = \sum_{j=1}^N a_{ij} (m_j^Q Q_j - m_i^Q Q_i)$$

0. Outline

1. REIDS Project

2. Control

1) Islanded mode

2) Grid-tied mode

3. Operation

1) Energy dispatch

2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

1) DG planning

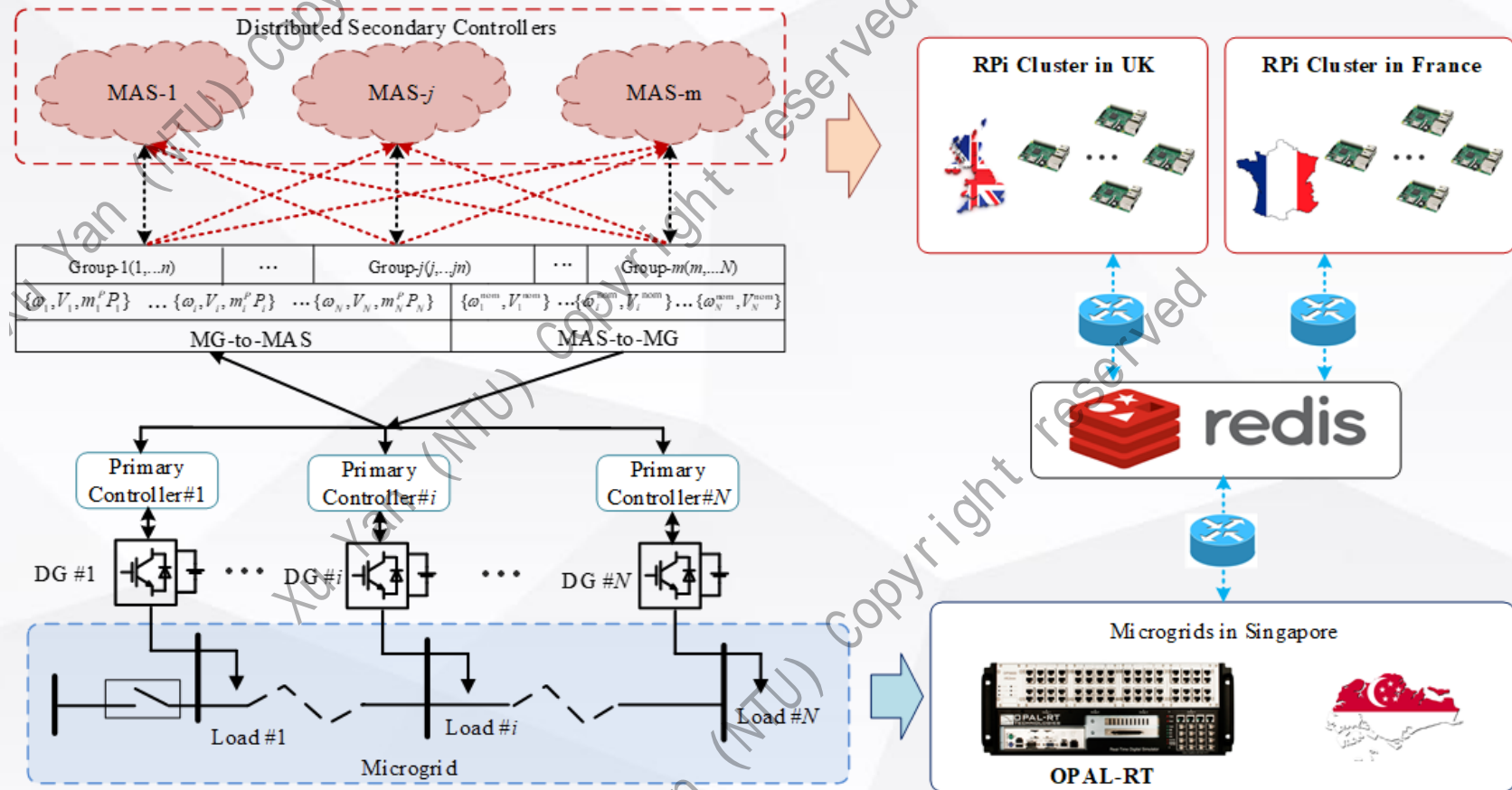
2) ESS planning

3) PRO algorithm

- Cross-national hardware-in-the-loop (HiL) testbed

Jointly developed by NTU (Singapore), University of Strathclyde (UK), and G2E Lab (France)

- Microgrids system with OPAL-RT in Singapore.
- Distributed controllers in Raspberry Pi in UK and France.
- Software environment based on gRPC and data exchange via Redis cloud server.



Y. Wang, T. L. Nguyen, M. H. Syed, **Y. Xu***. "A Distributed Control Scheme of Microgrids in Energy Internet and Its Multi-Site Implementation." *IEEE Transactions on Industrial Informatics*, 2020.

0. Outline

1. REIDS Project

2. Control

1) Islanded mode

2) Grid-tied mode

3. Operation

1) Energy dispatch

2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

1) DG planning

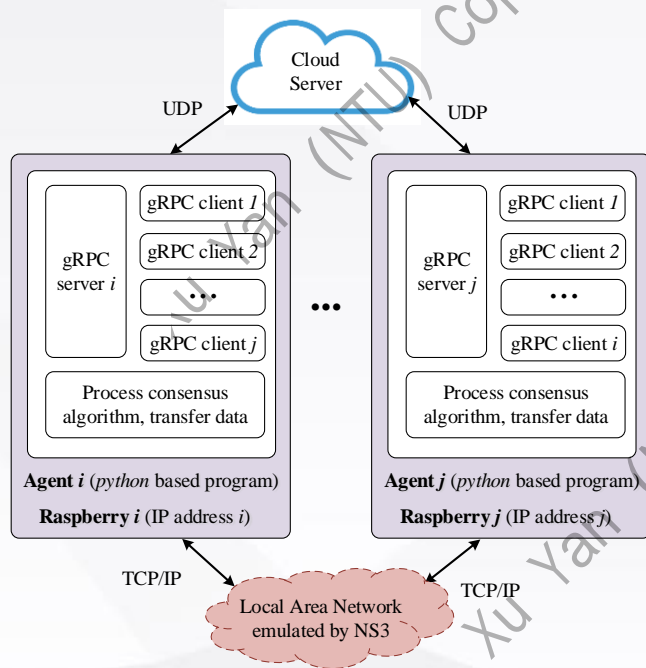
2) ESS planning

3) PRO algorithm

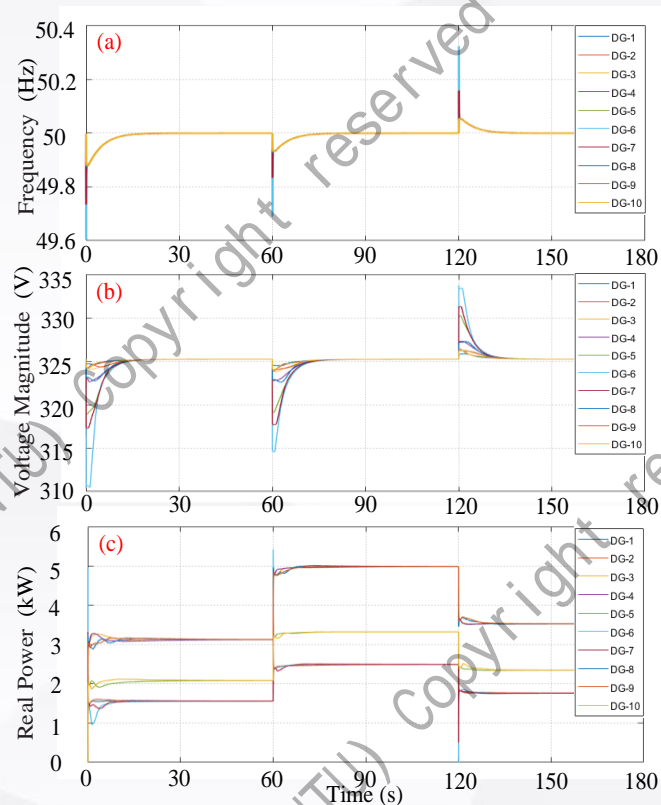
HiL Validation Results – Controller performance

**Test system: 10-DG with two controller in UK and France
(Each controller for 5 DGs)**

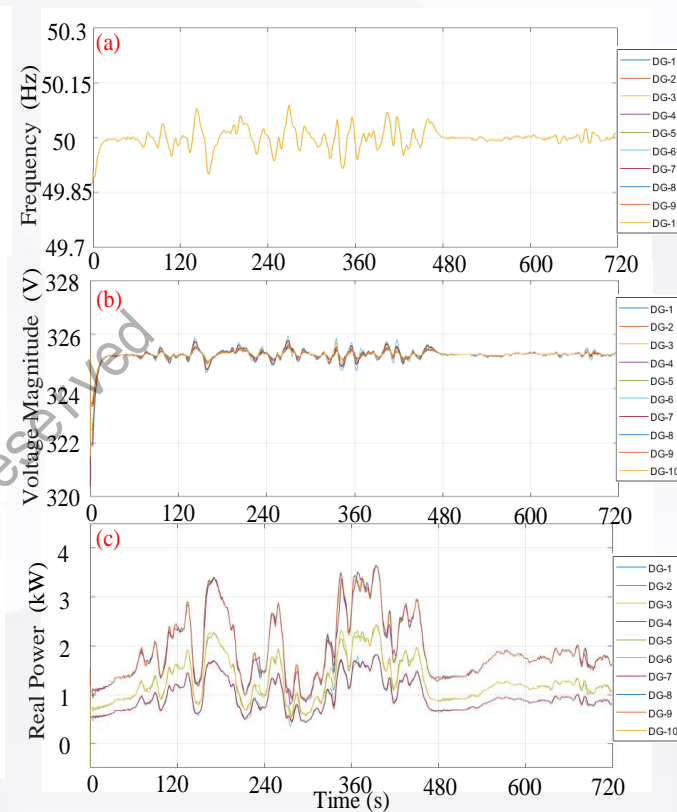
Structure of each agent based on gRPC



a) step load change case



b) Real PV and load profile case



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

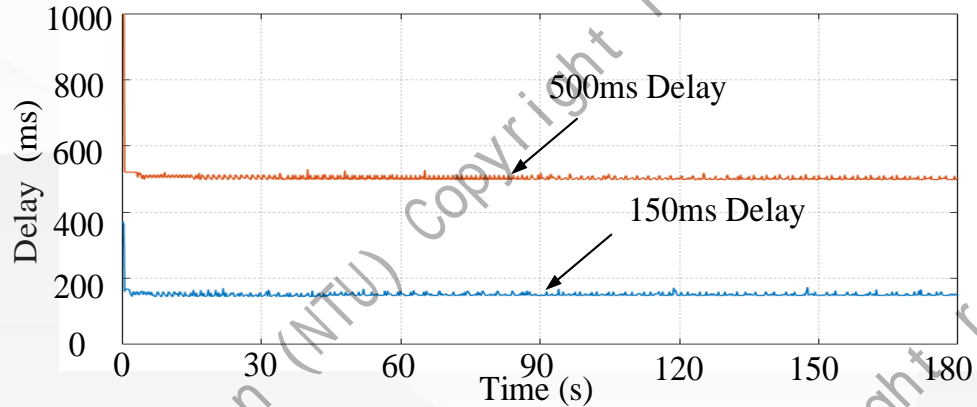
4. Hierarchy coordination

5. Planning

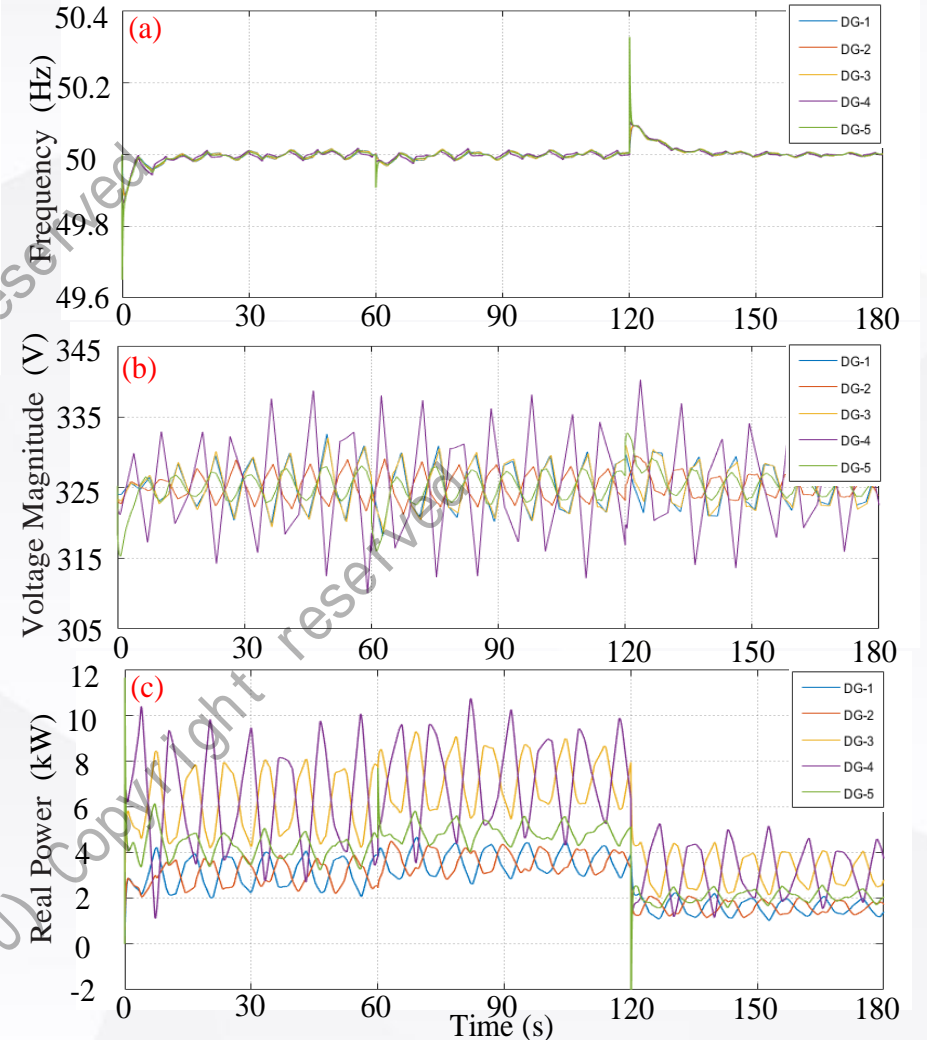
- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

HiL Validation Results – Communication delay

Communication delay emulated by NS3 simulation tools.



Test system: 5-DG MG with one MAS in UK



System oscillation under large delay, which can be mitigated by tuning the control gain.

- ✓ Larger control gain -> converge faster -> withstand smaller delay.
- ✓ Smaller control gain -> converge slower -> withstand larger delay

0. Outline

1. REIDS Project

2. Control

1) Islanded mode

2) Grid-tied mode

3. Operation

1) Energy dispatch

2) Volt/Var regulation

4. Hierarchy coordination

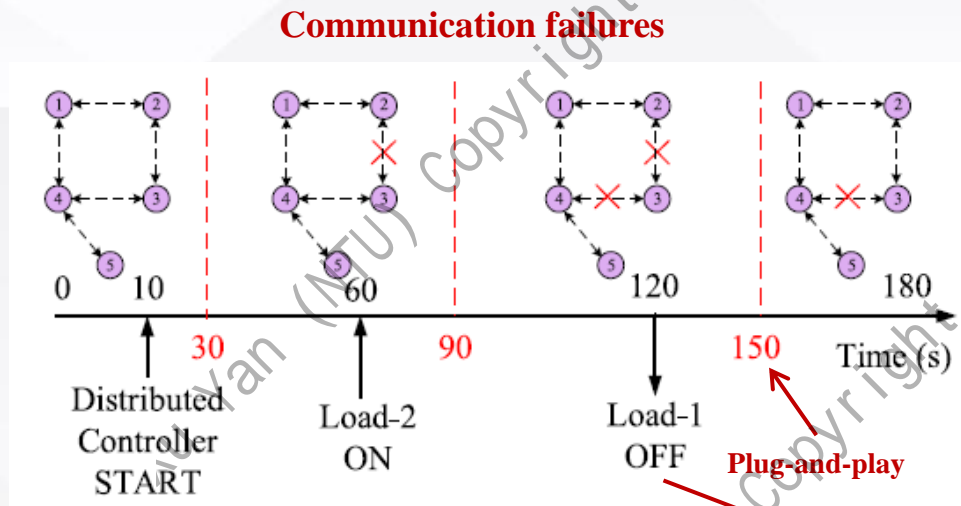
5. Planning

1) DG planning

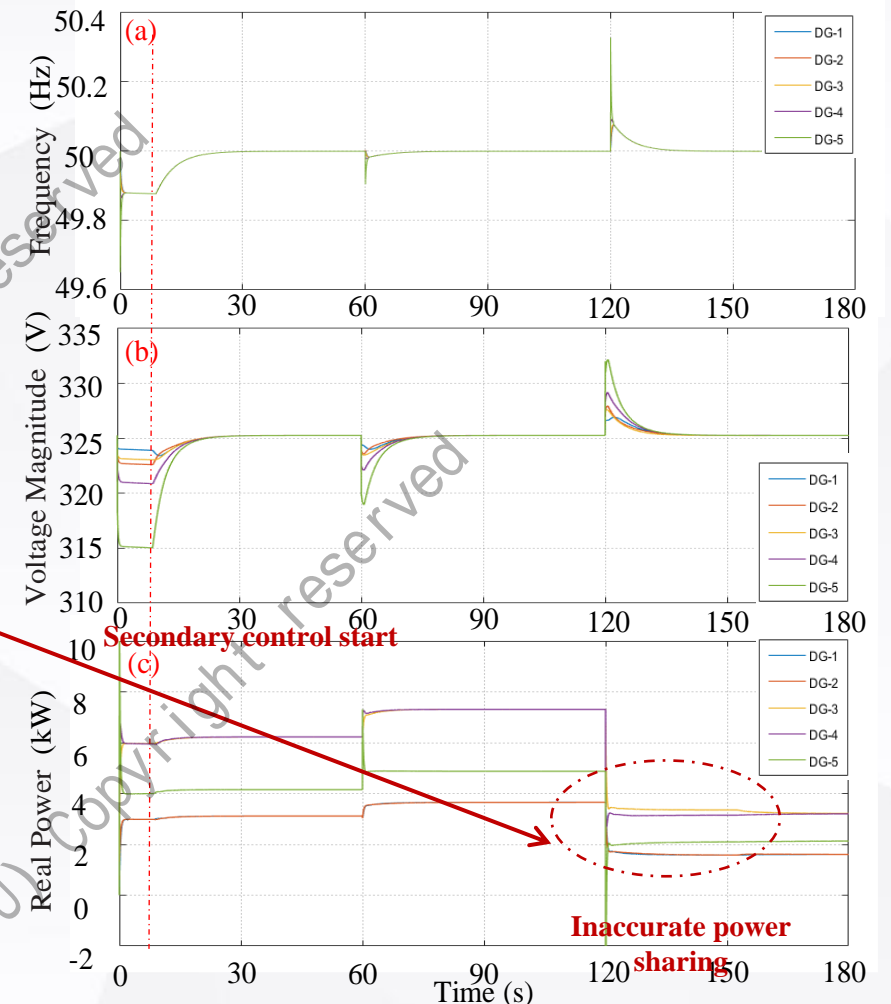
2) ESS planning

3) PRO algorithm

HiL Validation Results – Communication failures



Test system: 5-DG MG with one controller in UK



- ✓ Failure of communication will affect the convergence speed
- ✓ Loss of communication will lead to inaccurate power sharing

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

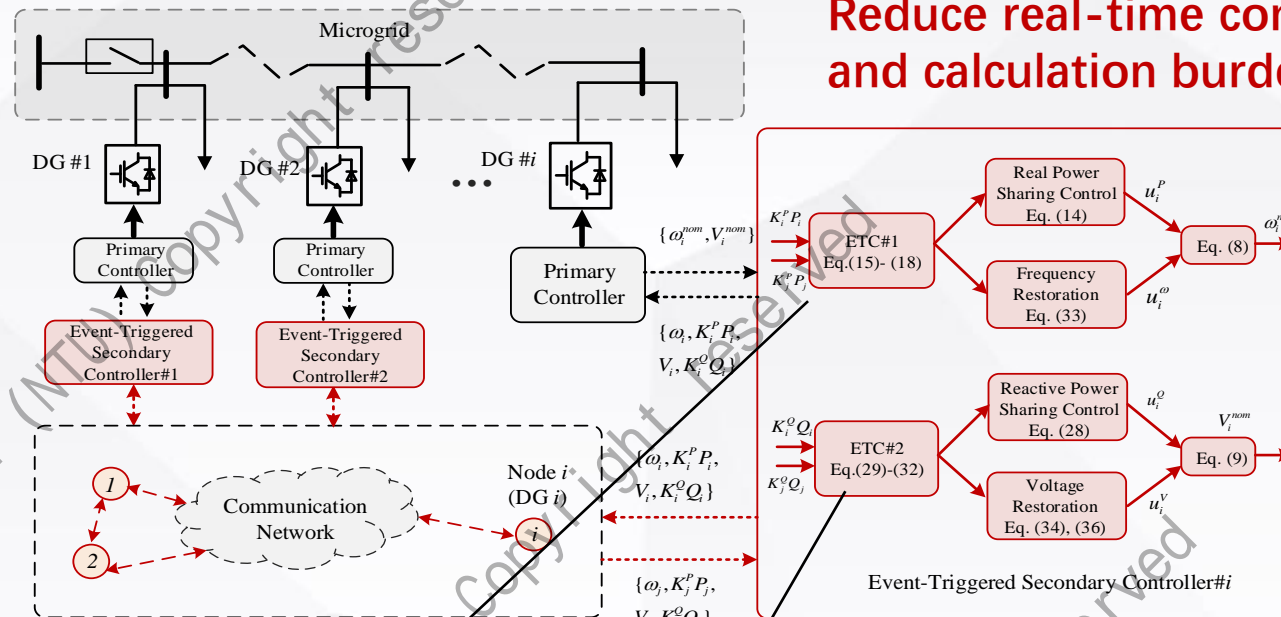
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Event-Triggered Distributed Control of Islanded Microgrids



Reduce real-time communication and calculation burden

Event-Trigger Condition for f and P :

$$f_i^P(t) = \|e_i^P(t)\|^2 - \frac{\sigma_i^P \alpha^P (1 - \alpha^P d_i)}{d_i} \|\delta_i^P(t)\|^2$$

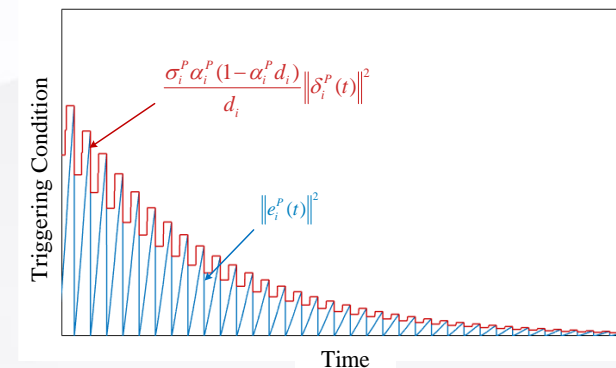
$$t_k^{Pi} = \inf\{t > t_{k-1}^{Pi} \mid f_i^P(t) = 0\}$$

Event-Trigger Condition for V and Q :

$$f_i^Q(t) = \|e_i^Q(t)\|^2 - \frac{\sigma_i^Q \alpha^Q (1 - \alpha^Q d_i)}{d_i} \|\delta_i^Q(t)\|^2$$

$$t_k^{Qi} = \inf\{t > t_{k-1}^{Qi} \mid f_i^Q(t) = 0\}$$

Effects of ETC



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

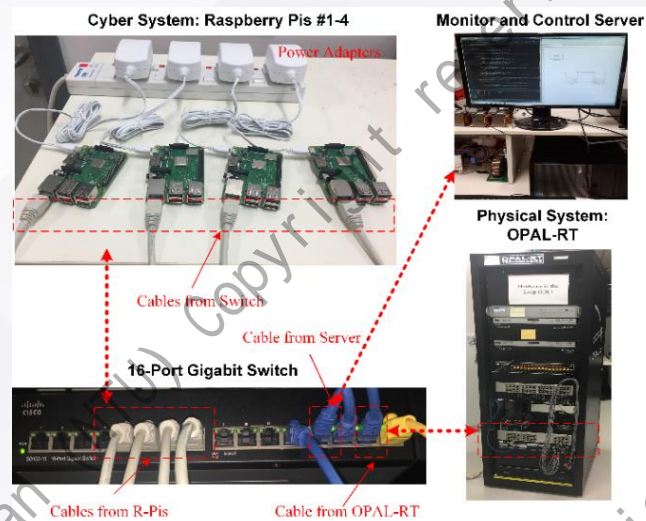
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

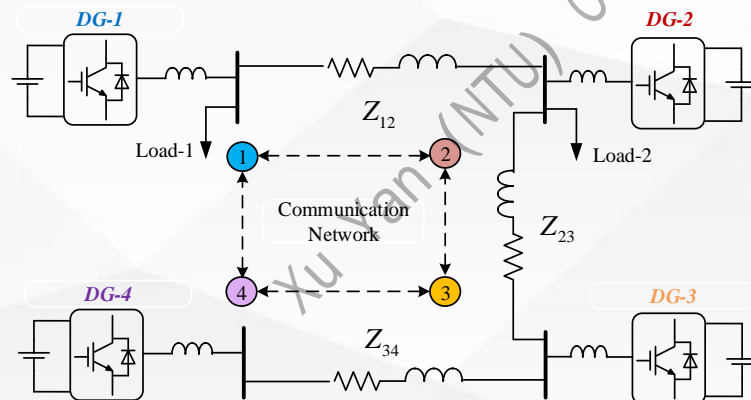
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

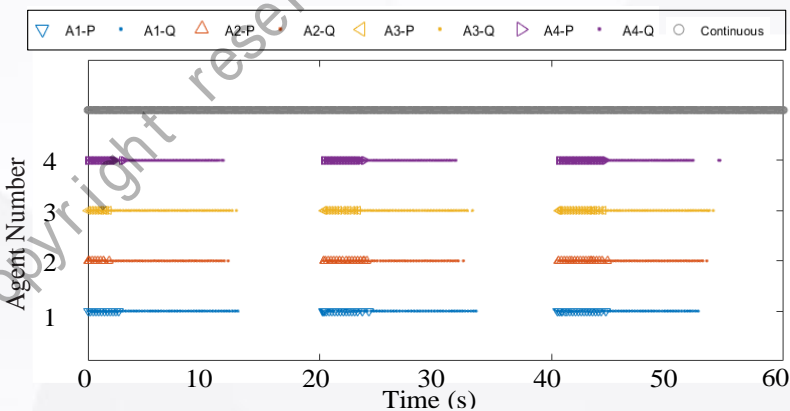
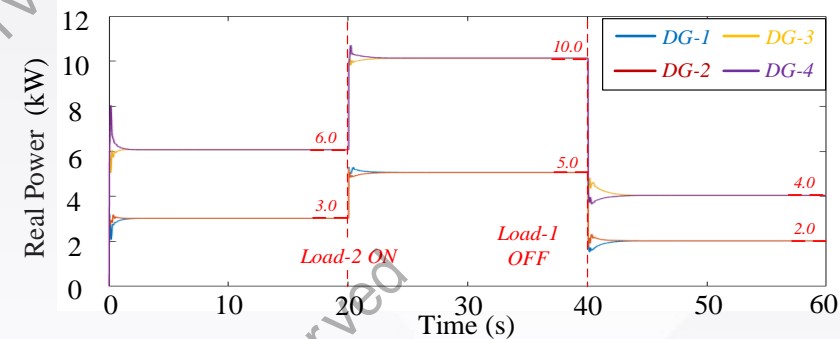
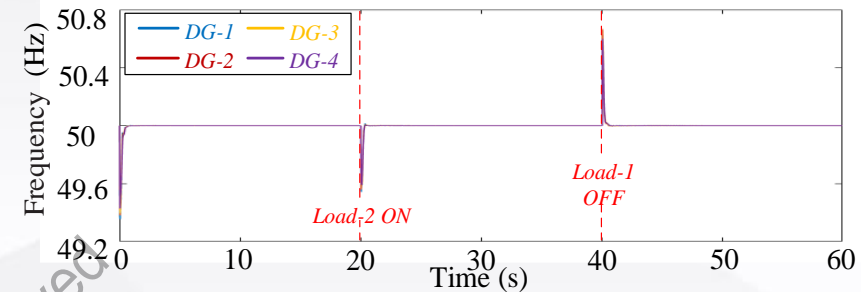
Controller Hardware-in-the-Loop (CHiL) Test



HiL testbed with Raspberry Pi and OPAL-RT



Microgrid topology with four DGs



Communication requirement

Y. Wang, T. L. Nguyen, Y. Xu*, et al, "Cyber-Physical Design and Implementation of Distributed Event-Triggered Secondary Control in Islanded Microgrids," *IEEE Trans. Industry Application*, 2019.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

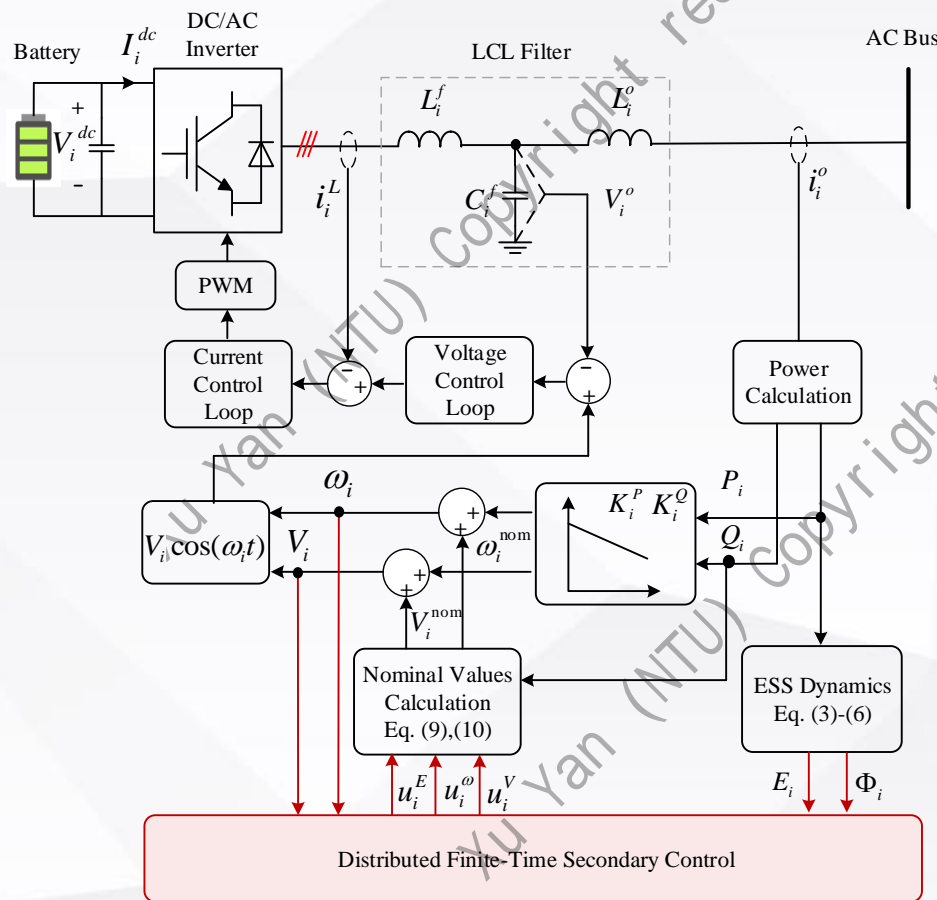
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Finite-Time Distributed Control of Energy Storage Systems



Control diagram of one ESS unit

Finite-time consensus control law

$$u_i^E = c_1 \text{sig}(\sum_{j=1}^N a_{ij}(E_j - E_i))^{\alpha_1} + c_2 \text{sig}(\sum_{j=1}^N a_{ij}(\Phi_j - \Phi_i))^{\alpha_2}$$

$$e_i^\omega = \sum_{j=1}^N a_{ij}(\omega_j - \omega_i) + g_i(\omega^{ref} - \omega_i)$$

$$e_i^V = \sum_{j=1}^N a_{ij}(V_j - V_i) + g_i(V^{ref} - V_i)$$

Control objectives

$$\lim_{t \rightarrow T^E} |\Phi_i(t) - \Phi_j(t)| = 0, \lim_{t \rightarrow T^E} |E_i(t) - E_j(t)| = 0$$

$$\Phi_i(t) = \Phi_j(t), E_i(t) = E_j(t) \forall t \geq T^E$$

$$\lim_{t \rightarrow T^\omega} |\omega_i(t) - \omega^{ref}| = 0, \omega_i(t) = \omega^{ref}, \forall t \geq T^\omega$$

$$\lim_{t \rightarrow T^V} |V_i(t) - V^{ref}| = 0, V_i(t) = V^{ref}, \forall t \geq T^V$$

Y. Wang, T. L. Nguyen, **Y. Xu***, D. Shi, "Distributed control of heterogeneous energy storage systems in islanded microgrids: Finite-time approach and cyber-physical implementation," *Int. J. Electrical Power & Energy Systems*, 2020.

0. Outline

1. REIDS Project

2. Control

1) Islanded mode

2) Grid-tied mode

3. Operation

1) Energy dispatch

2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

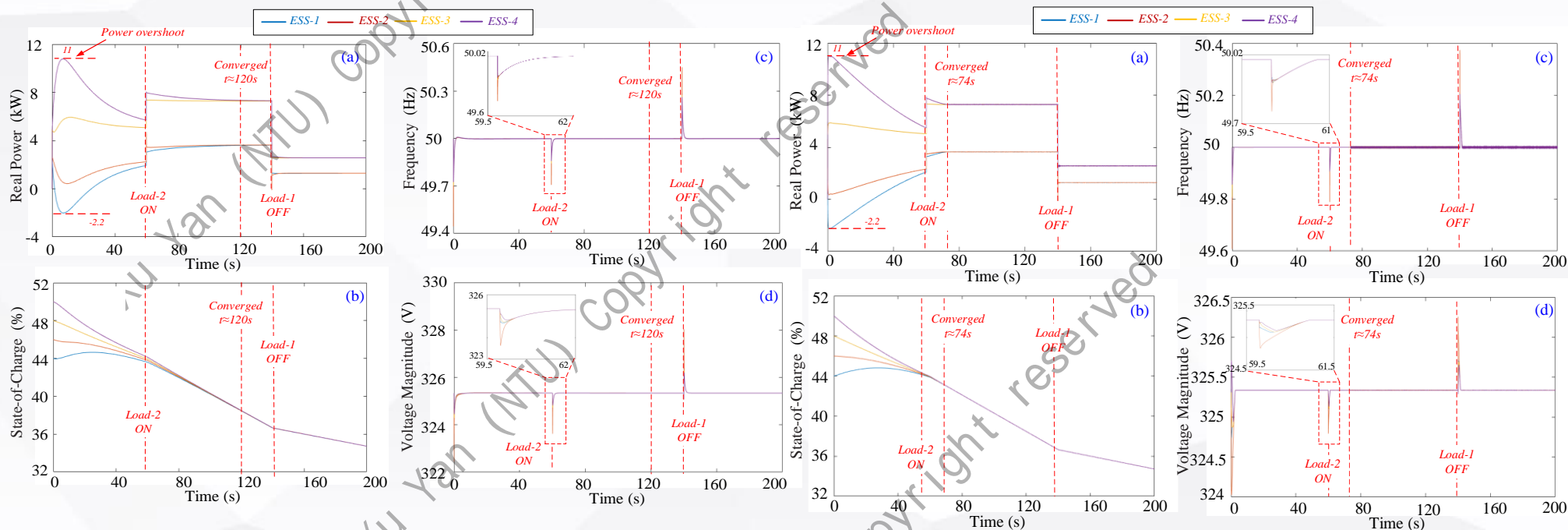
1) DG planning

2) ESS planning

3) PRO algorithm

Finite-Time Distributed Control of Energy Storage Systems

Under the same power overshoot, the proposed controller converges much faster (74s vs 120s)



Linear consensus control

Finite-time consensus control

Y. Wang, T. L. Nguyen, Y. Xu*, D. Shi, "Distributed control of heterogeneous energy storage systems in islanded microgrids: Finite-time approach and cyber-physical implementation," *Int. J. Electrical Power & Energy Systems*, 2020.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

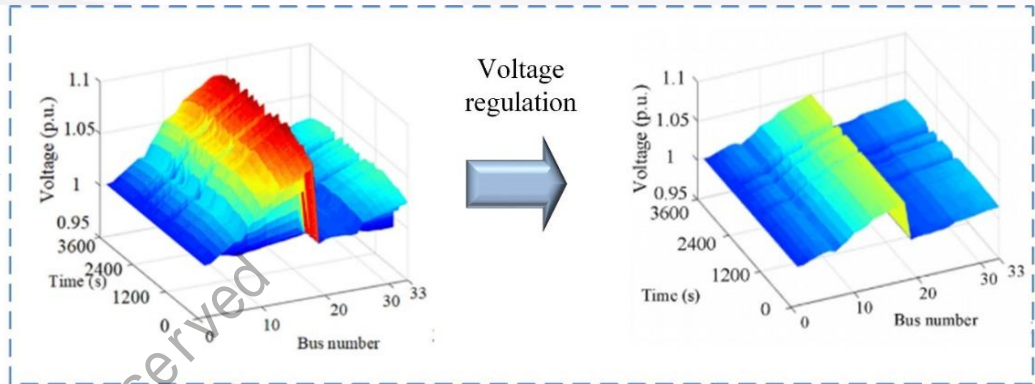
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

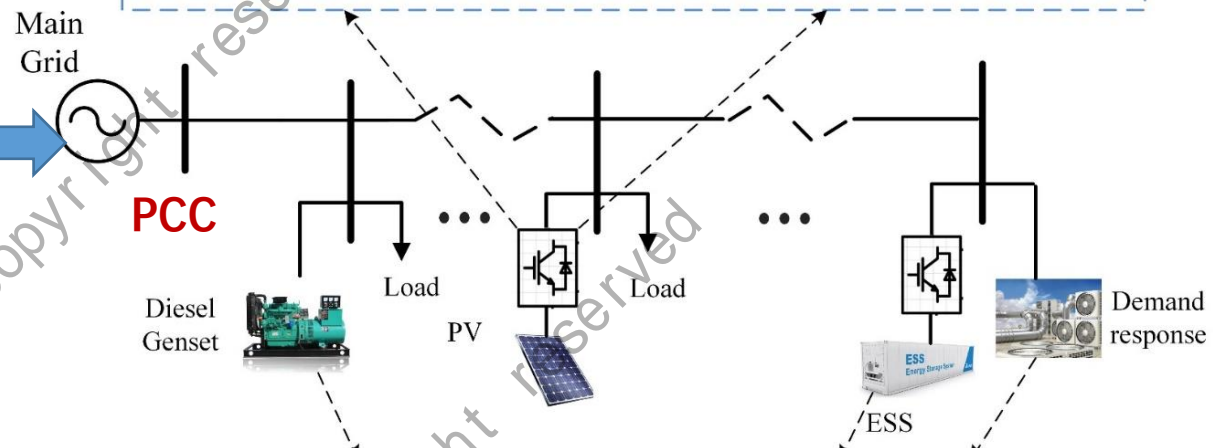
- Grid-connected mode of Microgrids (DER support)

Voltage control support:

mitigate voltage deviation
(seconds to minutes)

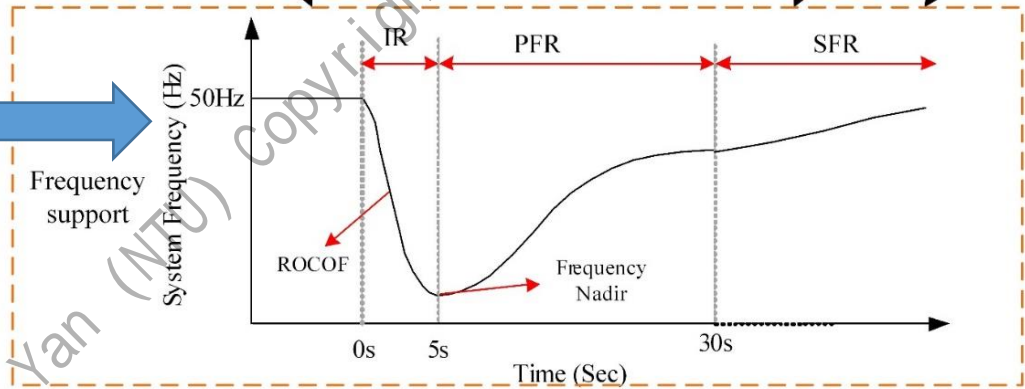


Frequency and voltage are dominated by the main grid through point of coupling connection (PCC).



Frequency control support:

mitigate frequency variation
(ms to seconds)



0. Outline

1. REIDS Project

2. Control

- 1) Isolated mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

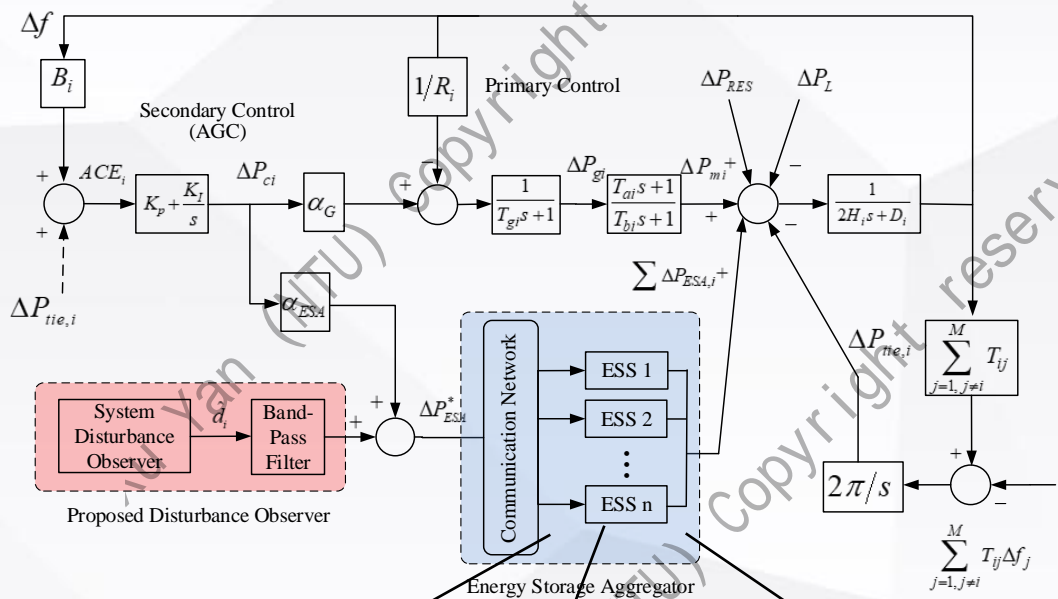
4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Frequency Support from Aggregated Energy Storage

Proposed load frequency control (LFC) framework



$$\Delta \dot{f}_i(t) = -\frac{D_i}{2H_i} \Delta f_i(t) + \frac{1}{2H_i} (\Delta P_{mi}(t) - \Delta P_{L,i}(t) + \Delta P_{RES,i}(t) - \Delta P_{tie,i}(t) + \Delta P_{ESA,i}(t))$$

$$\Delta \dot{P}_{mi}(t) = -\frac{1}{T_{bi}} \Delta P_{mi}(t) + \frac{1}{T_{bi}} \Delta P_{gi}(t) + \frac{T_{ai}}{T_{bi}} \Delta \dot{P}_{gi}(t)$$

$$\Delta \dot{P}_{gi}(t) = -\frac{1}{T_{gi}} \Delta P_{gi}(t) + \frac{1}{T_{gi}} \Delta P_{ci}(t) - \frac{1}{R_i T_{gi}} \Delta f_i(t)$$

$$\Delta \dot{P}_{tie,i}(t) = 2\pi \cdot \left[\sum_{j=1, j \neq i}^M T_{ij} (\Delta f_i(t) - \Delta f_j(t)) \right]$$

$$ACE_i(t) = B_i \Delta f_i(t) + \Delta P_{tie,i}(t)$$

$$\Delta P_{ci}(t) = -K_p ACE_i(t) - K_I \int ACE_i(t)$$



Lead acid battery



Lithium ion battery

...



Vanadium redox battery

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

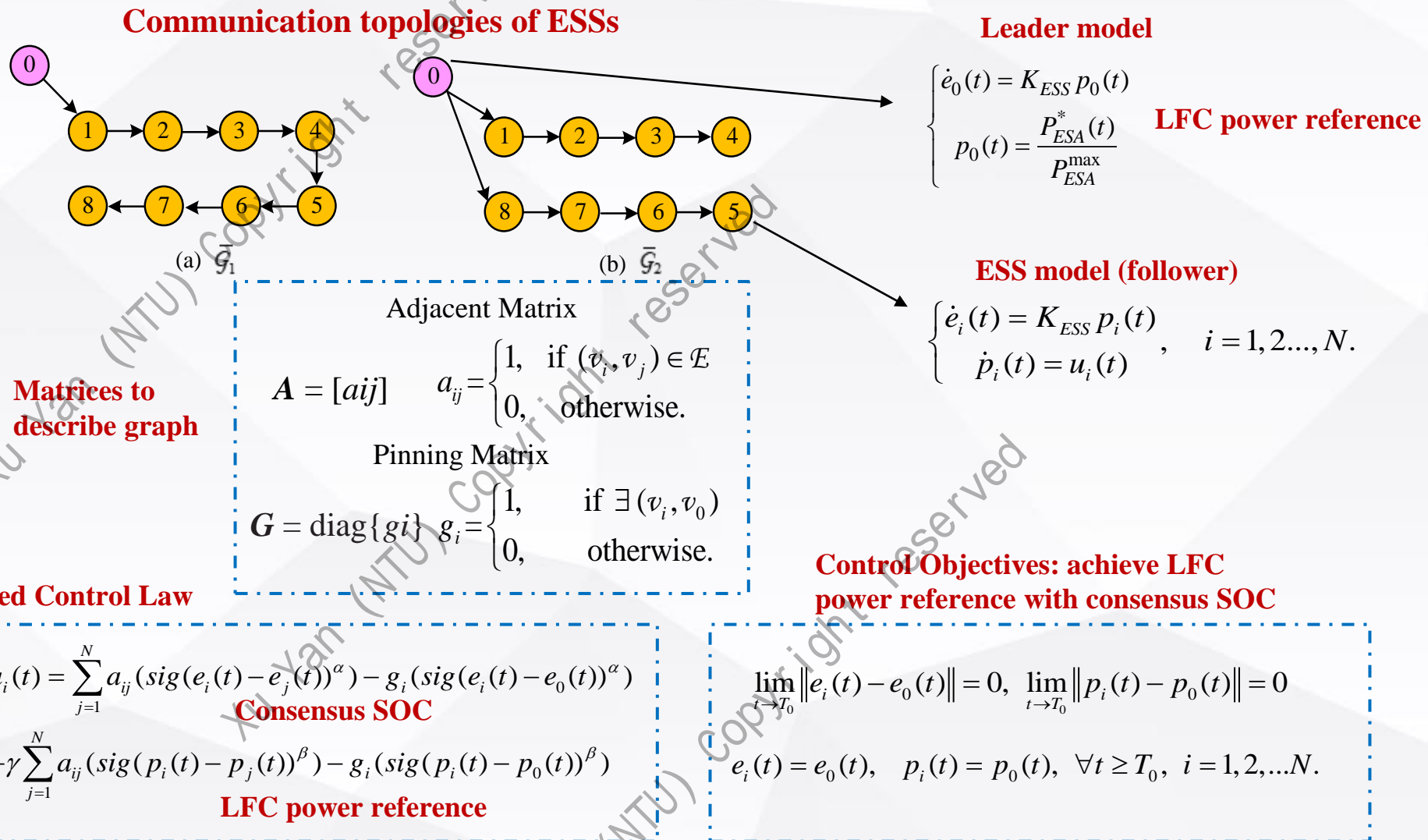
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Frequency Support from Aggregated Energy Storage



Y. Wang, **Y. Xu***, Y. Tang, et al "Aggregated Energy Storage for Power System Frequency Control: A Finite-Time Consensus Approach," *IEEE Trans. Smart Grid*, May 2018,

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

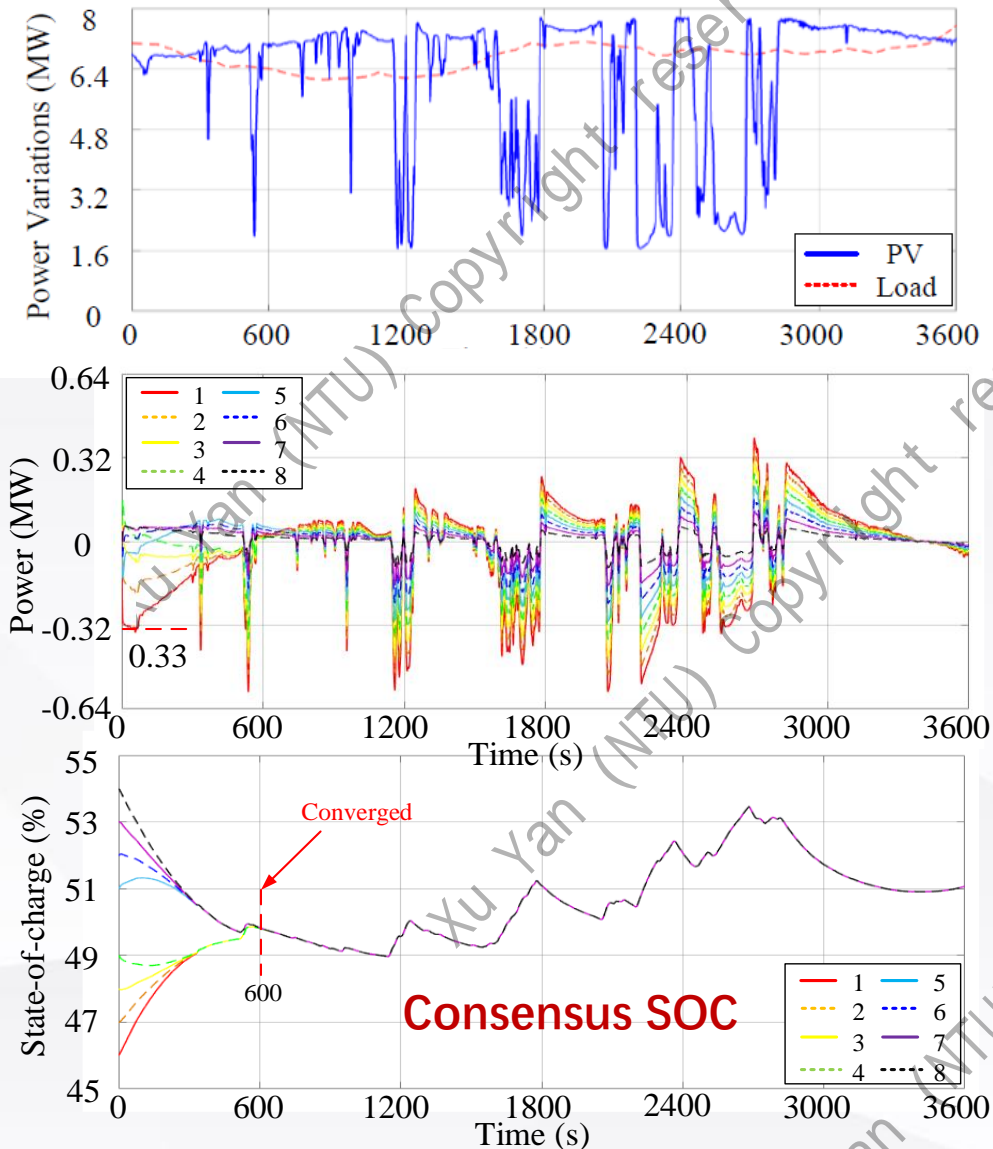
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

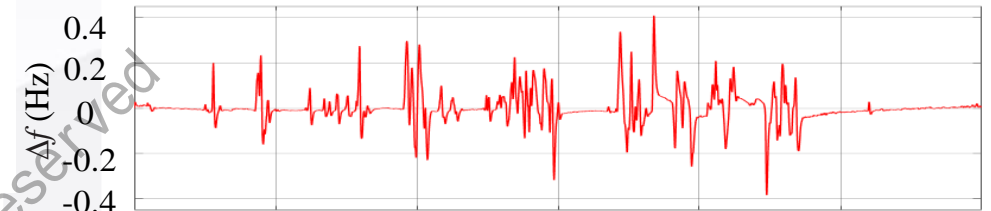
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

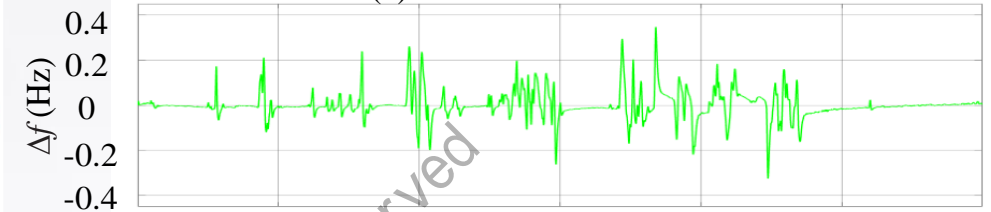
Simulation Results



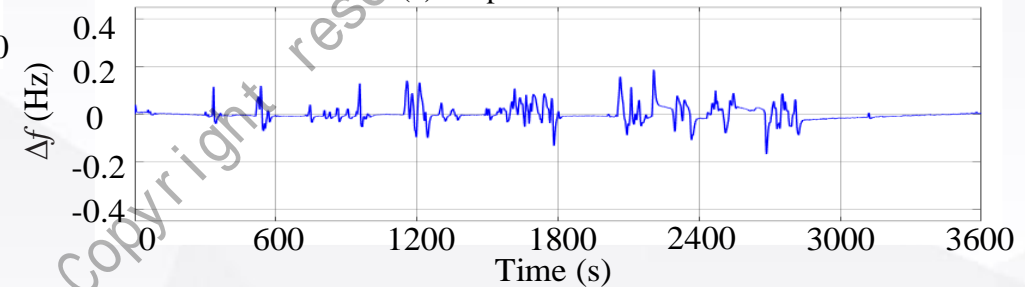
(a) Conventional LFC scheme



(b) LFC with ESA w/o observer



(c) Proposed control scheme



Y. Wang, Y. Xu*, Y. Tang, et al "Aggregated Energy Storage for Power System Frequency Control: A Finite-Time Consensus Approach," *IEEE Trans. Smart Grid*, May 2018.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Thermostatically Controlled Loads (TCLs) for frequency support

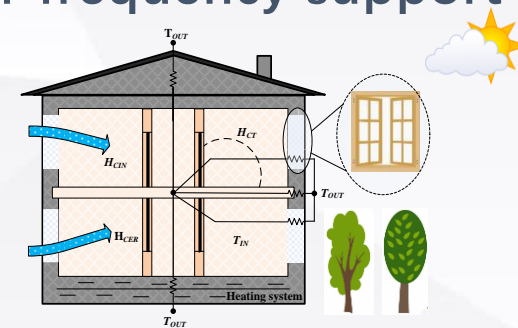
Temperature dynamics of TCL:

$$C_{th} \frac{dT_i(t)}{dt} = \frac{T_a(t) - T_i(t)}{R_{th}} - \eta \bar{P} \alpha_i(t), \quad i \in \mathcal{G}.$$

Heat exchange with the ambient

Thermal energy from VFAC

Assume power state α_i is a continuous variable from 0 to 1.



Comfort zone of TCL:

$$\beta_i(t) = \frac{T_i(t) - T_s + \Delta T}{2\Delta T}, \quad i \in \mathcal{G}$$

Comfort state β_i is an index from 0 to 1.

State-space model of TCL:

$$\underbrace{\begin{bmatrix} \frac{d\alpha_i(t)}{dt} \\ \frac{d\beta_i(t)}{dt} \end{bmatrix}}_{\dot{x}_i} = \underbrace{\begin{bmatrix} 0 & 0 \\ -\frac{2\Delta T}{C_{th}R_{th}} & -\frac{\eta \bar{P}}{C_{th}} \end{bmatrix}}_A \underbrace{\begin{bmatrix} \alpha_i \\ \beta_i \end{bmatrix}}_{x_i} + \underbrace{\begin{bmatrix} 1 \\ 0 \end{bmatrix}}_B u_i + \underbrace{\begin{bmatrix} 0 \\ \frac{T_a(t) - T_s + \Delta T}{C_{th}R_{th}} \end{bmatrix}}_W$$

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

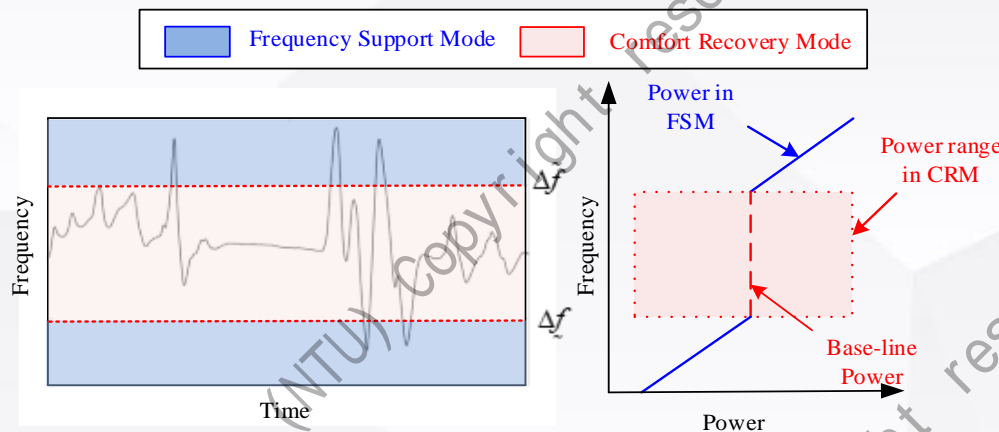
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

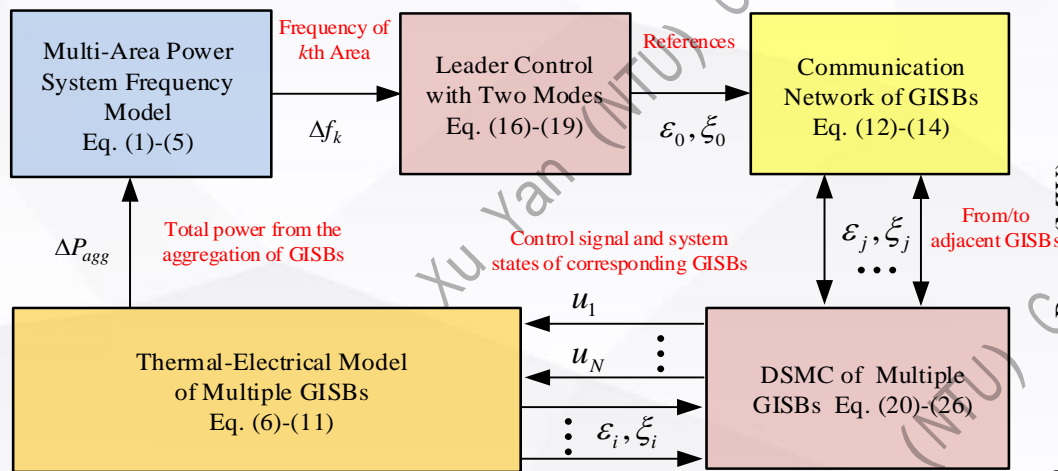
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

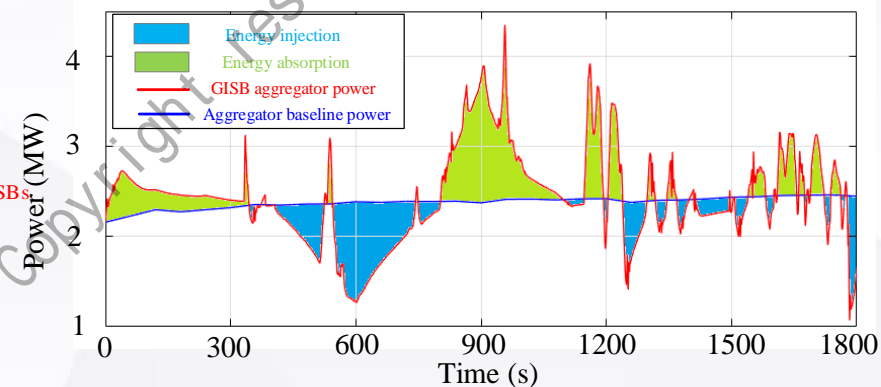
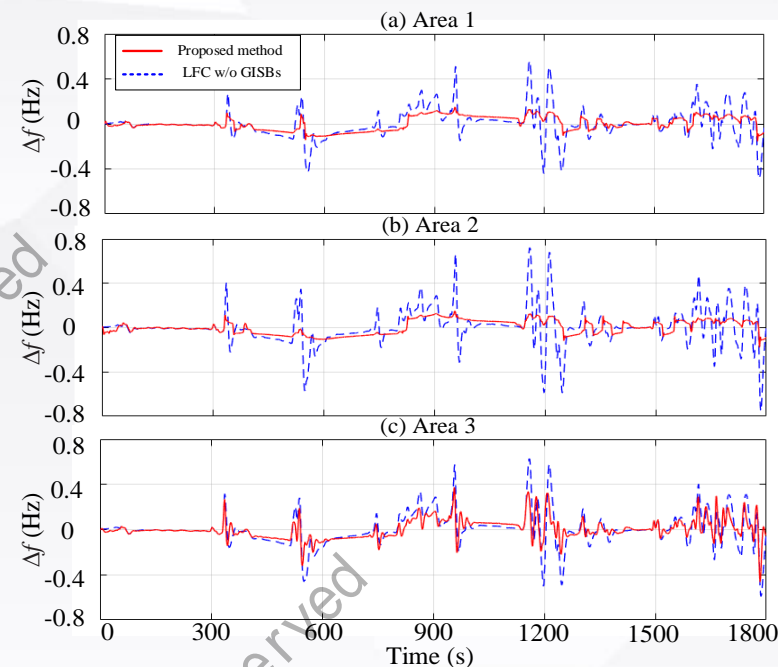
Thermostatically Controlled Loads (TCLs) for frequency support



Leader control mode: f support mode and comfort recover mode



Leader-follower consensus controller



Y. Wang, Y. Xu, and Y. Tang, "Distributed Aggregation Control of Grid-Interactive Smart Buildings for Power System Frequency Support," *Applied Energy*, 2019.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

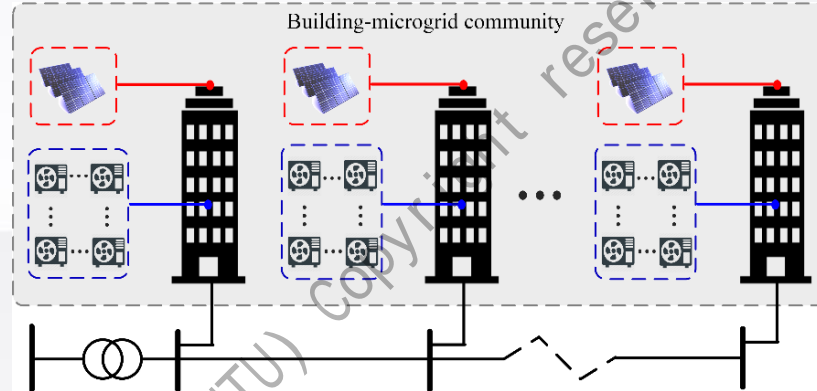
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

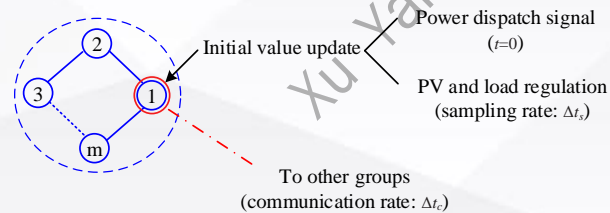
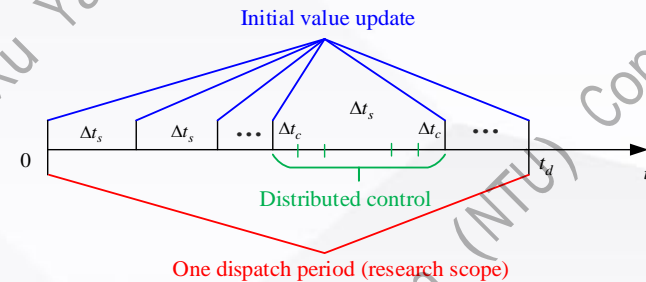
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

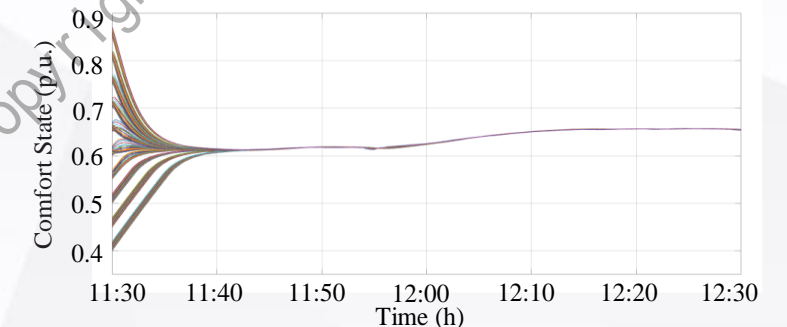
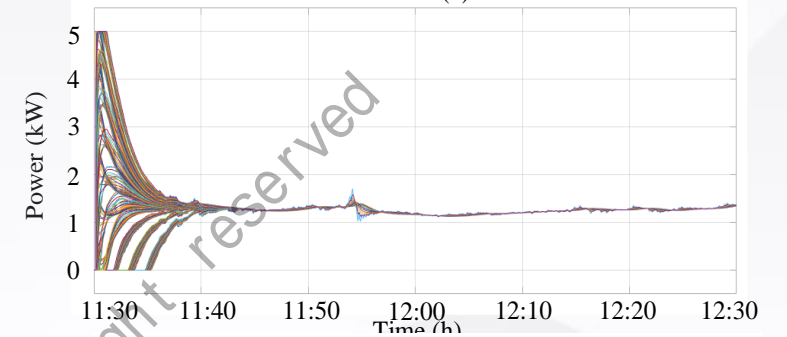
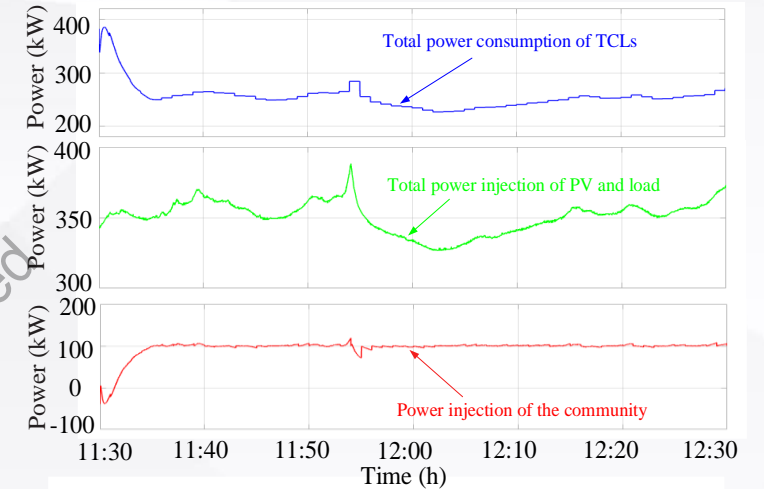
Ancillary Service Support from Smart Building Community



Smart building community:
TCLs+PVs



Initial value updating scheme



Y. Wang, Y. Tang, **Y. Xu***, et al, "A Distributed Control Scheme of Thermostatically Controlled Loads for Building-Microgrid Community," *IEEE Trans. Sustainable Energy*, 2019.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

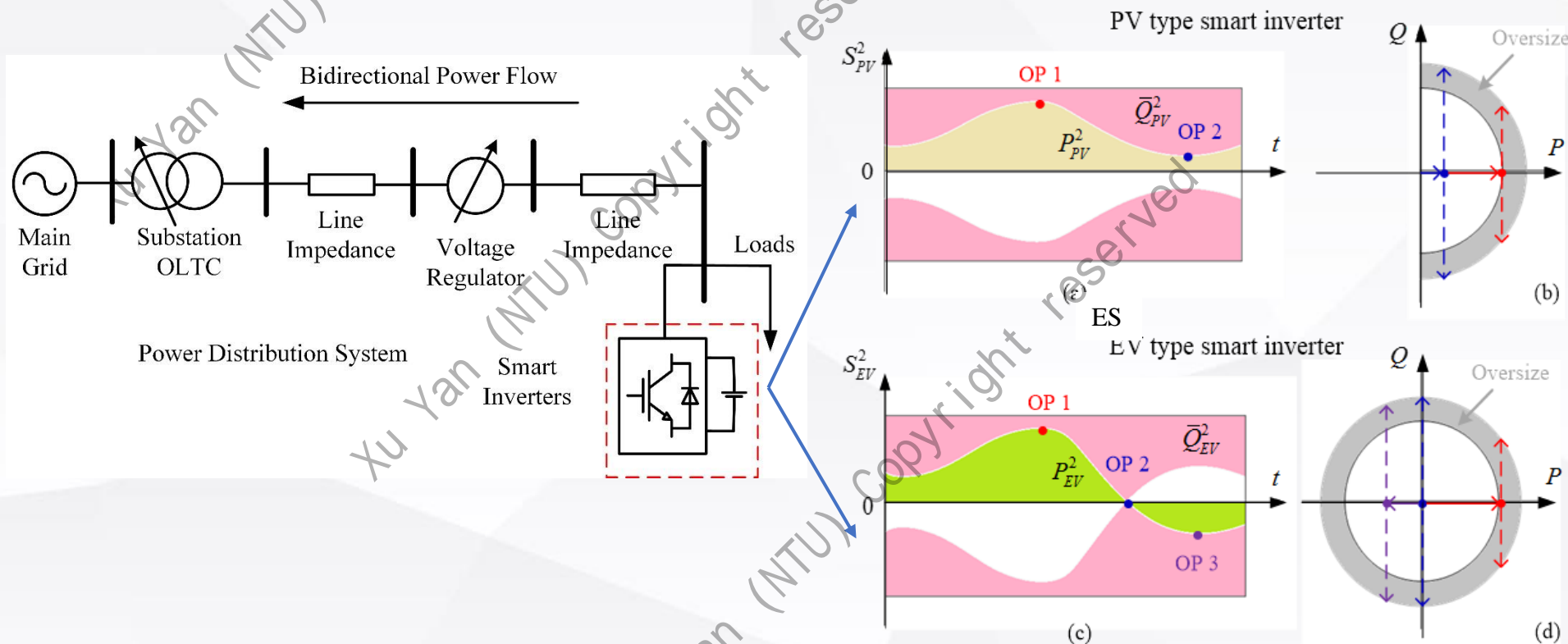
4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Real-time Voltage/Var Control (VVC) Support from DERs

- Existing Challenges: High PV penetration level, massive EV charging.
- Voltage quality issues: Voltage rise, drop and fast fluctuations.
- Potential solutions: inverter-assisted voltage/var support



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

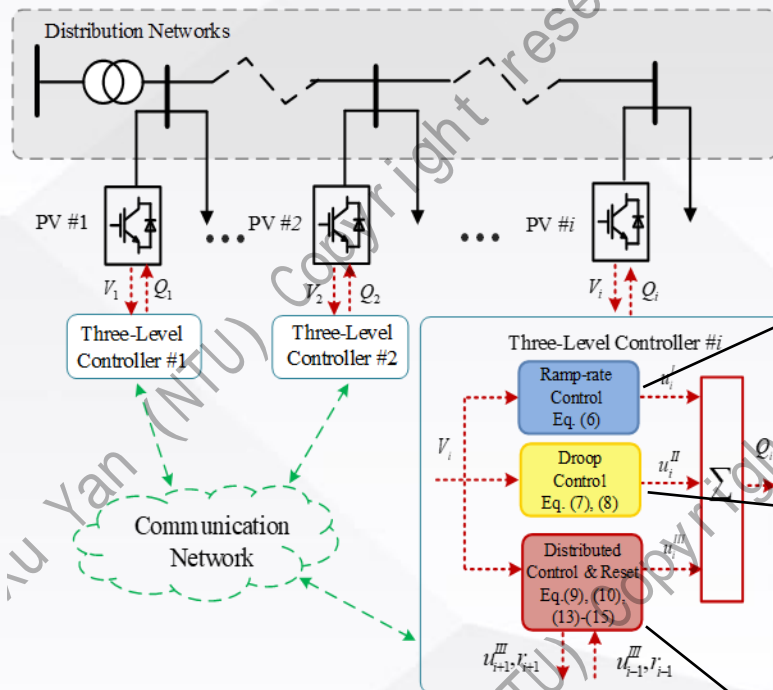
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Real-Time Coordinated Voltage/Var Control Controller



Controller design:

Level I: Ramp-rate Control -> smooth voltage fluctuation

$$u_i^I(t) = K_i^I \left[V_i(t) - \frac{\sum_{j=t-\omega}^t V_i(j)}{T(t) - T(t-\omega)} \right]$$

Level II: Droop Control -> immediate voltage support

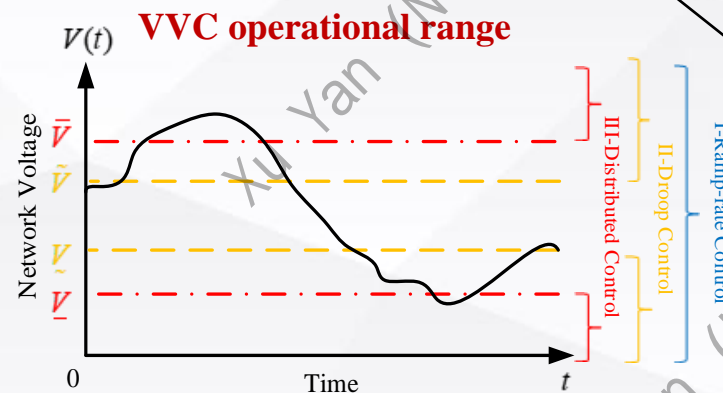
$$u_i^{II}(t) = \begin{cases} K_i^{II} (V_i(t) - \bar{V}), & V_i(t) > \bar{V} \\ 0, & \underline{V} \leq V_i(t) \leq \bar{V} \\ K_i^{II} (V_i(t) - \underline{V}), & V_i(t) < \underline{V} \end{cases}$$

Level III: Distributed Control -> voltage regulation to acceptable range

$$u_i^{III}(t) = G_i^{III} \left[\sum_{j=1}^N a_{ij} (u_j^{III}(t) - u_i^{III}(t)) \right] + e(t)$$

$$e(t) = \begin{cases} K_i^{III} (V_i(t) - \bar{V}), & V_i > \bar{V} \\ 0, & \underline{V} \leq V_i \leq \bar{V} \\ K_i^{III} (V_i(t) - \underline{V}), & V_i < \underline{V} \end{cases}$$

Dynamic consensus



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

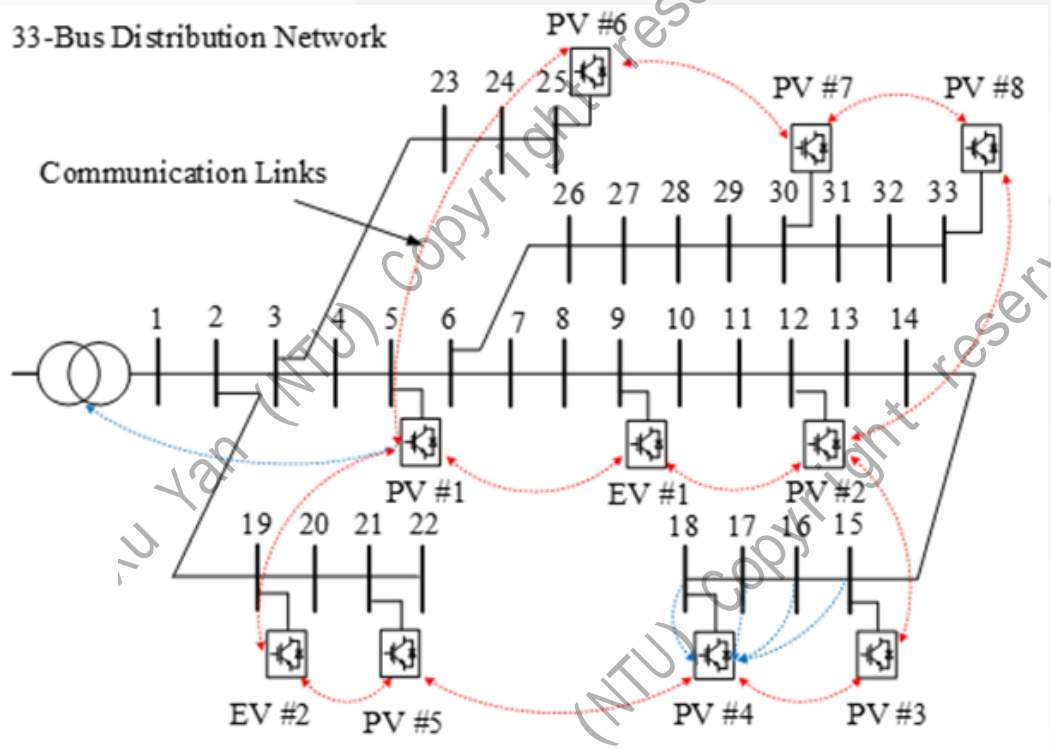
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

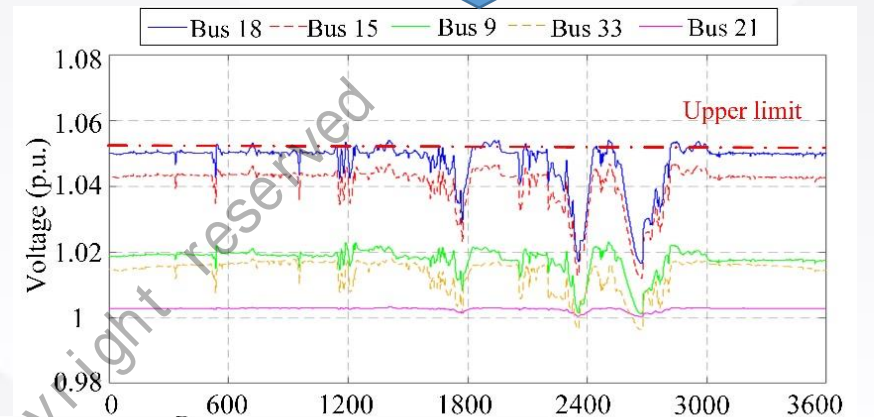
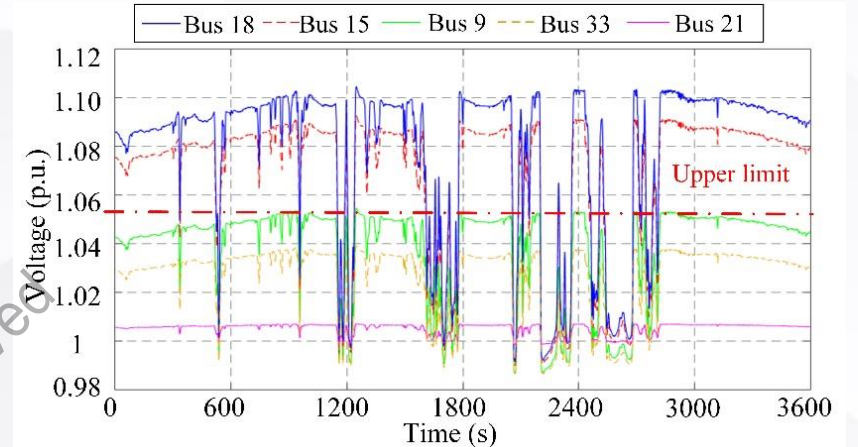
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

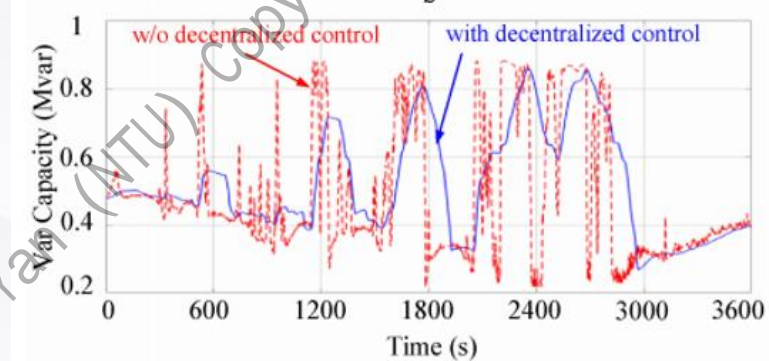
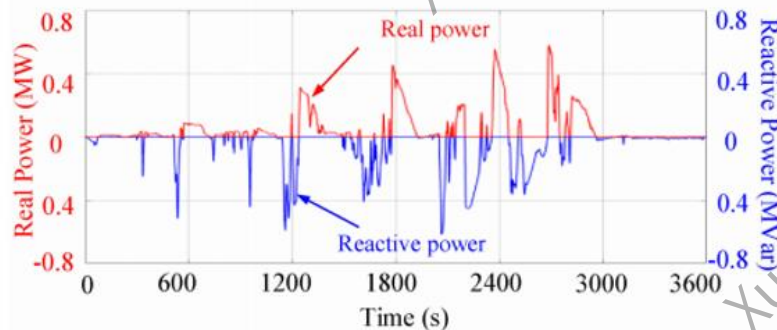
Simulation Tests



Real-time voltage/var control from inverters



Effectiveness of ramp-rate control



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

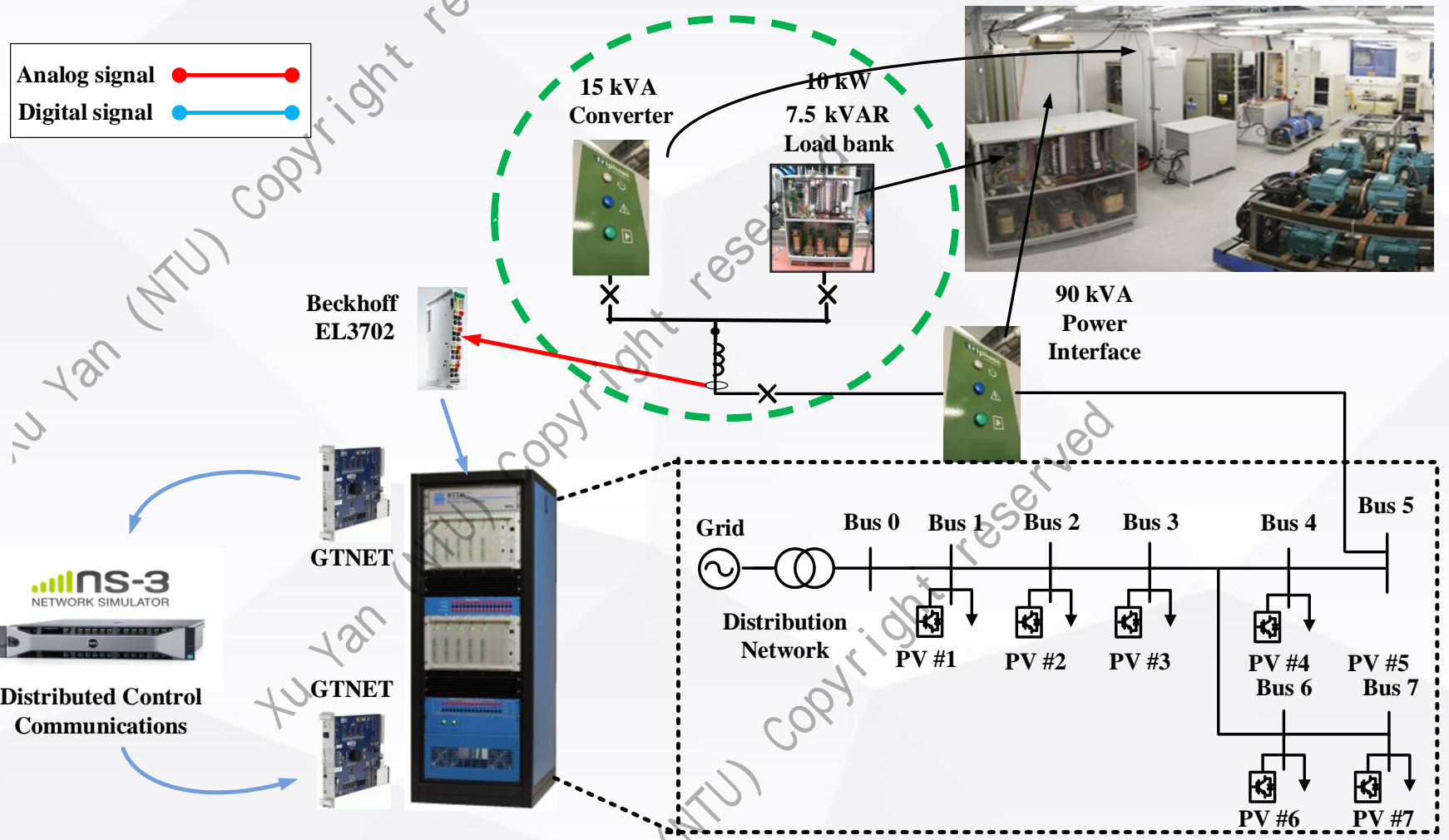
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Power Hardware-in-the-Loop (PHiL) Test



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

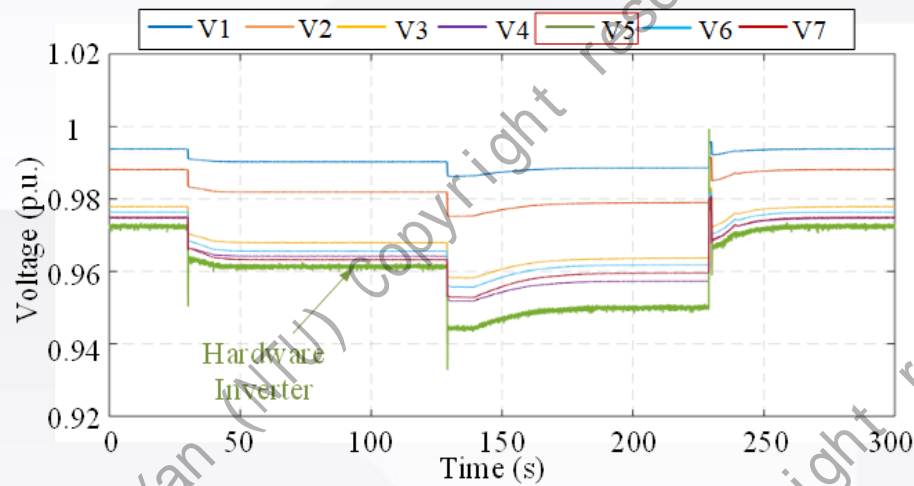
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

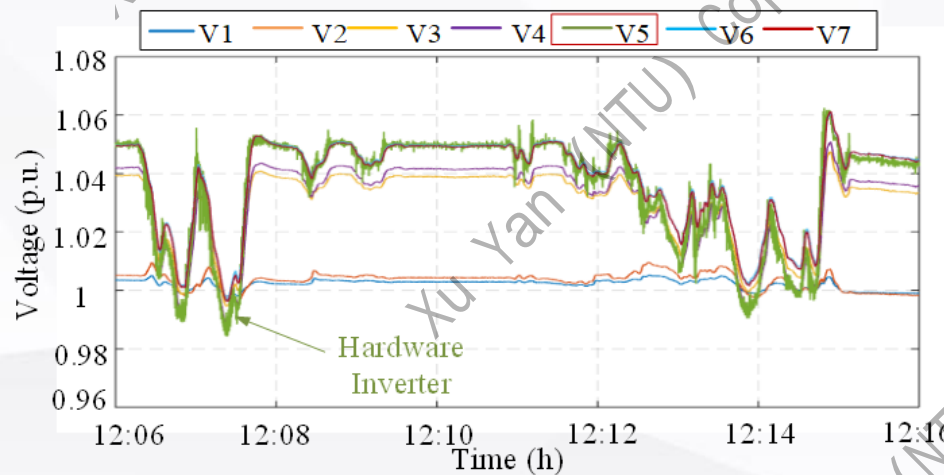
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

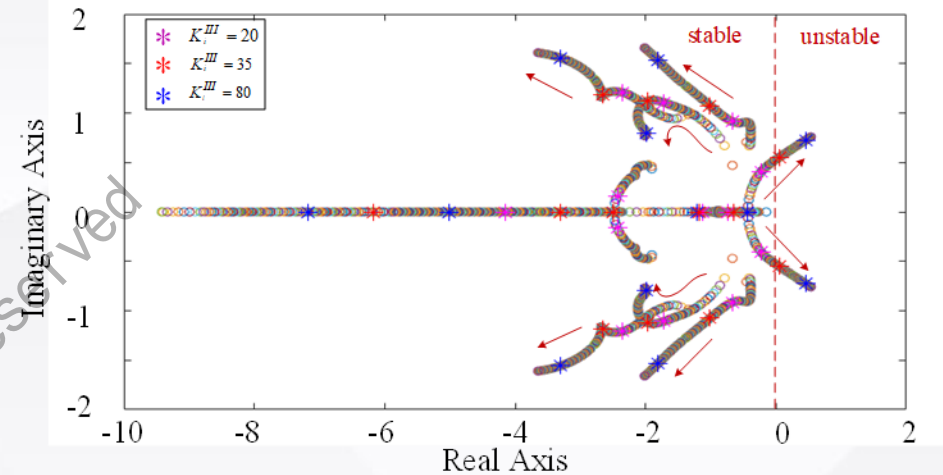
Power HiL Results and Eigenvalues



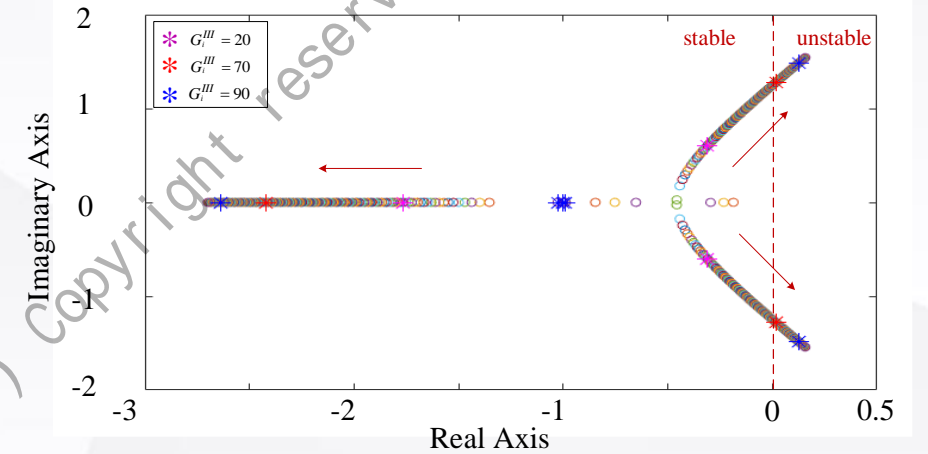
Voltage profiles under step load changes



Voltage profiles under real PV and load data



Trace of eigenvalues under different control gains



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

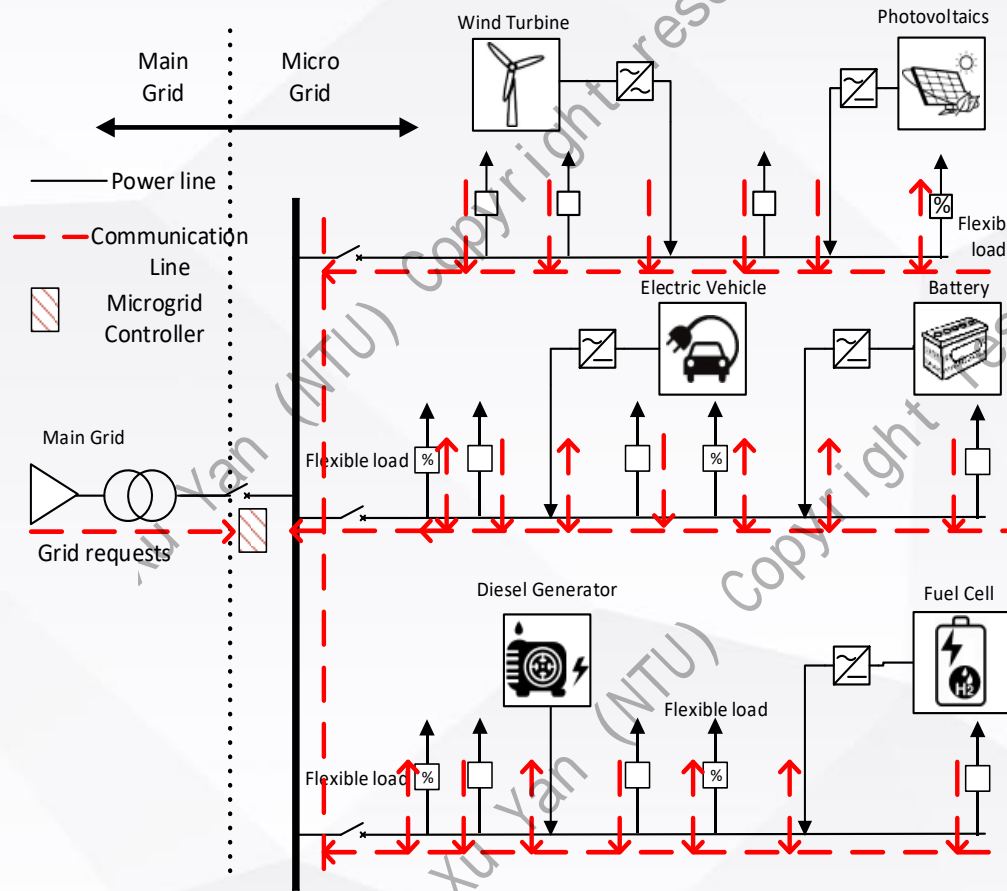
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Operation of DER - Energy Dispatch & Volt/Var Regulation in Microgrid



Control variables:

- 1) Micro-turbine
 - 2) Energy storage
 - 3) Demand response
 - 4) Capacitor banks
 - 5) On-load tap changers
 - 6) PV inverters
- Active power resource
- Reactive power resource

Parameters:

- 1) Load demand
 - 2) Wind and PV output
 - 3) Electricity price
 - 4) Network parameters (R,X,B)
- Uncertain

Network model:

- 1) Linearized Dist-Flow
- 2) Second-order cone model

State variables:

- 1) Bus voltage
- 2) Branch power flow
- 3) Power exchange with main grid

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

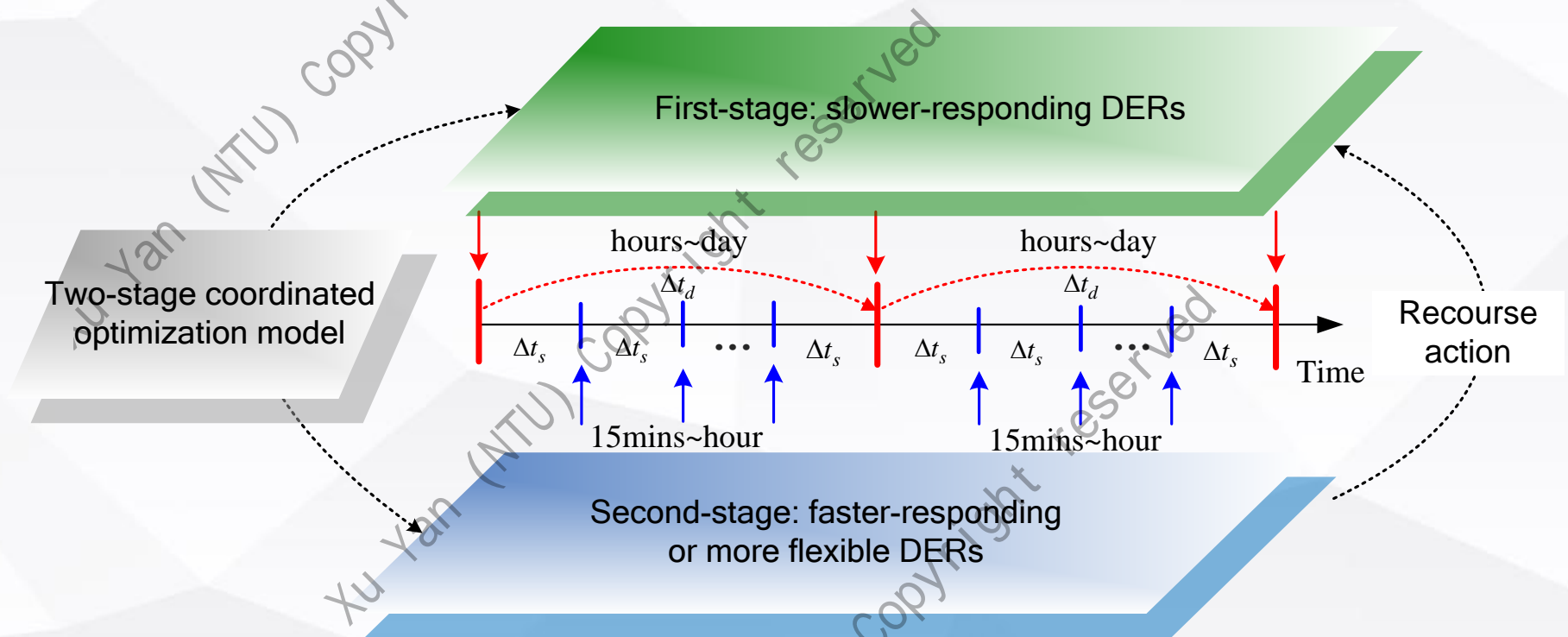
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Two-stage coordinated operation – Temporal Coordination of DERs

Principle: coordinate different DERs in different timescales against uncertainty.

- **First-stage:** slower-responding DER in longer timescale.
- **Second-stage:** faster-responding or more flexible DER in shorter timescale.



- **First-stage decisions** are implemented before uncertainty realizes and will be fixed in the second-stage.
- **Second-stage decisions** will be re-optimized and implemented after uncertainty realizes, therefore it is a recourse action to the first-stage decision.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

■ Optimization Methods

Method	Stochastic Programming	Robust Optimization (RO)
Uncertainty Modeling	Probabilistic scenarios based on probability distribution function (PDF)	Uncertainty set with bounds and budgets
Inputs	Point prediction	Interval prediction
Model	Optimize under expectation $\min_{x \in F} \{f(x) + E[Q(x, \xi)]\}$	Optimize under worst case $\min_x \left(c^T x + \max_{d \in \mathcal{D}} \min_{y \in \Omega(x, d)} b^T y \right)$
Advantages	<ul style="list-style-type: none">• Simpler formulation and solution process	<ul style="list-style-type: none">• No need for PDF• Fully robust within the uncertainty sets
Disadvantages	<ul style="list-style-type: none">• Need for PDF• Probabilistic robustness	<ul style="list-style-type: none">• Complex formulation and solution process• May be conservative

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

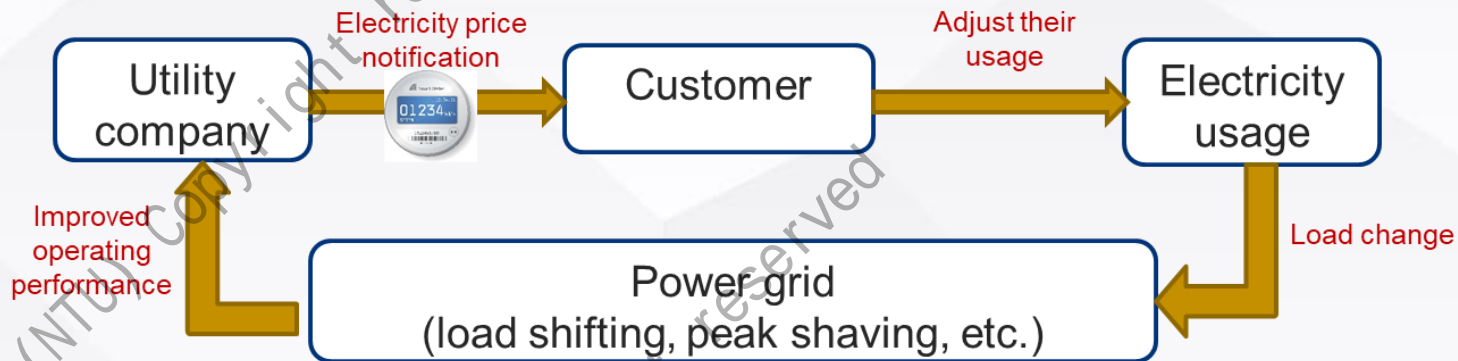
4. Hierarchy coordination

5. Planning

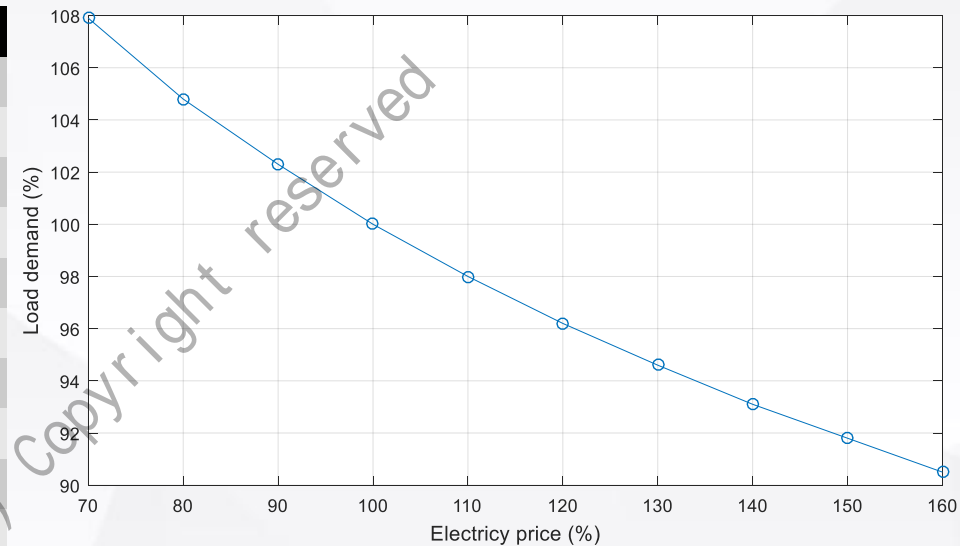
- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Robustly Coordinated Energy Management Day-ahead Price-based Demand Response & Hourly-ahead Microturbine

Price-based Demand Response (PBDR)



Level	Price Rate (%)	Load Rate (%)
1	70	107.9
2	80	104.8
3	90	102.3
4	100	100.0
5	110	98.0
6	120	96.2
7	130	94.6
8	140	93.1
9	150	91.8
10	160	90.5



$$P_t^D = A P r_t^\varepsilon$$

where ε is **price elasticity** of electric demand, and A is a constant value modeling the relationship between the price and load demand. E.g., the price elasticity of load is -0.38 for Australian power systems. ³⁸

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

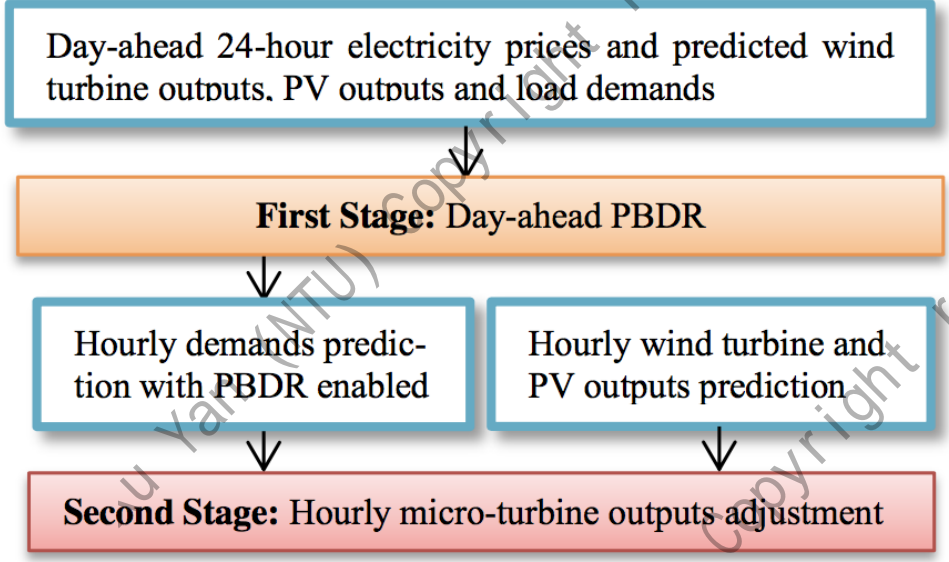
4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Robustly Coordinated Energy Management Day-ahead Price-based Demand Response & Hourly-ahead Microturbine

Two-Stage Operation Framework



Two-Stage Robust Optimization (TSRO) model

$$\min_x c^T x + \max_u \min_y d^T y + e^T u$$

s.t.

$$Ax \geq b$$

$$y \in O(x, u) = \{Fx + Gy \leq v, Hx + Iy + Ju = w\}$$

$$u \in U$$

Objective function

$$\min_{\alpha} -C_{rev}^{pr} + \max_{R_{WT}, R_{PV}, R_D^{unc}} \min_{P_{MT, V, P, Q}} C_{MT} + C_{WT} + C_{PV} + C_{grid} - C_{rev}^{unc}$$

Uncertainty modeling – uncertainty set

$$U_{WT} = \{R_{WT, n, t} \in \mathbb{R}^{n_{wt}}:$$

$$\mu_{WT, l} \leq \frac{\sum_{n \in N_{WT}} \sum_{t \in T} R_{WT, n, t}}{\sum_{n \in N_{WT}} \sum_{t \in T} R_{WT, n, t}^{pr}} \leq \mu_{WT, u},$$

$$R_{WT, n, t}^{low} \leq R_{WT, n, t} \leq R_{WT, n, t}^{up}, \forall n, t\},$$

$$U_{PV} = \{R_{PV, n, t} \in \mathbb{R}^{n_{pv}}:$$

$$\mu_{PV, l} \leq \frac{\sum_{n \in N_{PV}} \sum_{t \in T} R_{PV, n, t}}{\sum_{n \in N_{PV}} \sum_{t \in T} R_{PV, n, t}^{pr}} \leq \mu_{PV, u},$$

$$R_{PV, n, t}^{low} \leq R_{PV, n, t} \leq R_{PV, n, t}^{up}, \forall n, t\},$$

$$U_{LD} = \{P_D^{unc} \in \mathbb{R}^{n_{ld}}:$$

$$\mu_{LD, l} \leq 1 + \frac{1}{n_i n_t} \sum_{i \in N_D} \sum_{t \in T} \sum_{j \in J} \alpha_{j, t} R_{D, i, j, t}^{unc} \leq \mu_{LD, u},$$

$$R_{D, i, j, t}^{low} \leq 1 + R_{D, i, j, t}^{unc} \leq R_{D, i, j, t}^{up}, \forall i, j, t\}.$$

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Robustly Coordinated Energy Management Day-ahead Price-based Demand Response & Hourly-ahead Microturbine

Modelling for Price-based DR

$$C_{rev} = C_{rev}^{pr} + C_{rev}^{unc} \quad (9)$$

$$C_{rev}^{pr} = \sum_{t \in T} \sum_{i \in N_D} P_{D,i,t}^{pr} \sum_{j \in J} \alpha_{j,t} L_j Pr_j \quad (10)$$

$$C_{rev}^{unc} = \sum_{t \in T} \sum_{i \in N_D} P_{D,i,t}^{pr} \sum_{j \in J} \alpha_{j,t} L_j Pr_j R_{D,i,j,t}^{unc} \quad (11)$$

$$\alpha_{j,t} \in \{0, 1\}, \forall j, t \quad (12)$$

$$\sum_{j \in J} \alpha_{j,t} = 1, \forall t \quad (13)$$

$$\sum_{t \in T} \sum_{i \in N_D} P_{D,i,t}^{pr} \sum_{j \in J} \alpha_{j,t} L_{j,t} Pr_{j,t} \leq \sum_{t \in T} \sum_{i \in N_D} P_{D,i,t}^{pr} Pr_{0,t} \quad (14)$$

$$\sum_{t \in T} \sum_{i \in N_D} P_{D,i,t}^{pr} \sum_{j \in J} \alpha_{j,t} L_{j,t} \geq \sum_{t \in T} \sum_{i \in N_D} P_{D,i,t}^{pr} \quad (15)$$

- Considering the characteristics of the uncertain load demands, in (9), the revenue from the demands is split into two parts i.e. the predicted revenue based on the predicted load demands and the uncertain revenue difference from the predicted one.
- Constraints (10) and (11) support the calculation functions of these two revenue items respectively.
- Constraint (12) denotes the decision variable for each PBDR level is binary.
- Constraint (13) guarantees that only one PBDR level decision can be carried out for each hour.
- Constraint (14) and (15) guarantees the bills for the customers cannot increase and the energy which the customers can use cannot decrease. These mean that the proposed PBDR does not reduce the customers' economic benefits.



C. Zhang, Y. Xu, Z. Y. Dong, "Robust Coordination of Distributed Generation and Price-Based Demand Response in Microgrids," *IEEE Trans. Smart Grid*, 2018. **Web-of-Science Highly Cited Paper**

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

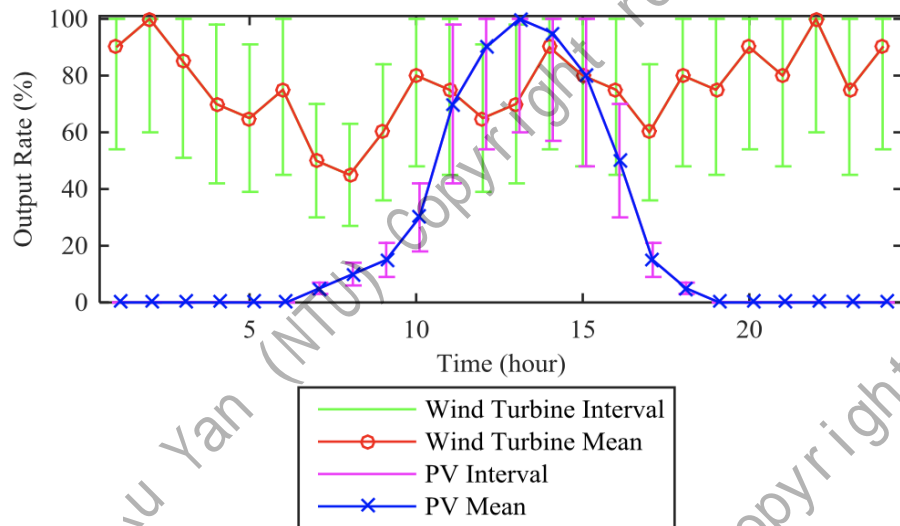
4. Hierarchy coordination

5. Planning

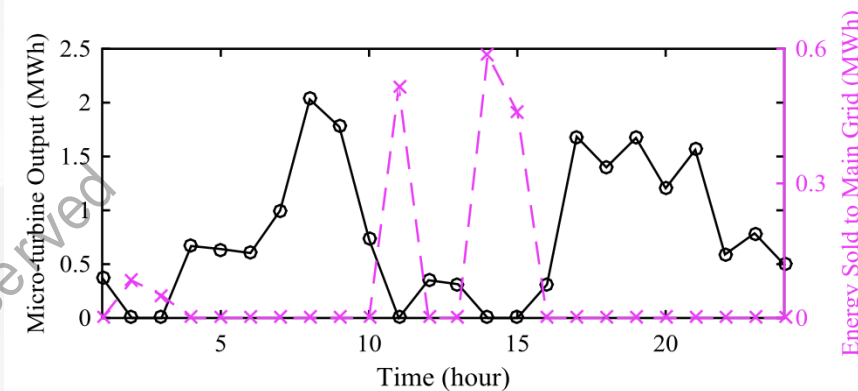
- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Robustly Coordinated Energy Management Day-ahead Price-based Demand Response & Hourly-ahead Microturbine

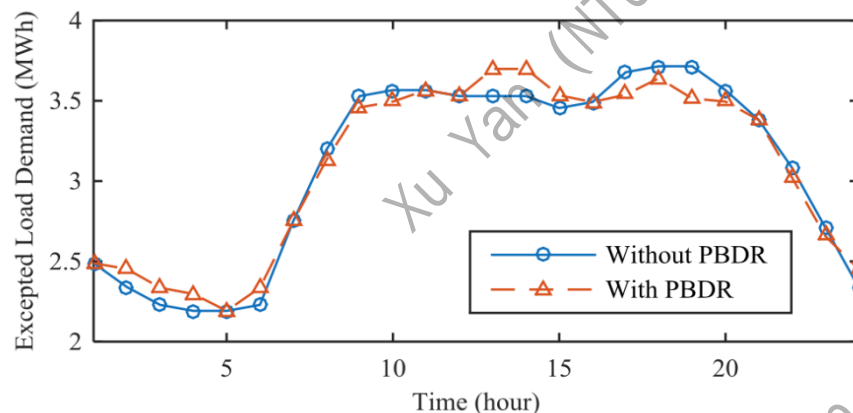
Day-ahead Interval Prediction



Hourly Microturbine Dispatch



Day-ahead PBDR Decision



Strategy	Average Profit (\$)	Micro-Turbine Generation (MWh)	Energy Bought from Main Grid (MWh)	Energy Sold to Main Grid (MWh)	Average Maximal Voltage Deviation (%)	TSRO beat Single in profit (%)	TSRO beat Single in voltage deviation (%)
Deviation Group 1: $\sigma_{WT} = 5\%M_{WT}$; $\sigma_{PV} = 5\%M_{PV}$; $\sigma_D = 1\%M_D$							
TSRO	3484.56	18.148	0.000	0.704	1.51%	100%	85.2%
Single	3465.65	17.612	0.970	1.225	1.52%		
Deviation Group 2: $\sigma_{WT} = 10\%M_{WT}$; $\sigma_{PV} = 10\%M_{PV}$; $\sigma_D = 2\%M_D$							
TSRO	3479.21	18.514	0.000	0.796	1.52%	100%	93.6%
Single	3437.12	17.612	1.989	1.970	1.60%		
Deviation Group 3: $\sigma_{WT} = 20\%M_{WT}$; $\sigma_{PV} = 20\%M_{PV}$; $\sigma_D = 4\%M_D$							
TSRO	3464.49	19.564	0.009	1.055	1.54%	100%	99.5%
Single	3378.48	17.612	4.064	3.246	1.83%		

C. Zhang, Y. Xu, Z. Y. Dong, "Robust Coordination of Distributed Generation and Price-Based Demand Response in Microgrids," *IEEE Trans. Smart Grid*, 2018. **Web-of-Science Highly Cited Paper**

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

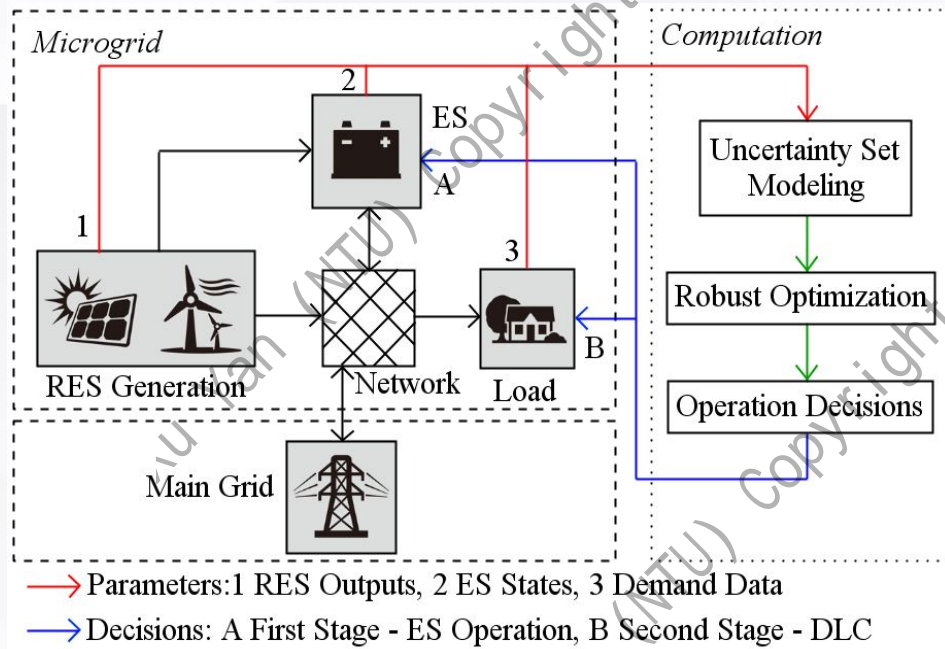
4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Robustly Coordinated Energy Management
Hourly-ahead energy storage & 15min-ahead direct load control (DLC)

Two-stage coordination framework



Two-stage robust optimization model

$$\min_{\alpha_{dis}, \alpha_{ch}} C_{ES} + \max_{P_{WT}, P_{PV}, K_{DLC}, V, P, Q \in O} \min_{C_{WT} + C_{PV} + C_{grid} - C_{rev.}}$$

ESS economic model

$$C_{ES,dis} E_{dis} + C_{ES,ch} E_{ch} = C_{ES,OM} E_{stored}$$

$$E_{stored} = \eta_{dis} E_{dis} = \eta_{ch} E_{ch}, \eta_{dis} > 1, \eta_{ch} < 1$$

$$\frac{C_{ES,dis}}{\eta_{dis}} + \frac{C_{ES,ch}}{\eta_{ch}} = C_{ES,OM}$$

ESS operation model

$$P_{ES,dis,m} = P_{dis,m}^{max} \sum_{j \in I_{dis}} \alpha_{dis,m,j} L_{dis,m,j} \quad P_{ES,ch,m} = P_{ch,m}^{max} \sum_{j \in I_{ch}} \alpha_{ch,m,j} L_{ch,m,j}$$

C. Zhang, Y. Xu, Z. Y. Dong, "Robust Operation of Microgrids via Two-Stage Coordinated Energy Storage and Direct Load Control," *IEEE Trans. Power Syst.*, 2017.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

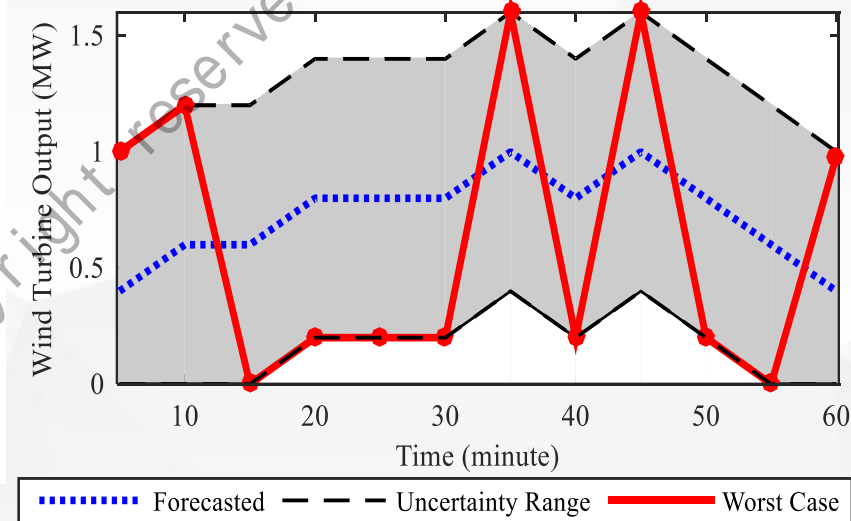
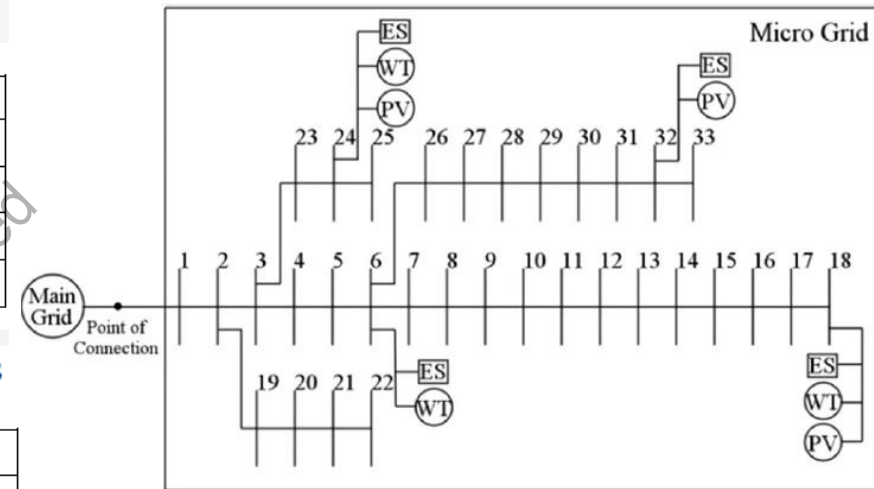
Robustly Coordinated Energy Management Hourly-ahead energy storage & 15min-ahead direct load control (DLC)

UNCERTAINTY BUDGET SETS UNDER TESTS

Test No	1	2	3	4	5	6
$\mu_{WT,l}$	95%	90%	85%	80%	75%	70%
$\mu_{WT,u}$	105%	110%	115%	120%	125%	130%
$\mu_{PV,l}$	97.5%	95%	92.5%	90%	87.5%	85%
$\mu_{PV,u}$	102.5%	105%	107.5%	110%	112.5%	115%

SOLUTION RESULTS FOR BASE CASE UNDER DIFFERENT UNCERTAINTY SETS

Test No	1	2	3	4	5	6	
ES Dis-charging	ES 1	0%	10%	0%	10%	10%	10%
	ES 2	0%	0%	10%	0%	0%	0%
	ES 3	20%	20%	40%	20%	40%	40%
	ES 4	30%	20%	20%	30%	30%	30%
DLC under Worst Case	0-15 min	0%	0%	0%	0%	0%	0%
	15-30 min	46%	0%	43%	39%	38%	38%
	30-45 min	0%	0%	0%	0%	31%	0%
	45-60 min	3%	6%	2%	2%	0%	0%
Profit under Worst Case (\$)	192.39	187.94	184.45	179.86	177.30	174.29	
Iteration Number	5	5	3	3	3	2	
Solution Time (s)	61.39	15.96	12.04	13.84	18.34	7.01	



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

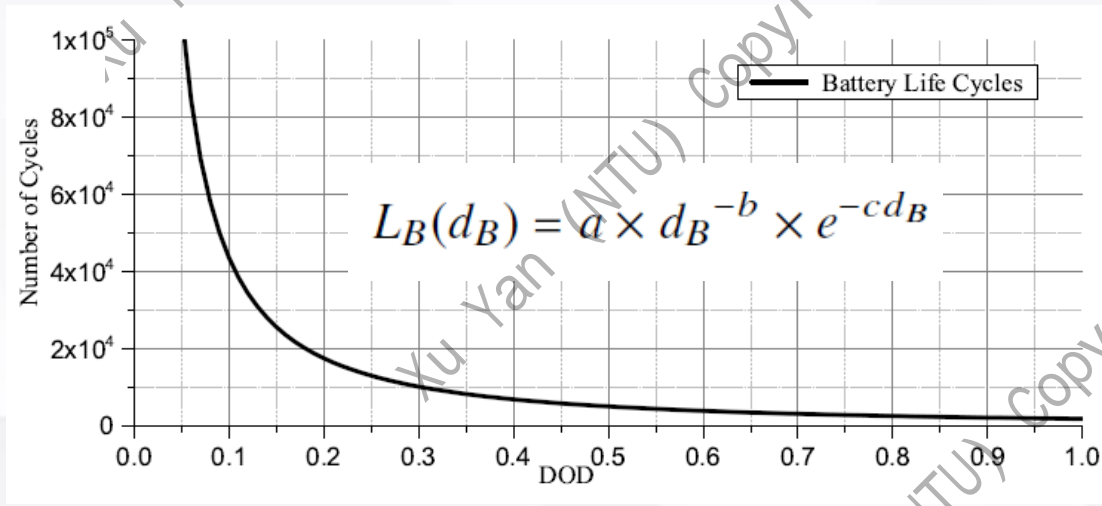
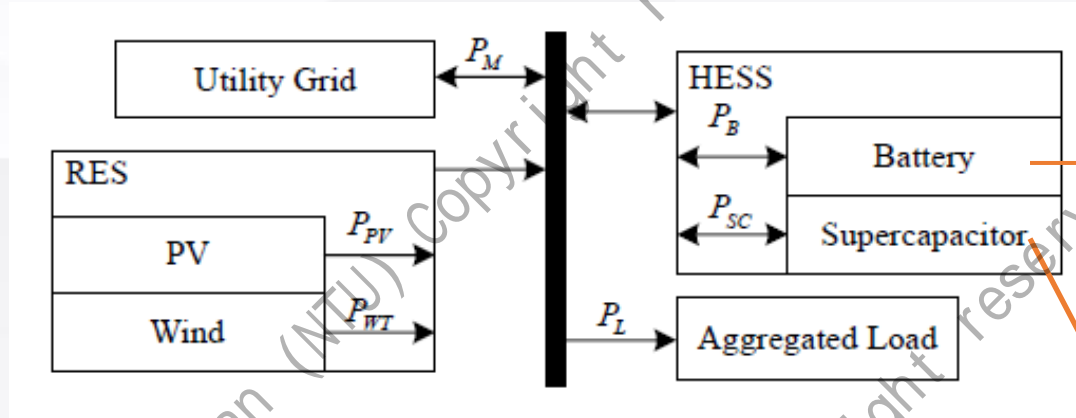
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Two-Stage Dispatch of Hybrid Energy Storage considering battery health



Relationship between the number of life cycles and the DOD of Ni-Cd batteries



C. Ju, P. Wang, L. Goel, and Y. Xu, "A two-layer energy management system for microgrids with hybrid energy storage considering degradation costs," *IEEE Trans. Smart Grid*, 2017

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

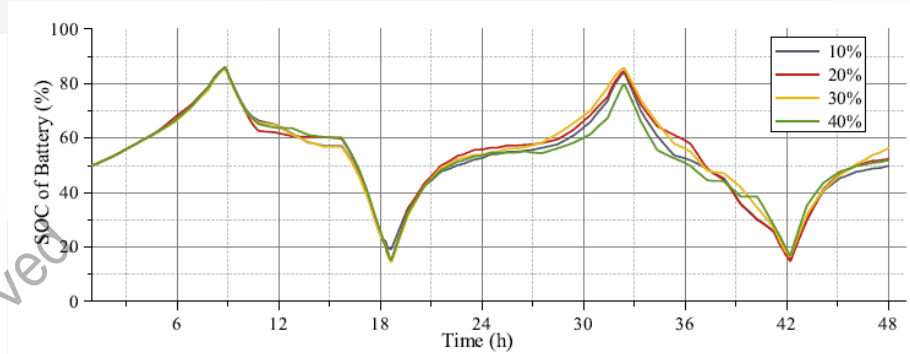
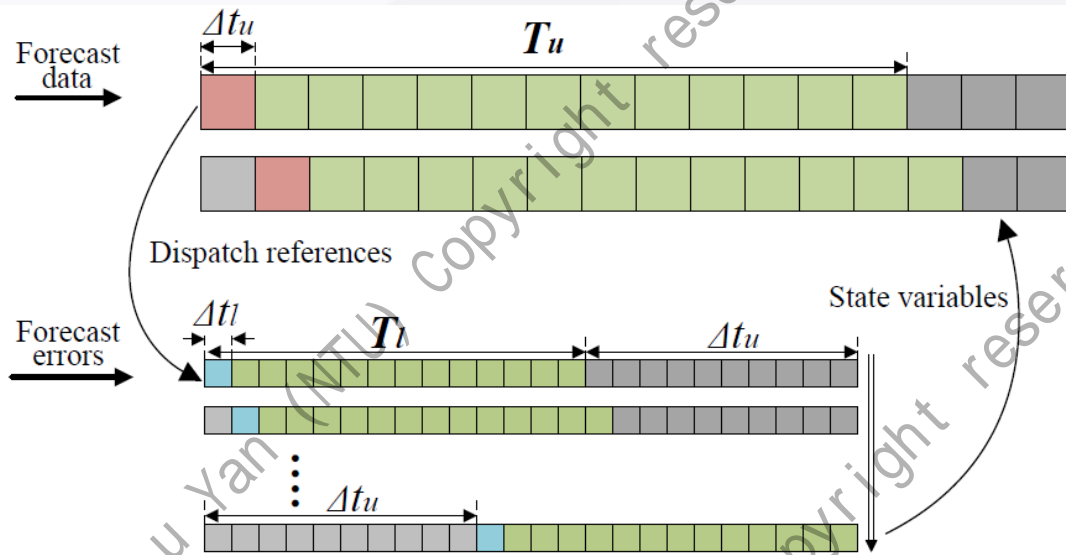
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

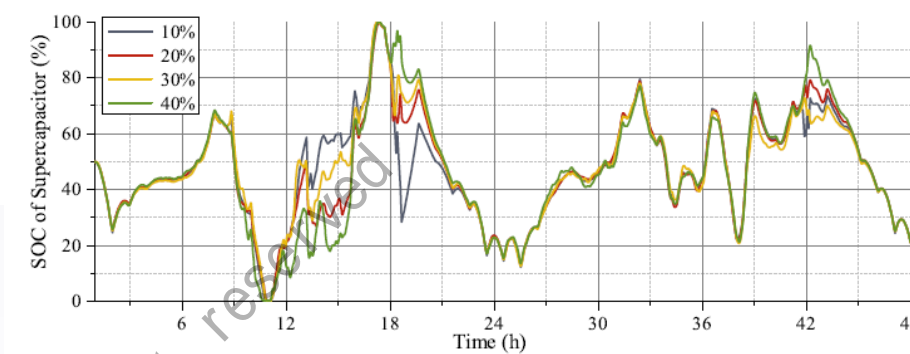
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Two-Stage Dispatch of Hybrid Energy Storage considering battery health

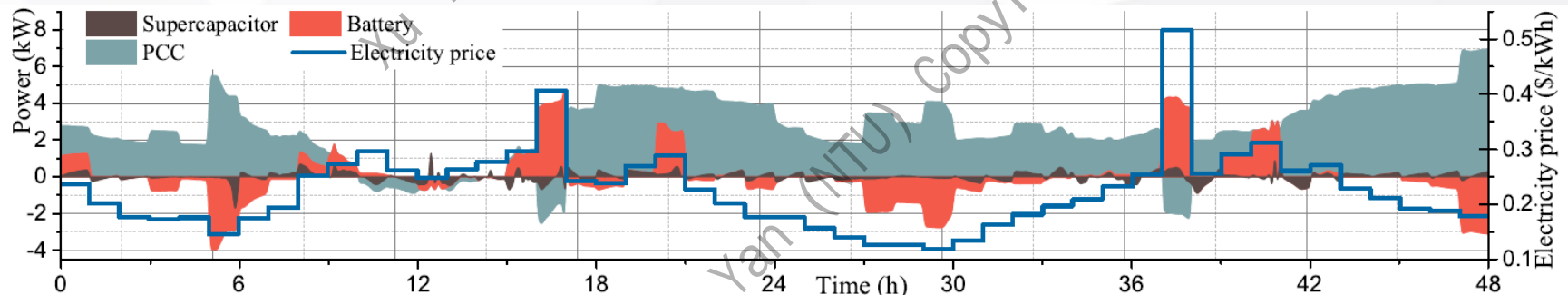


(a) SOC of battery



(b) SOC of supercapacitor

- ✓ **First-stage: battery dispatch with SOH degradation cost**
- ✓ **Second-stage: supercapacitor dispatch**



(b) Optimal dispatch in real-time pricing

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

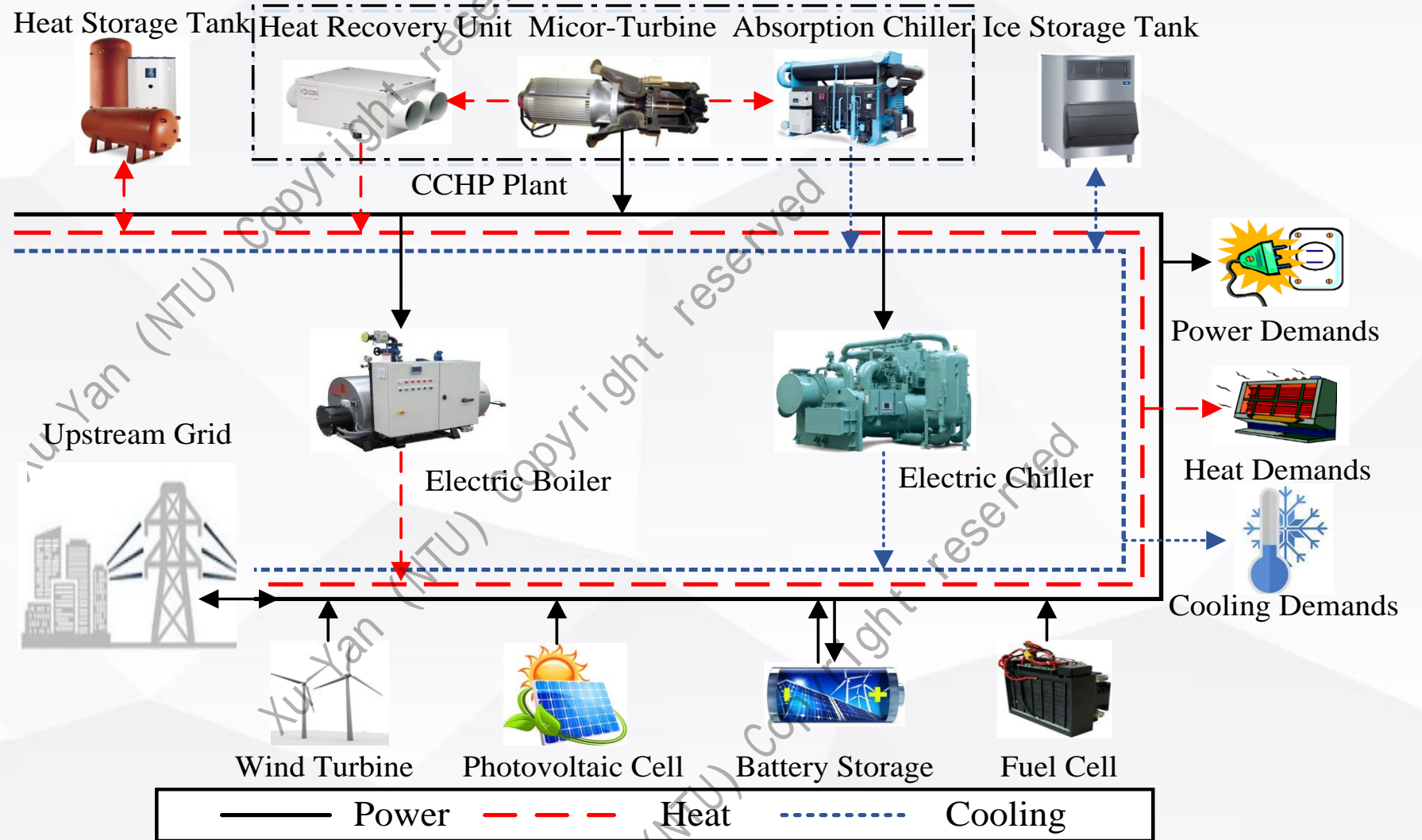
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Multi-Energy Microgrid



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

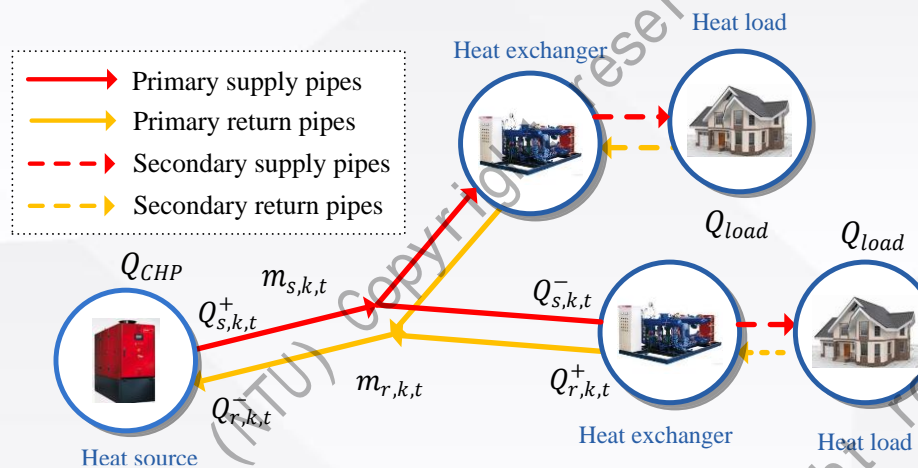
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

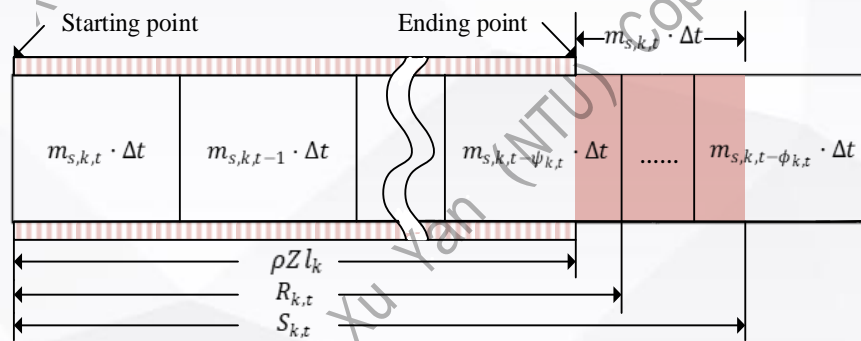
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

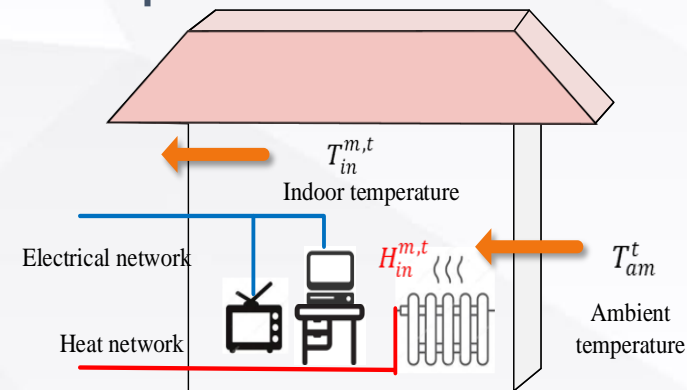
Multi-Energy Microgrid – Modeling of thermal part



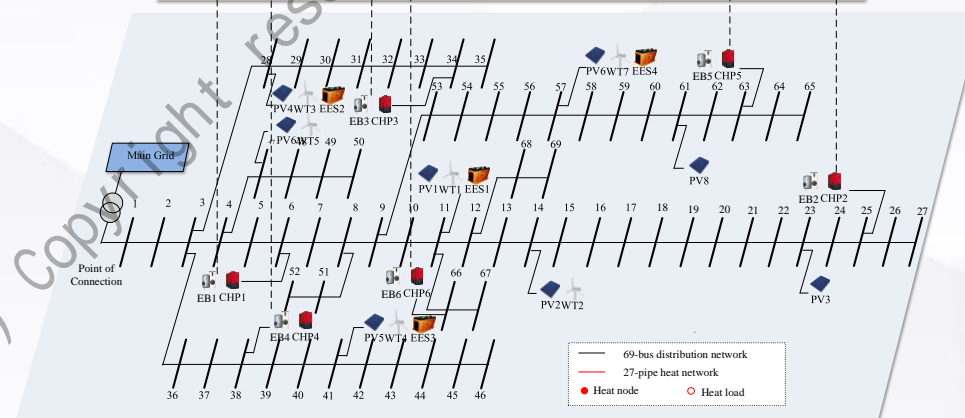
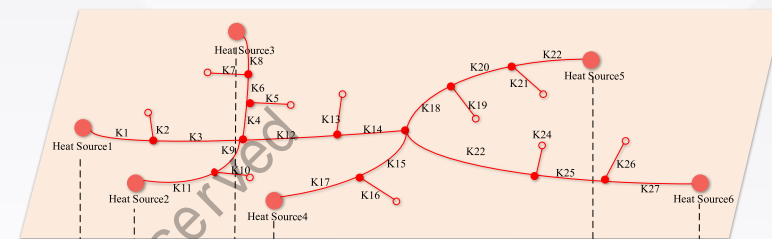
District Heat Network



Vertical section of a pipe



Thermal conduction of a building



Coupled electric-thermal network

Y. Chen, Y. Xu*, Z. Li, "Optimally Coordinated Dispatch of Combined-Heat-and-Electrical Network," *IET Gen. Trans. & Dist.*, 2019.

Z. Li and Y. Xu*, "Optimal coordinated energy dispatch for a multi-energy microgrid in grid-connected and islanded modes," *Applied Energy*, 2017. **Web-of-Science Highly Cited Paper**

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

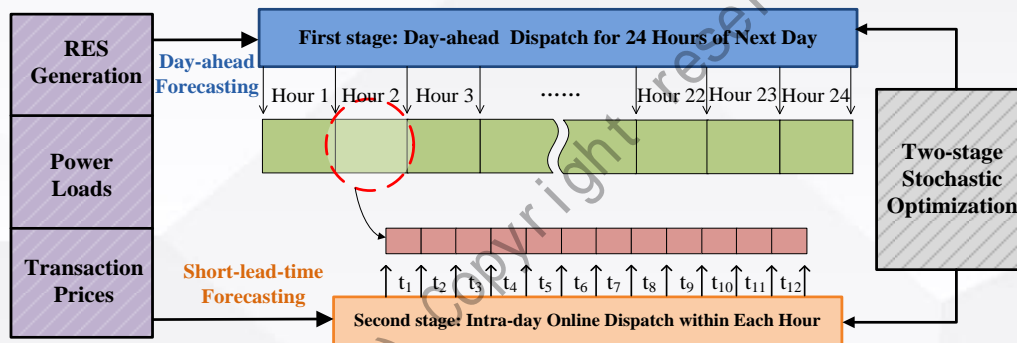
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Multi-Energy Dispatch – Two-Stage Coordinated Operation



Temporally-coordinated Stochastic Operation Framework

$$\begin{aligned}
 \text{MIN } F_G &= C_{FC} + C_{OM} + C_{EX} + C_{ST} + C_{SD} - C_{HR} \\
 C_{FC} &= \sum_{t \in N_T} \sum_{i \in N_M} (\gamma_G P_{MT}^{t,i} / \eta_{MT}^{t,i}) \Delta t \\
 C_{EX} &= \sum_{t \in N_T} (\gamma_B P_{BUY}^{t,1} - \gamma_S P_{SELL}^{t,1}) \Delta t \\
 C_{OM} &= \sum_{t \in N_T} \sum_{i \in N_W} [\gamma_{WT} P_{WT}^{t,i} + \dots + \sum_{i \in N_B} \gamma_{TST} (P_{TSTC}^{t,i} + P_{TSTD}^{t,i})] \Delta t \\
 C_{ST} &= \sum_{t \in N_T} \sum_{i \in (N_M \cup N_E)} \max\{0, U_{CG}^{t,i} - U_{CG}^{t-1,i}\} C_{CG}^U \\
 C_{SD} &= \sum_{t \in N_T} \sum_{i \in (N_M \cup N_E)} \max\{0, U_{CG}^{t-1,i} - U_{CG}^{t,i}\} C_{CG}^D \\
 C_{HR} &= \sum_{t \in N_T} \sum_{i \in N_M} \gamma_{HR} H_L^{t,i} \Delta t
 \end{aligned}$$

$$\min_{z, y_1, y_2, \dots, y_n} F(z) + \sum_{n \in N_S} \chi_n L(y_n)$$

$$\text{s.t. } z \in F_A$$

$$y_n \in \Omega(z, \omega_n), \forall n$$

Two-Stage Stochastic Optimization model

$$U_{CG}^{t,i} \cdot P_{CG}^{min,i} \leq P_{CG}^{t,i} \leq U_{CG}^{t,i} \cdot P_{CG}^{max,i}$$

$$R_{CG}^{down,i} \Delta t \leq P_{CG}^{t,i} - P_{CG}^{t-1,i} \leq R_{CG}^{up,i} \Delta t$$

$$1 - \Delta V_{BUS}^{max} \leq V_{BUS}^{t,i} \leq 1 + \Delta V_{BUS}^{max}$$

$$P_{PF}^{t,b+1} = P_{PF}^{t,b} - P_{PF}^{t,0,b+1} - P_L^{t,i} + \dots - P_{PT}^{t,i}, b \in Br(i), \forall i, t$$

$$Q_{PF}^{t,b+1} = Q_{PF}^{t,b} - Q_{PF}^{t,0,b+1} - Q_L^{t,i}, b \in Br(i), \forall i, t$$

$$V_{BUS}^{t,i+1} = V_{BUS}^{t,i} - (R^b P_{PF}^{t,b} + X^b Q_{PF}^{t,b}) / V_0, b \in Br(i, i+1), \forall i, t$$

$$H_L^{t,i} = H_{MT}^{t,i} + H_{PT}^{t,i} + P_{TSTD}^{t,i} - P_{TSTC}^{t,i}$$

$$\xi_{ES}^{min,i} Cap_{ES}^i \leq E_{ES}^{t,i} \leq \xi_{ES}^{max,i} Cap_{ES}^i$$

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

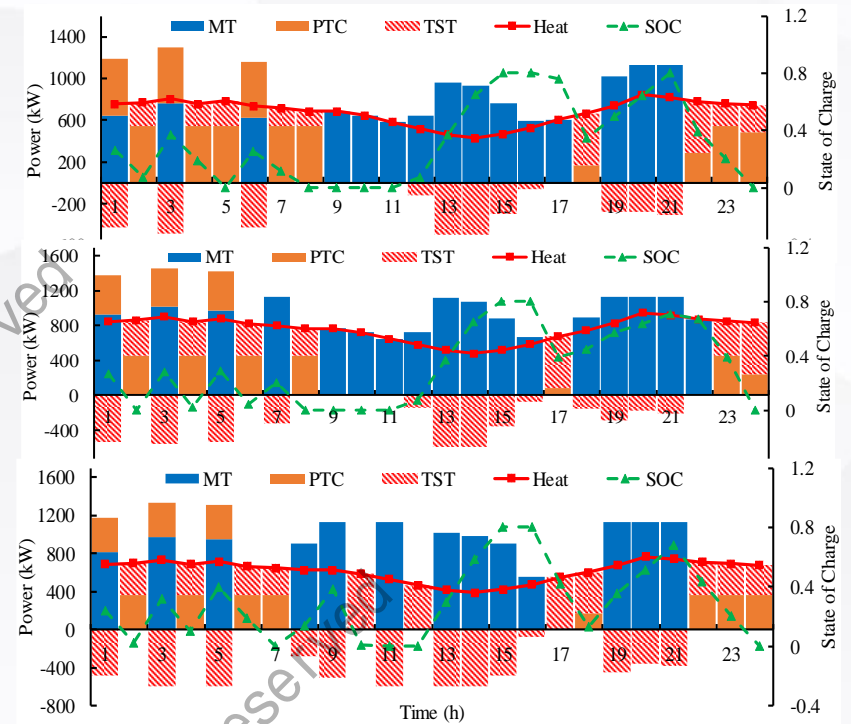
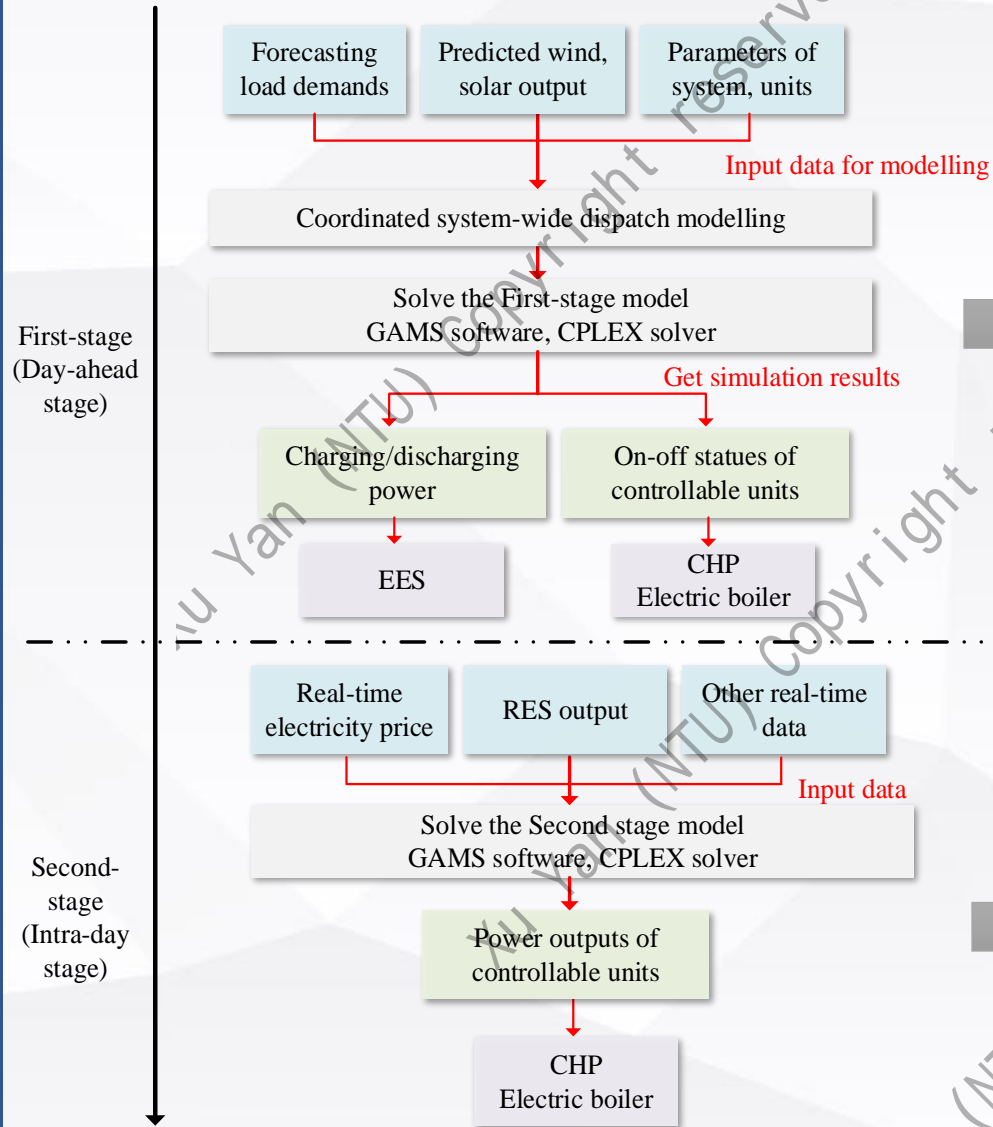
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

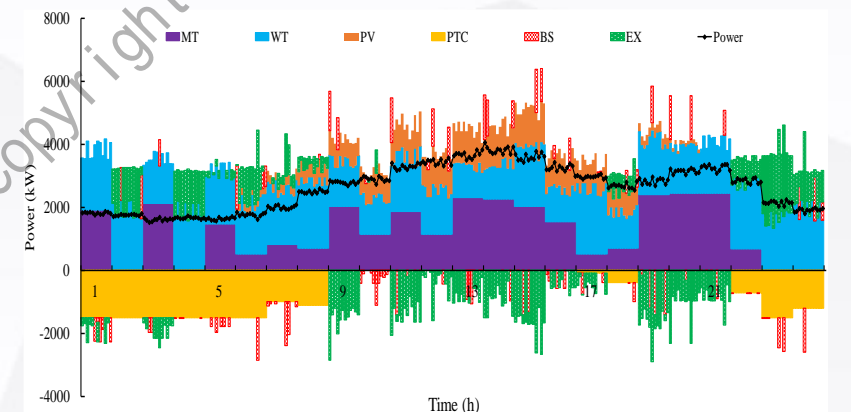
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Multi-Energy Dispatch – Two-Stage Coordinated Operation



Day-ahead dispatch results



Intra-day dispatch results

Z. Li and Y. Xu*, "Temporally-Coordinated Optimal Operation of a Multi-energy Microgrid under Diverse Uncertainties," *Applied Energy*, 2019.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

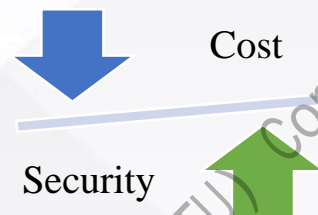
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Multi-Energy Dispatch – Two-Stage Coordinated Operation



Method #1: Single-stage deterministic operation

Method #2: Single-stage stochastic operation

Method#3: Two-stage deterministic optimization

Item	Method #1	Method #2	Method #3	Our Method
Uncertainty level 1 (Lower Uncertainty)				
Average cost (\$)	2183.46	2149.65	2468.20	2440.22
Average voltage violation (%)	30.40	16.50	0	0
Uncertainty level 2 (Medium Uncertainty)				
Average Cost (\$)	2218.89	2188.97	2483.19	2450.78
Average voltage violation (%)	74.70	49.80	0	0
Uncertainty level 3 (High Uncertainty)				
Average Cost (\$)	2341.64	2282.66	2556.04	2508.65
Voltage violation (%)	97.20	77.90	0	0

Z. Li and Y. Xu*, “Temporally-Coordinated Optimal Operation of a Multi-energy Microgrid under Diverse Uncertainties,” *Applied Energy*, 2019.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

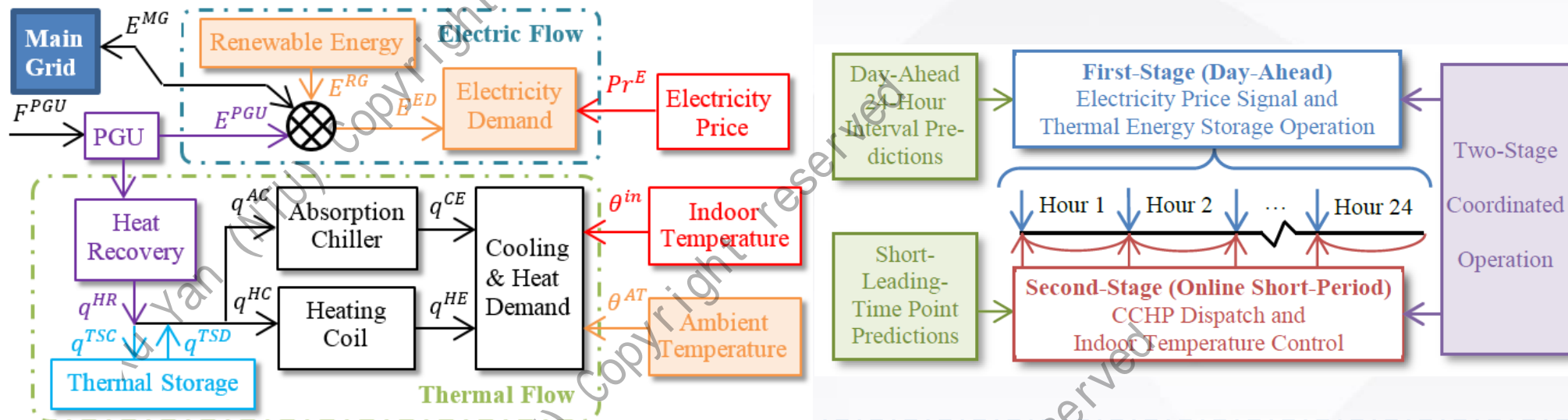
4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Multi-Energy Demand Response

indoor temperature control (thermal load) and **price-based DR (electric load)** to counteract uncertain renewable power generation, load, and ambient temperature



Day-ahead robust optimization model

$$\min_x \max_u \min_y (C_{CCHP} + C_{OM} + C_{grid} - C_{rev}^{elec} - C_{rev}^{thm}) \quad (48)$$

s.t. (10)-(47)

Intra-day optimization model

$$-C_{rev}^{elec} + \min_y (C_{CCHP} + C_{OM} + C_{grid} - C_{rev}^{thm}) \quad (49)$$

s.t. (10)-(14), (25)-(46)

- 1) x is the *first-stage control variables*, denoting the day-ahead operation decisions including the electricity price $\alpha_{j,t}$ as well as the thermal storage operation state $\beta_{m,t}^{TSC/D}$ and $q_{m,t}^{TSC/D}$;
- 2) y is the *second-stage control variables*, expressing the intra-day operation decisions including the CCHP electric power output $P_{m,t}^{CCHP}$ and the indoor temperature setpoint $\theta_{m,k,t}^{in}$;
- 3) u is the *uncertain variables* which include the renewable power outputs $P_{n,t}^{WT/PV}$, the electric load demand $P_{0,i,t}^{ED}$ and the ambient temperature $\theta_{m,k,t}^{am}$.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

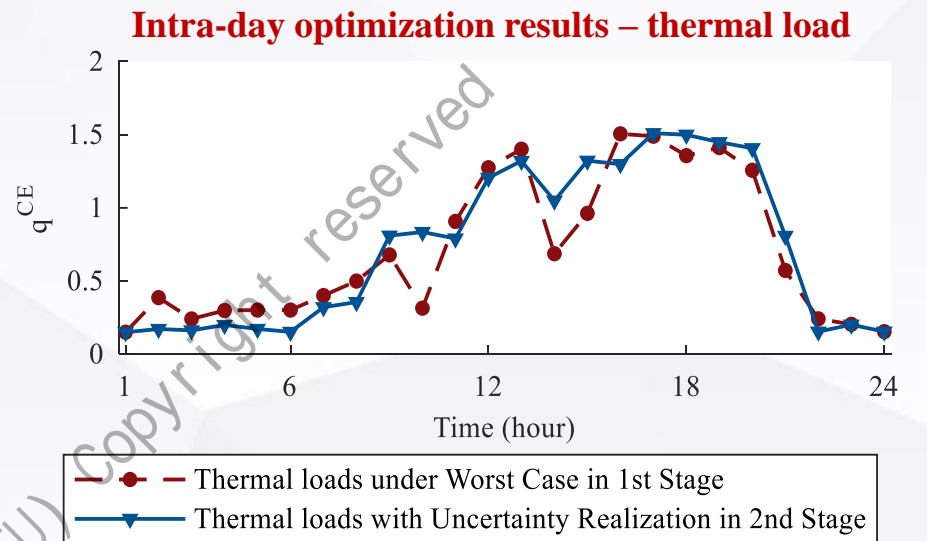
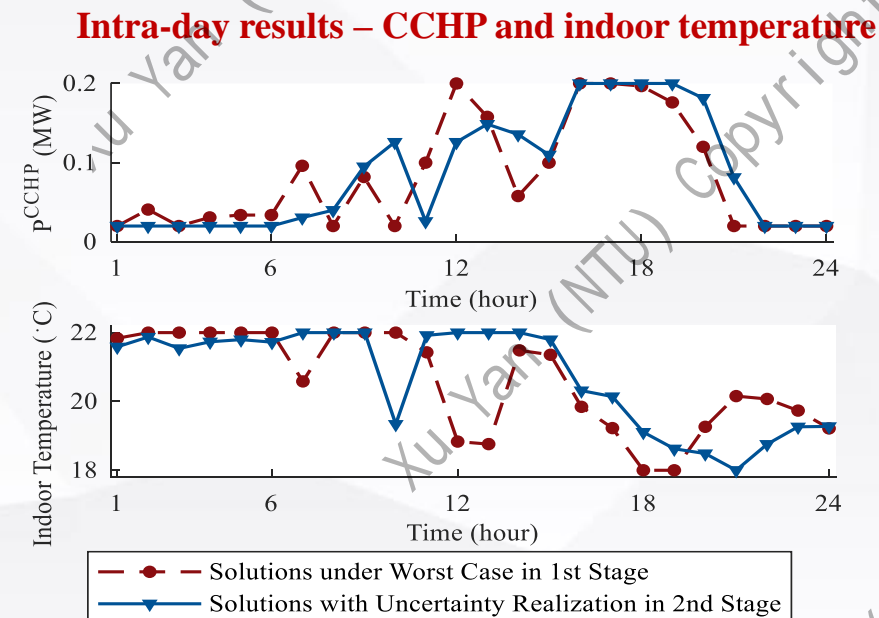
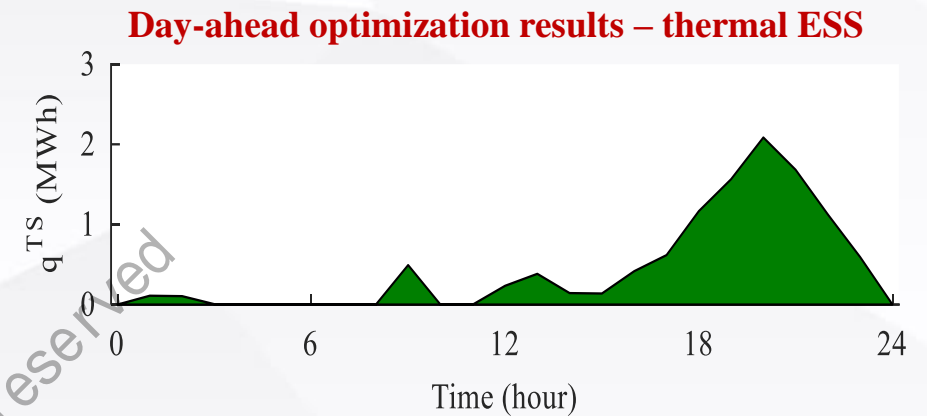
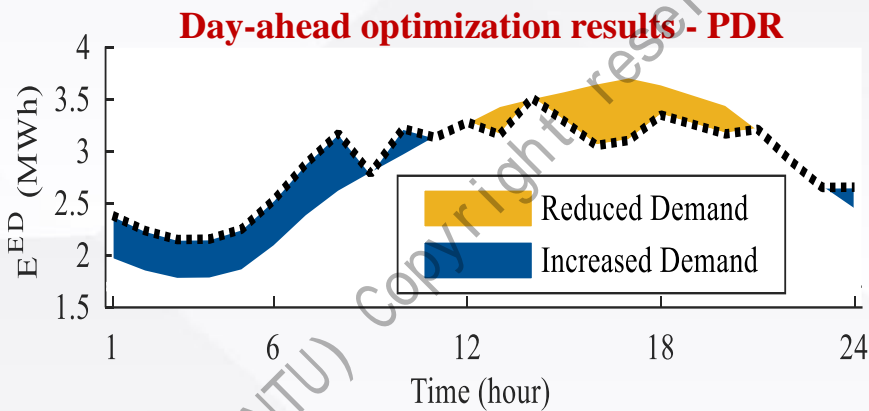
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Multi-energy demand response



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm



Robustness VS Conservativeness

Robustness:

Possibility of a feasible solution (or no operating constraint violation) whatever uncertainties realize (**Advantage**)

- Full Robustness: Always a feasible solution

Conservativeness:

Compromise in optimization process when considering uncertainties (**Drawback**)

Design of Uncertainty Budgets

- Larger Budgets
 - > Higher Robustness
 - > Higher Conservativeness
- Uncertainty Degree Analysis

Robustness under Different Uncertainty Budgets

UNCERTAINTY SETS WITH DIFFERENT UNCERTAINTY BUDGETS

Uncertainty Set Group No	$\underline{\mu}^{PV}$	$\overline{\mu}^{PV}$	$\underline{\mu}^{EL}$	$\overline{\mu}^{EL}$	$\underline{\mu}^{HE}$	$\overline{\mu}^{HE}$
1	0.95	1.05	0.98	1.02	0.99	1.01
2	0.9	1.1	0.96	1.04	0.98	1.02
3	0.8	1.2	0.94	1.06	0.97	1.03

FEASIBILITY CHECK RESULTS IN ISLANDED MODE

Method	Deterministic Method	Proposed Robustly Coordinated Operation		
Uncertainty Set Group No	N. A.	1	2	3
Optimized Total Operating Cost in Day-Ahead Stage (\$)	5993	6387	6586	6822
MCS Group 1: $\sigma^{PV} = 5\% \hat{p}^{PV}$, $\sigma^{EL} = 2\% \hat{p}^{EL}$, $\sigma^{HE} = 1\% \hat{q}^{HE}$				
Average Total Operating Cost of Feasible Cases (\$)	6020	6036	6044	6034
Infeasible Case Rate (%)	0.1%	0.0%	0.0%	0.0%
MCS Group 2: $\sigma^{PV} = 10\% \hat{p}^{PV}$, $\sigma^{EL} = 4\% \hat{p}^{EL}$, $\sigma^{HE} = 2\% \hat{q}^{HE}$				
Average Total Operating Cost of Feasible Cases (\$)	6051	6056	6064	6052
Infeasible Case Rate (%)	12.5%	1.6%	1.0%	0.0%
MCS Group 3: $\sigma^{PV} = 20\% \hat{p}^{PV}$, $\sigma^{EL} = 8\% \hat{p}^{EL}$, $\sigma^{HE} = 4\% \hat{q}^{HE}$				
Average Total Operating Cost of Feasible Cases (\$)	6097	6095	6103	6087
Infeasible Case Rate (%)	25.9%	6.5%	5.7%	0.0%

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

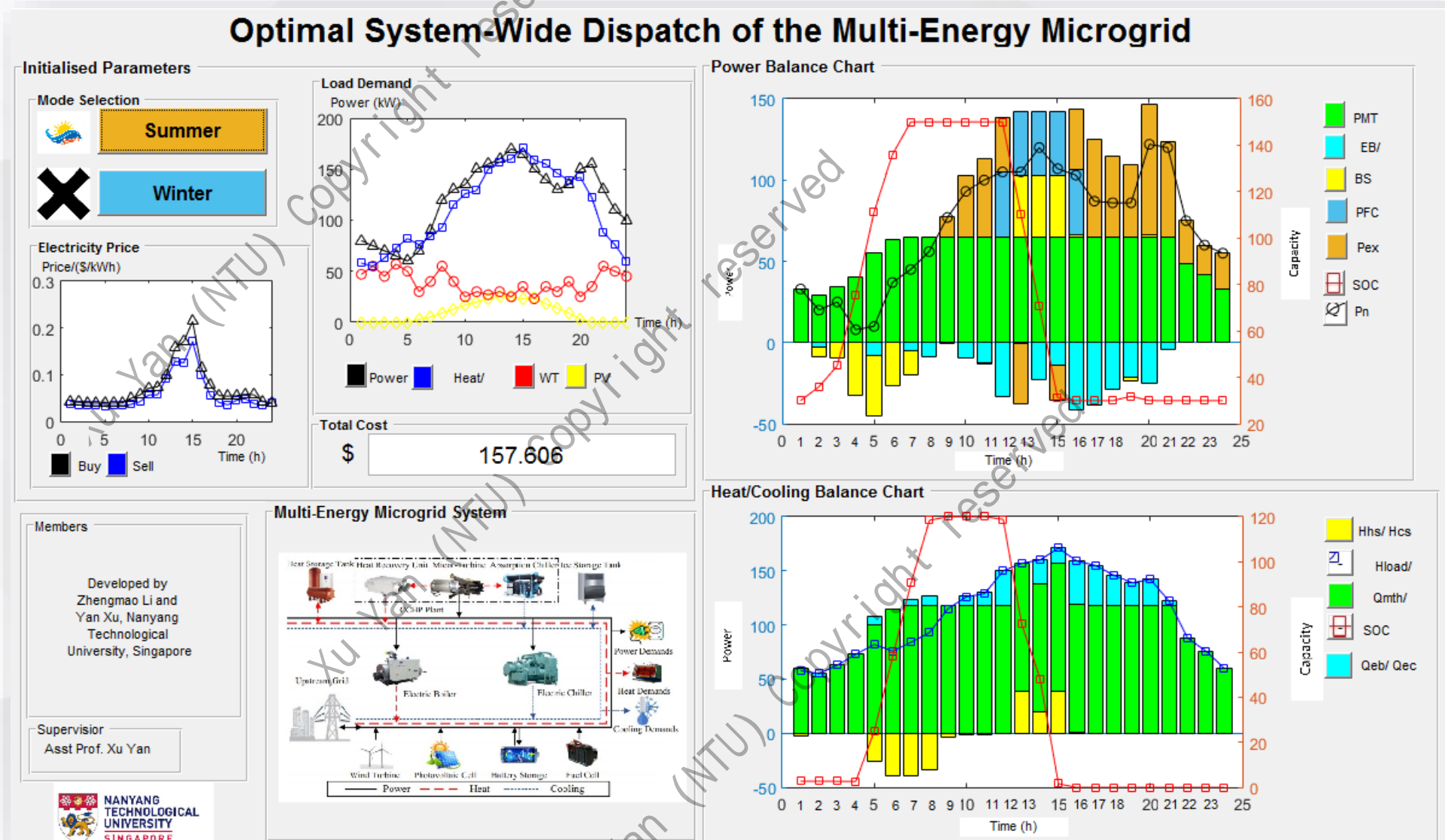
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Multi-Energy Dispatch GUI Prototype



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

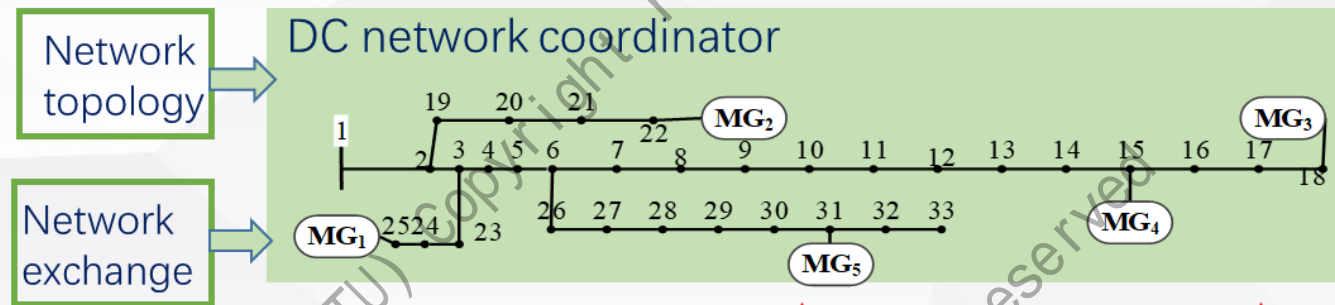
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Robustly Coordinated Energy Management Distributed robust optimization for Networked-Hybrid AC/DC Microgrids



Individual MG

$$\min_{\mathbf{P}_i(t), \beta_i(t), \forall t \in \mathcal{T}} \mathbb{E} \sum_{t \in \mathcal{T}} f(\mathbf{P}_i(t), \beta_i(t)) =$$

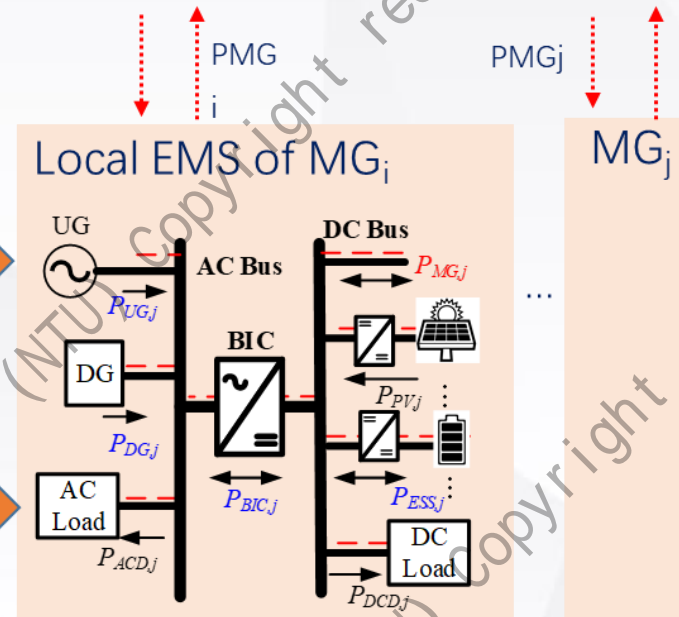
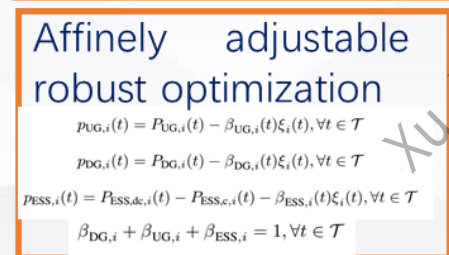
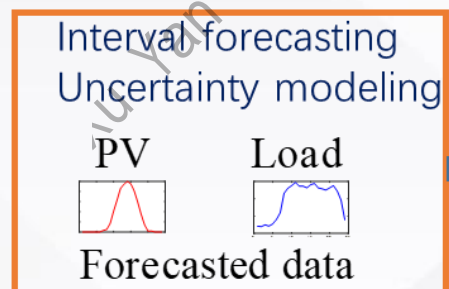
$$\sum_{t \in \mathcal{T}} [a_{DG,0,i} P_{DG,i}^2(t) + a_{DG,1,i} P_{DG,i}(t) + a_{DG,2,i} +$$

$$a_{DG,0,i} \beta_{DG,i}^2(t) + b_{PV,i} P_{PV,i}(t) + \lambda(t) P_{UG,i}(t) +$$

$$c_{ESS,dc,i} P_{ESS,dc,i}(t) + c_{ESS,c,i} P_{ESS,c,i}(t)] \Delta t$$

Networked-MG

$$\min_{\mathbf{P}_j(t), \beta_j(t), \forall j \in \mathcal{N}, j \rightarrow k \in \mathcal{E}, t \in \mathcal{T}} \mathbb{E} \sum_{t \in \mathcal{T}} \{f(\mathbf{P}_i(t), \beta_i(t)) + \sum_{j:j \rightarrow k} l_{jk}(t) r_{jk}\}$$



1. Affinely adjustable robust optimization modeling
2. Model convexification
3. Distributed solution based on ADMM

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

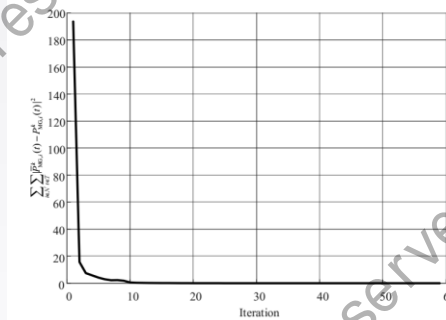
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Simulation results

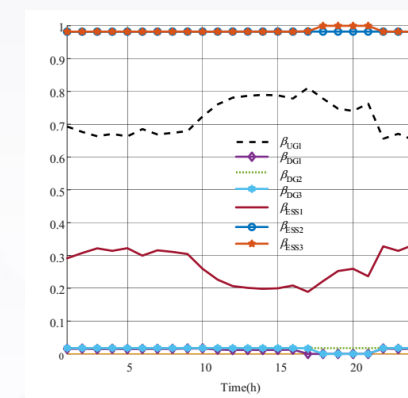
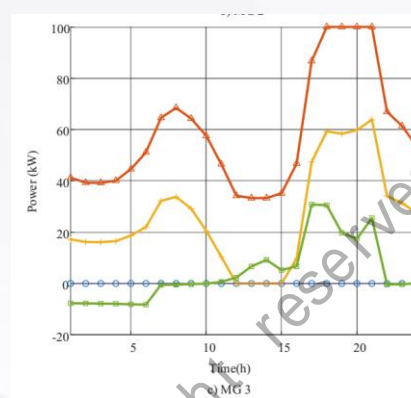
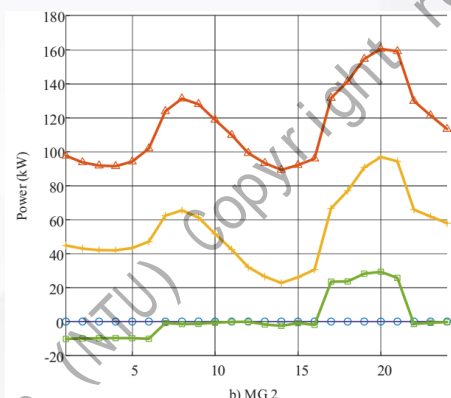
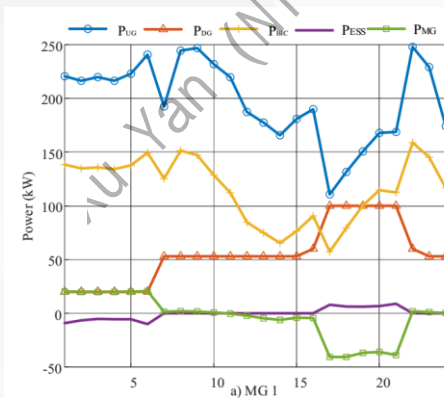
A 3 networked microgrid system in an IEEE 4 bus system

Scenario I: centralized deterministic;
Scenario II: centralized stochastic; (100)
Scenario III: proposed

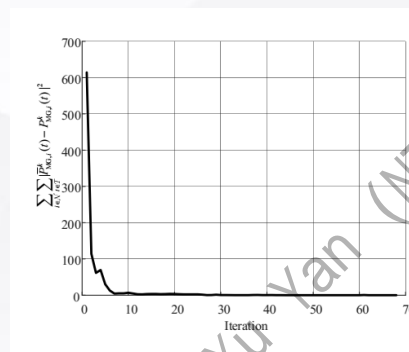
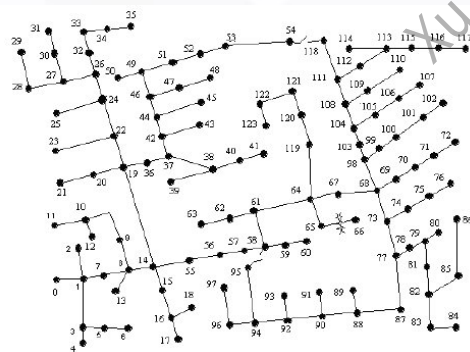


COMPARISON RESULTS UNDER CASE I (A SYSTEM OF THREE NETWORKED MGs)

	Scenario <i>i</i>		
	I	II	III
Objective value(\$)	2,484.84	2,483.89	2,580.33
Running time(s)	0.17	308.14	4.85
Number of decision variables	864	2232	2520
Number of constraints	792	73008	1944



A 30 networked microgrid system in a revised IEEE 123 bus system



COMPARISON RESULTS UNDER CASE II (A SYSTEM OF 30 NETWORKED MGs)

	Scenario <i>i</i>		
	I	II	III
Objective value(\$)	17,849.00	17,840.87	17,849.24
Running time(s)	1.28	471.37	368.92
Number of decision variables	16008	666168	31848
Number of constraints	13800	734520	23880

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

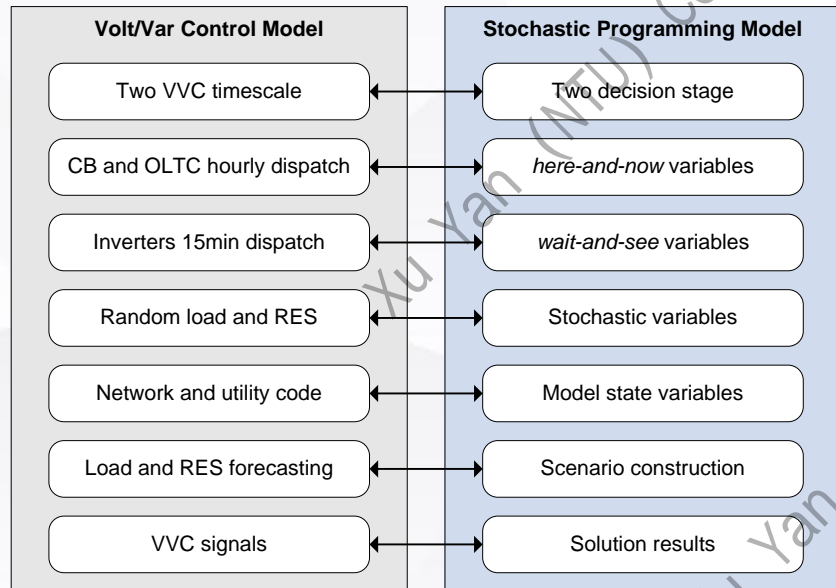
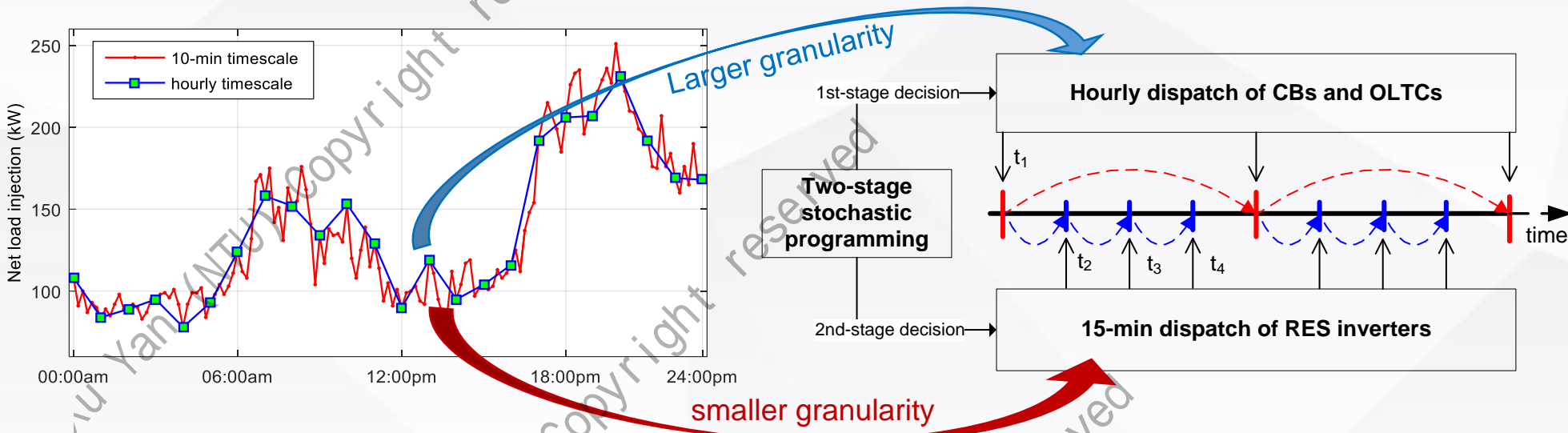
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Two-stage Coordinated Volt/Var Regulation under uncertainty
Hourly dispatch of CB and OLTC & 15min dispatch of PV inverters



- **First-Stage:** Slow switching devices such as OLTCs and CBs are scheduled one day ahead.
- **Second-Stage:** Fast responding devices such as PV-associated inverters are updated to operate in short time-window.

Y. Xu*, Z.Y. Dong, et al, "Multi-timescale coordinated voltage/var control of high renewable-penetrated distribution networks," *IEEE Trans. Power Syst.*, 2018.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Mathematical modeling

A. Stochastic Model

The VVC is realized at two coordinated timescales and the mathematical model of (5)–(21) is formulated into a two-stage stochastic programming model as follows:

$$\min_{x \in F} \{f(x) + E[Q(x, \xi)]\} \quad (22)$$

where $f(x)$ is the first-stage problem, i.e., the long-term (hourly timescale) VVC, and x is the first-stage decision vector; $Q(x, \xi)$ is optimal value of the second-stage problem, i.e., the short-term (15-min timescale) VVC: $\min_{y \in \Omega(x, \xi)} g(y)$, where y is the second-stage decision vector, ξ is the random vector, and $E[Q(x, \xi)]$ is the expected value of the second-stage problem.

C. Scenario Construction

The stochastic variations of RES generation and load from their predicted values are assumed to respectively follow the Beta distribution and the normal distribution [5], [6], [20].

The Beta distribution is defined by two shape parameters: α and β which represent the prediction error (stochastic variation) for a predicted power \hat{P} [20]:

$$f_{\hat{P}}(y) = y^{\alpha-1} \cdot (1-y)^{\beta-1} \cdot N \quad (27)$$

where f is the Beta distribution function and y is the occurrence of the active power value, N is the normalization factor.

B. Deterministic Equivalent

Assuming ξ has a finite number of possible realizations, called scenarios, denoted as ξ_1, \dots, ξ_K with respective possibilities of ρ_1, \dots, ρ_k , then the expectation term in (22) can be written as:

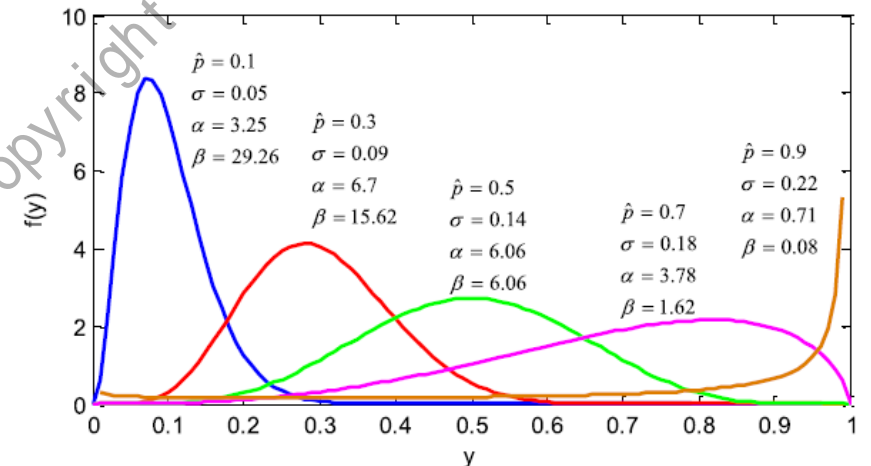
$$E[Q(x, \xi)] = \sum_{k=1}^K \rho_k Q(x, \xi_k) \quad (23)$$

Then, the original two-stage stochastic programming model can be reformulated as the following *deterministic equivalence*:

$$\min_{x, y_1, \dots, y_K} f(x) + \sum_{k=1}^K \rho_k g(y_k) \quad (24)$$

$$\text{s.t. } x \in F \quad (25)$$

$$y_k \in \Omega(x, \xi_k), \forall k \quad (26)$$



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

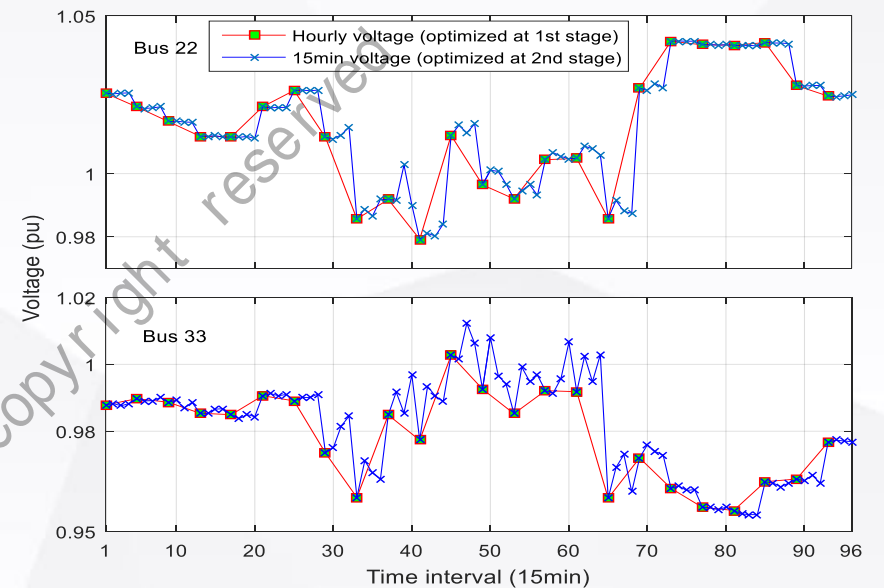
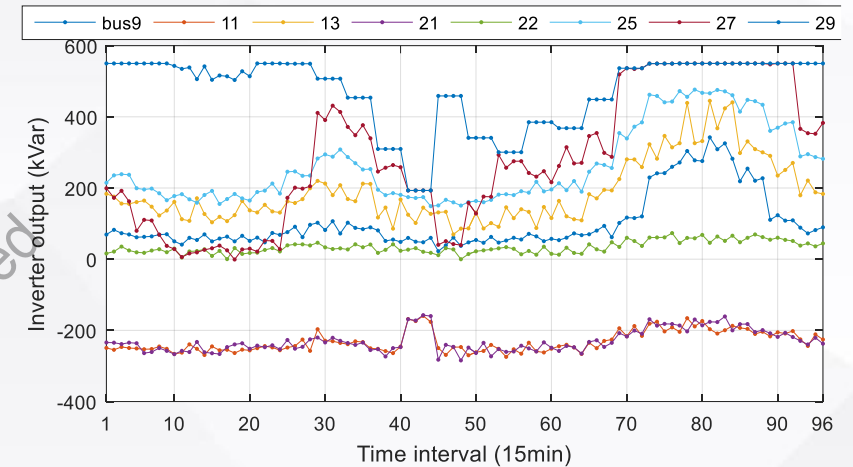
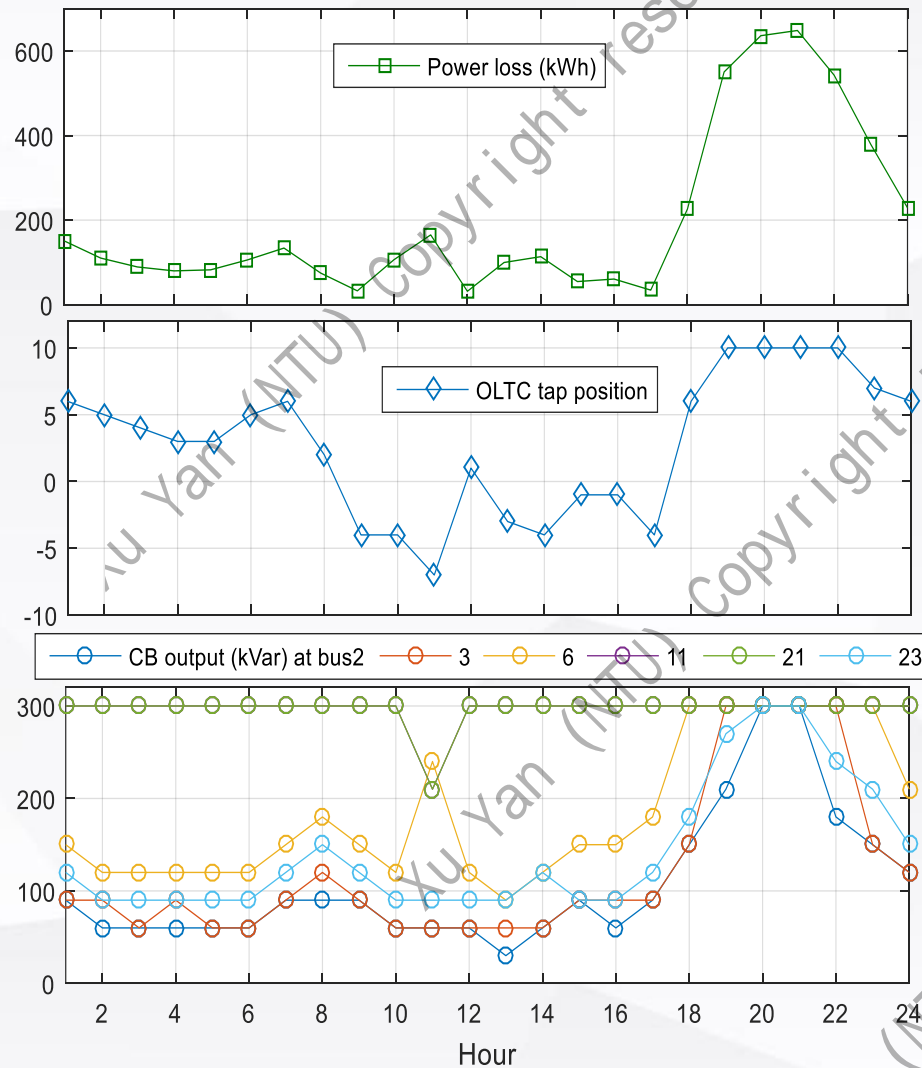
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Simulation Results



Y. Xu*, Z.Y. Dong, et al, "Multi-timescale coordinated voltage/var control of high renewable-penetrated distribution networks," *IEEE Trans. Power Syst.*, 2018.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm



Multi-Objective Adaptive Robust Voltage/VAR Regulation

- **Minimizing voltage deviation conflicts with minimizing network power loss.**
- **Multi-objective “min-max-min” problem**

$$\min_x \max_u \min_y [f_1(x, u, y), f_2(x, u, y)]$$

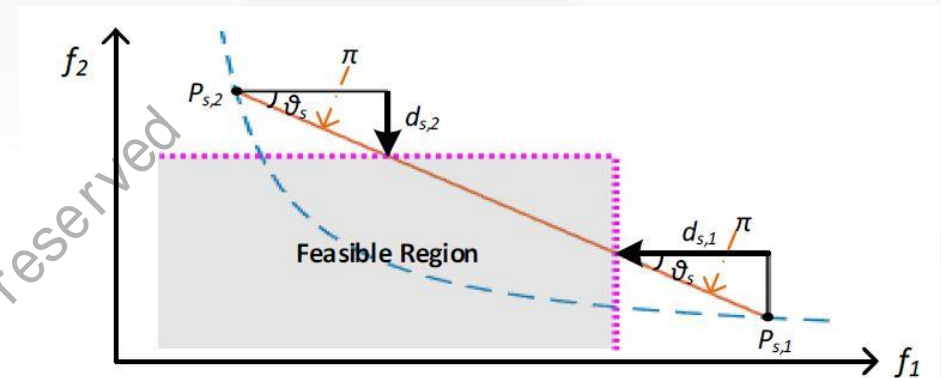
s.t.

$$Ax \geq b$$
$$Cx + Dy \leq v$$
$$Ex + Gy + Hu = w$$
$$u \in U$$

Key point:

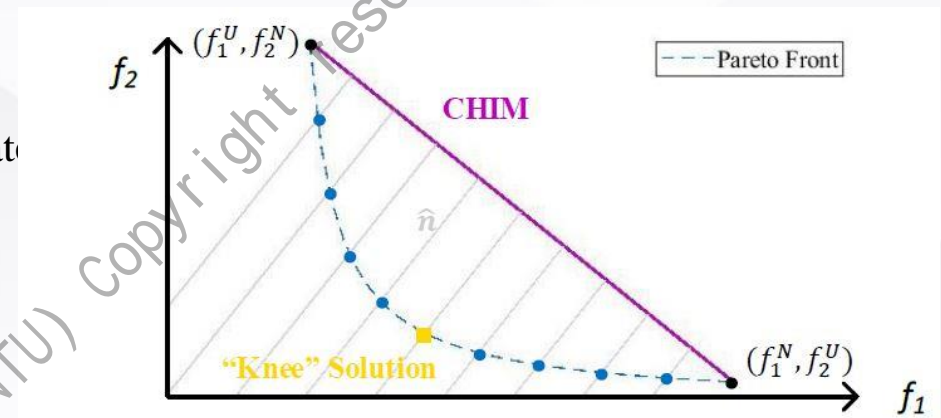
- 1) **Voltage deviation index:** load-weighted voltage deviation index (LVDI)
- 2) **Which MOP algorithm is more efficient** to generate accurate Pareto front and get a fair trade-off?
 - a) Classic Weighted-Sum (CWS)
 - b) Classic ϵ -Constrained (CeC)
 - c) **Adaptive Weighted-Sum (AWS)**
 - d) **Normal Boundary Intersection (NBI)**

Adaptive Weighted Sum (AWS)



Reduced feasible region used in AWS algorithm.

Normal Boundary Intersection (NBI)



Pareto front generated by NBI algorithm.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

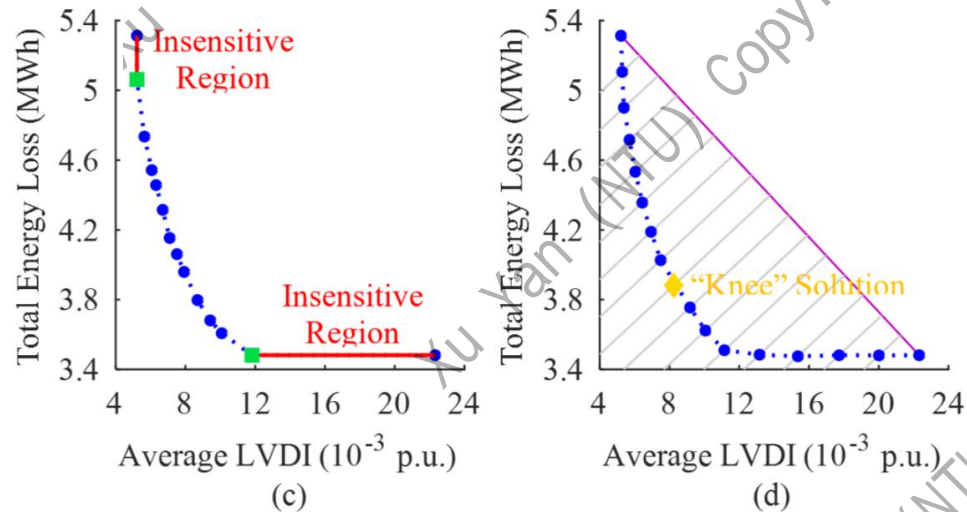
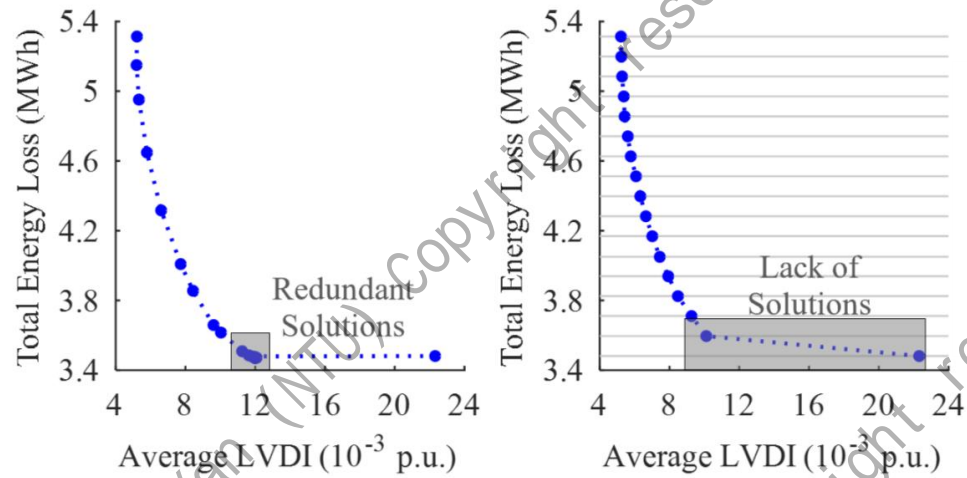
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Multi-Objective Adaptive Robust Voltage/VAR Regulation



(a) CWS; (b) CeC; (c) AWS; (d) NBI

COMPUTATION EFFICIENCY COMPARISON

Method	CWS	CeC	AWS	NBI
Number of Solutions	17	17	14	17
MOP Processing Time (s)	53	62	44	60
GUROBI Solver Time (s)	569	2344	869	2384
Total Time (s)	622	2406	913	2444

The AWS and NBI algorithms are suggested depending on different optimization requirements.

- ✓ If a relatively accurate Pareto front with high computation efficiency is required, the **AWS** algorithm is preferred.
- ✓ If a more accurate Pareto front with evenly distributed solutions or the “knee” solution is required, the **NBI** algorithm is preferred.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

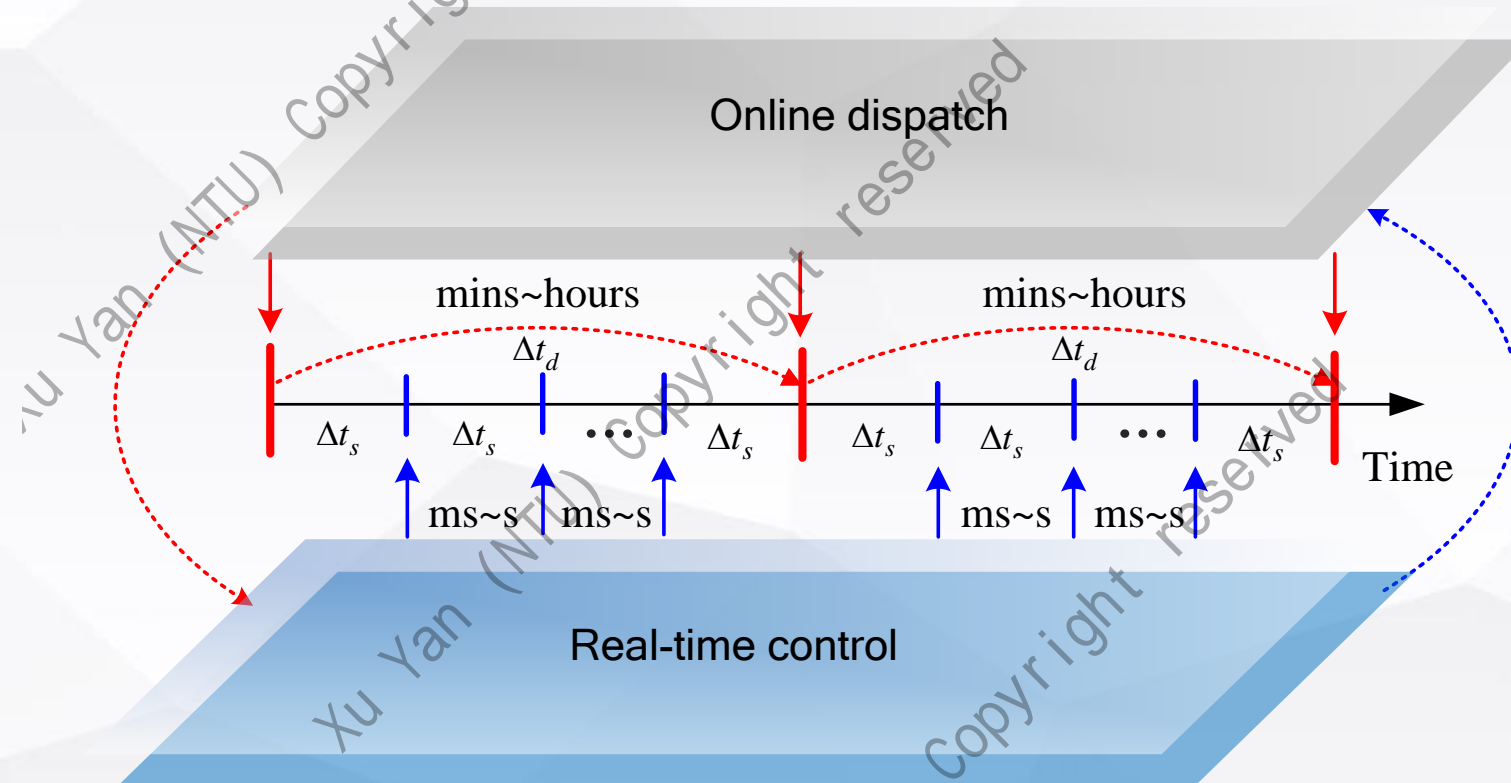
4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

▪ Hierarchically coordinated operation and control of DERs

- ✓ Operational optimization and real-time control are traditionally decoupled.
- ✓ Existing two-stage coordination methods are all for operational timeframe (e.g., day-ahead & hourly-ahead or hourly-ahead & 15mins-ahead).



- ✓ Need to coordinate the operation level and control level for enhanced system performance, i.e., optimizing the operation decisions considering the real-time controllers' effects, or simultaneously optimizing operational variables and controller parameters.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

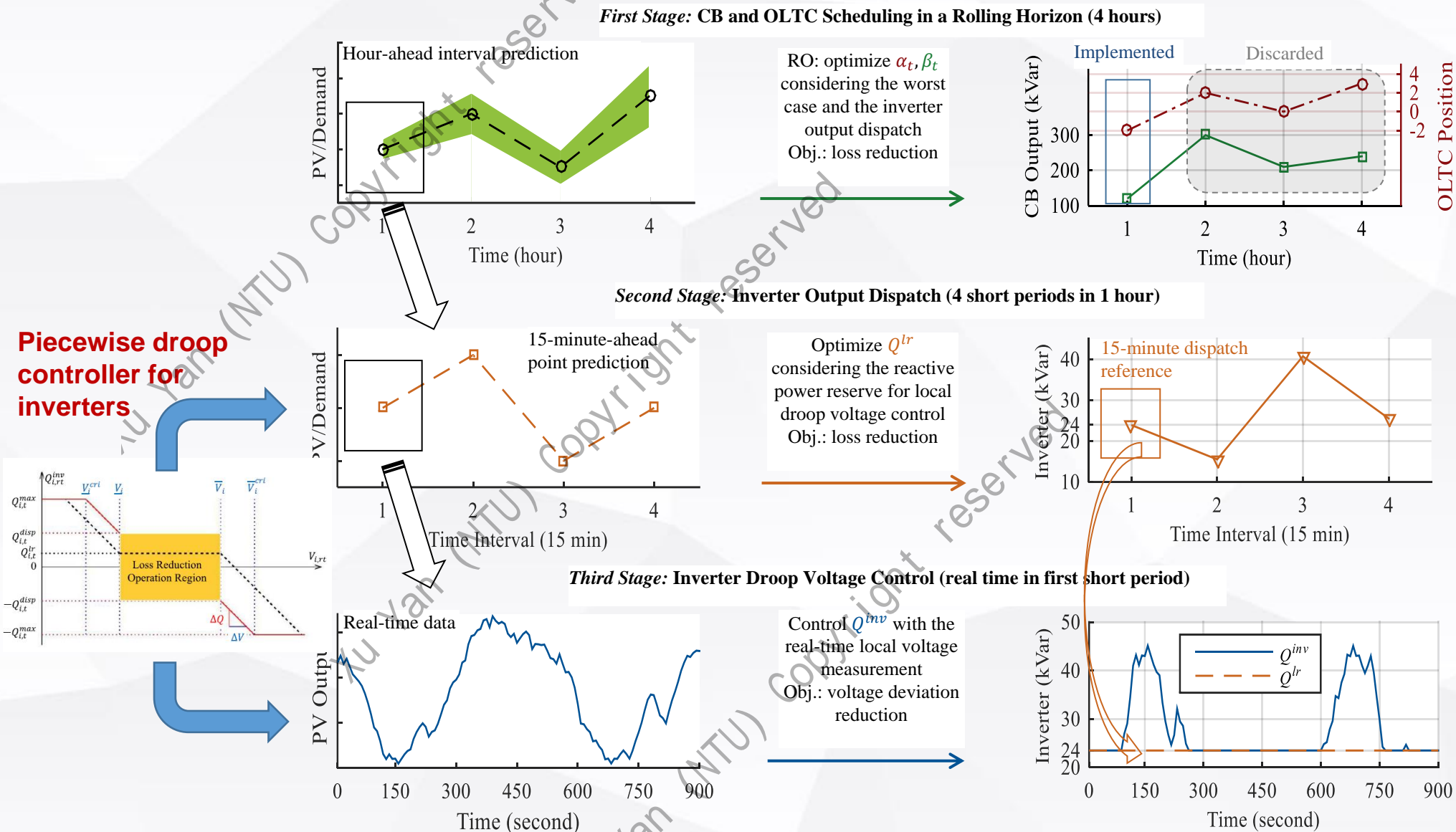
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Three-Stage Robust Volt/Var Control (TRI-VVC)



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

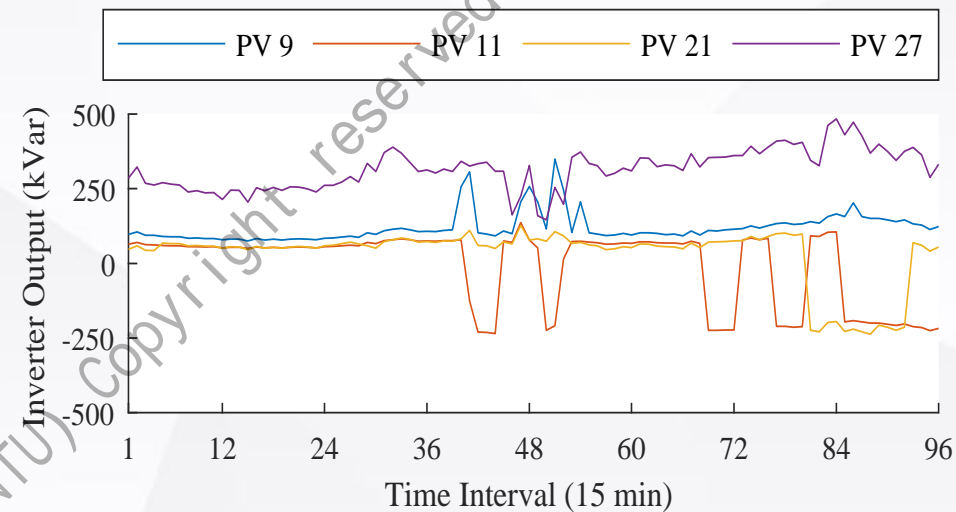
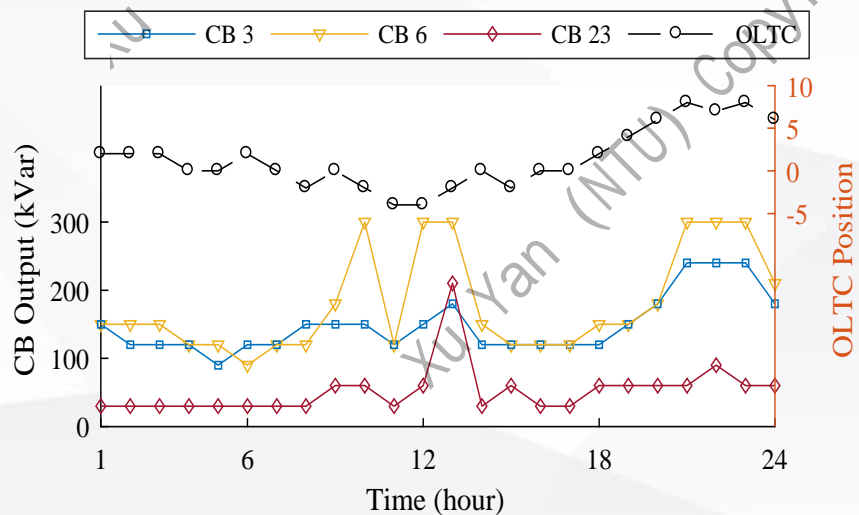
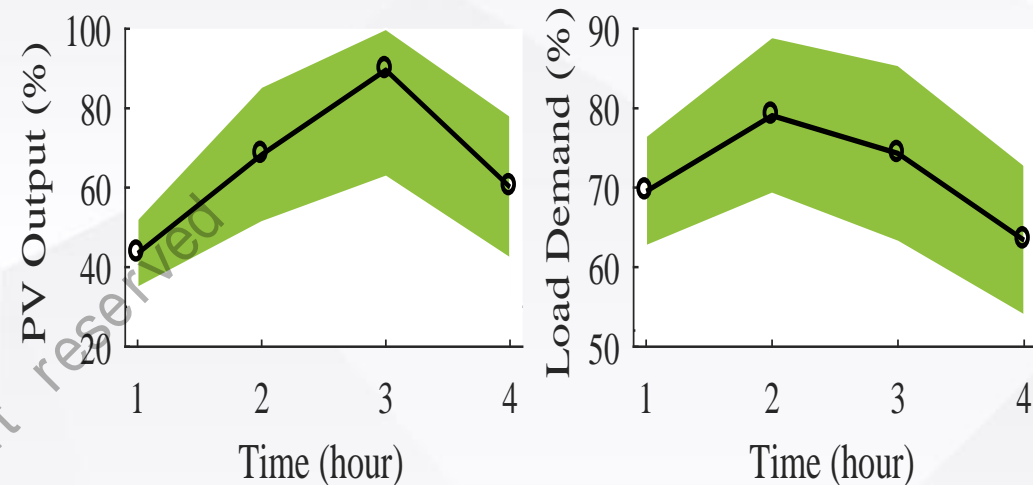
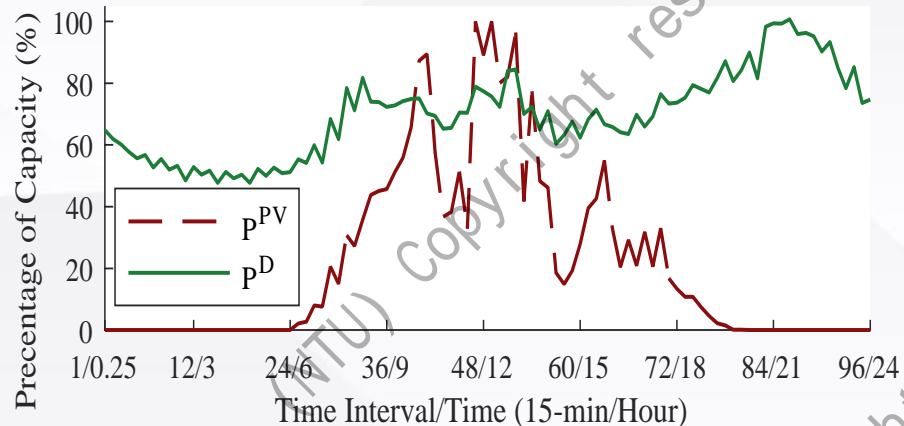
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Simulation Results



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

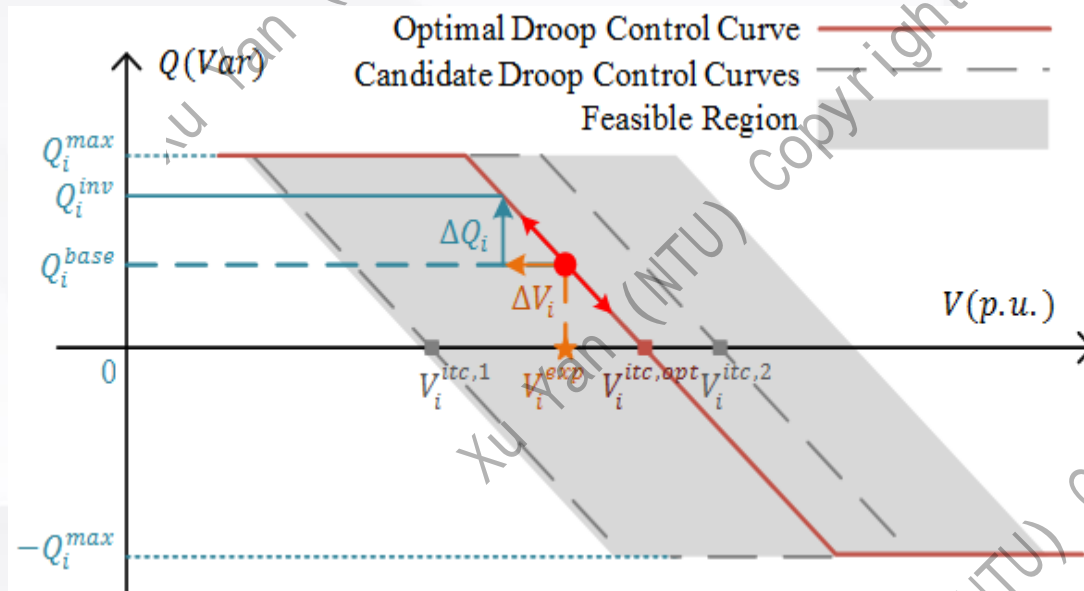
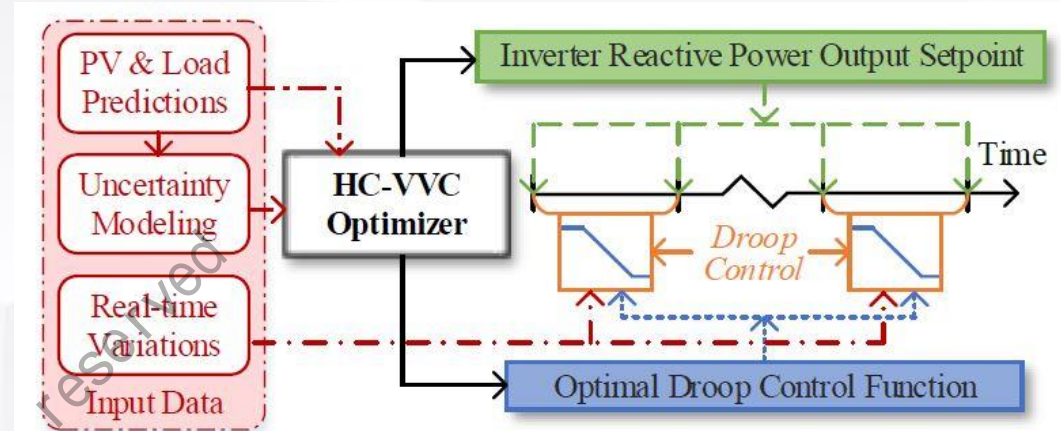
4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

▪ Hierarchically-Coordinated Voltage/VAR Control (HC-VVC)

- ✓ Central VVC considers the network level information (power flow)
- ✓ Local VVC focuses on the real-time variation (bus voltage)



linear droop controller for inverters

Inverter Droop Control Model

- The central VVC hierarchy implements the base reactive power output setpoint of each inverter, i.e. Q_i^{base} under the expected operating condition.
- The local VVC hierarchy implements the local droop control by adjusting the reactive power output responding to the local voltage deviation. $\Delta Q = f(\Delta V)$

C. Zhang and Y. Xu*, "Hierarchically-Coordinated Voltage/VAR Control of Distribution Networks Using PV Inverters," *IEEE Trans. Smart Grid*, 2020.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

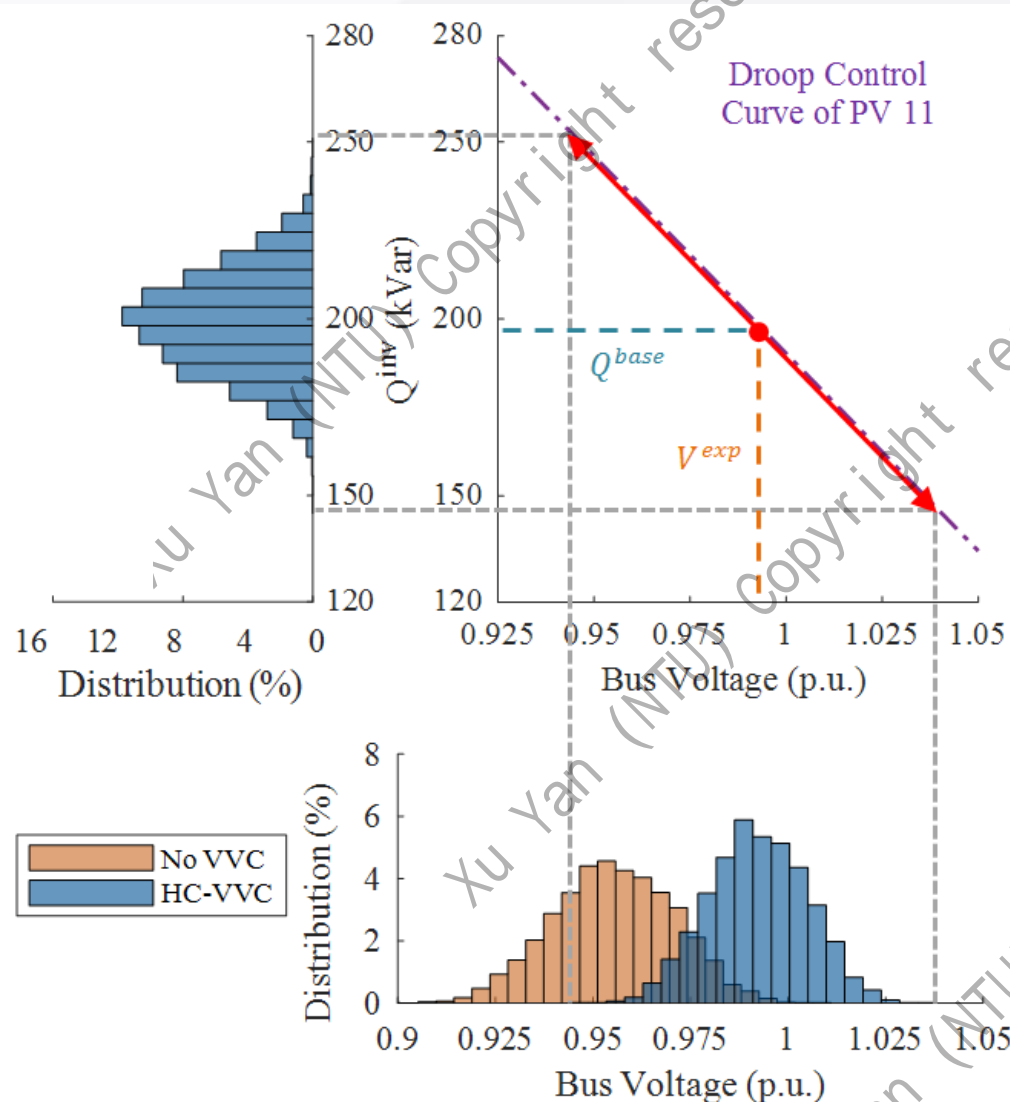
4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm



▪ Hierarchically-Coordinated Voltage/VAR Control (HC-VVC)



Voltage control results:

In response to the local bus voltage variation, the inverter reactive power output moves along the droop control curve.

The mean bus voltage magnitude with the HC-VVC is very close to 1 p.u.

COMPARISON RESULTS FOR DIFFERENT VVC METHODS

Method	#1	#2	#3	HC-VVC
Average Power Loss (kW)	24.1	32.9	110.3	26.7
Voltage Violation Rate (%)	3.4%	0.2%	51.8%	0.1%
Average Voltage (p.u.)	0.990	0.998	0.971	0.993
Average Absolute Voltage Deviation (p.u.)	0.012	0.010	0.029	0.009

Comparison with other VVC methods

HC-VVC: least voltage violation rate; least voltage magnitude deviation; second least average power loss; second average voltage close to 1 p.u.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

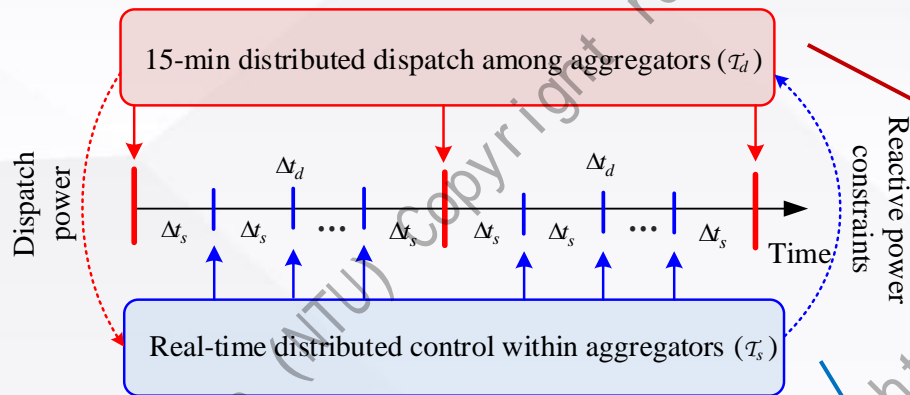
4. Hierarchy coordination

5. Planning

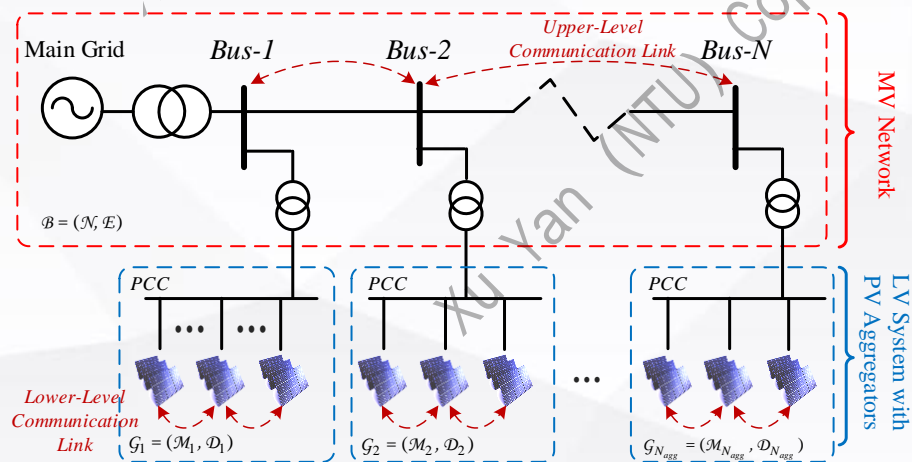
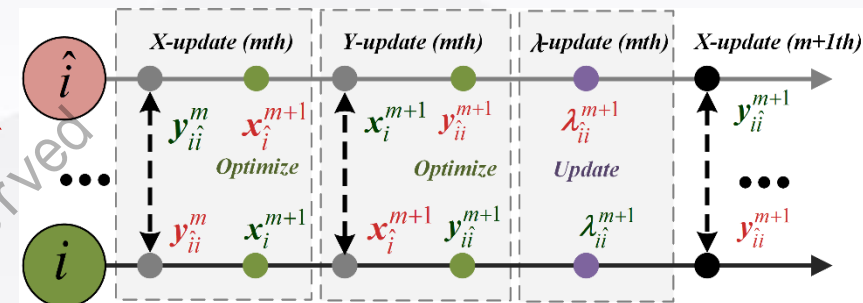
- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Fully Distributed Two-Level Volt/Var Control

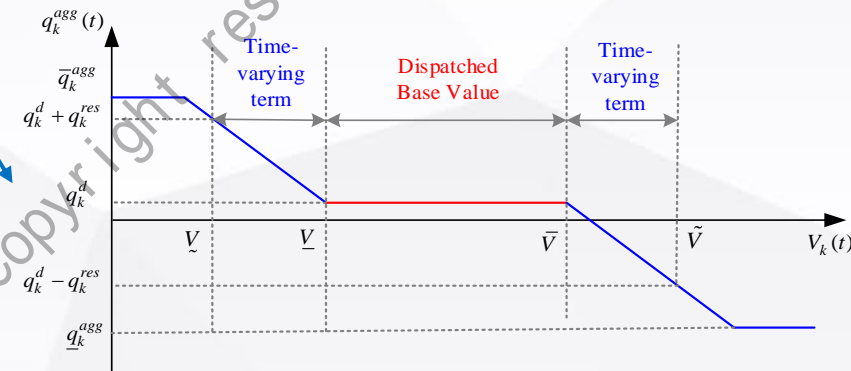
Two-level VVC with time scale coordination



Distributed dispatch by ADMM



Distributed real-time voltage control



Y. Wang, T. Zhao, C. Ju, Y. Xu*, P. Wang "Two-Level Distributed Voltage/Var Control of Aggregated PV Inverters in Distribution Networks," *IEEE Trans. Power Delivery*, 2019.

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

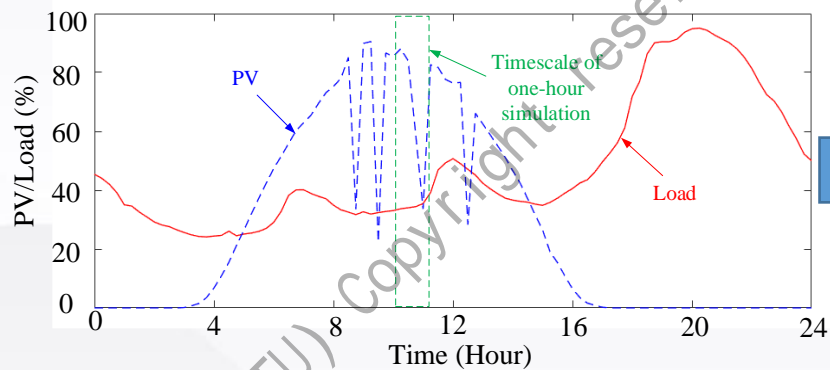
4. Hierarchy coordination

5. Planning

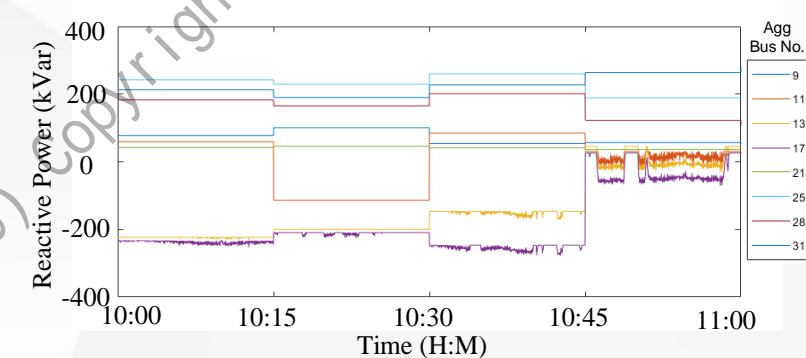
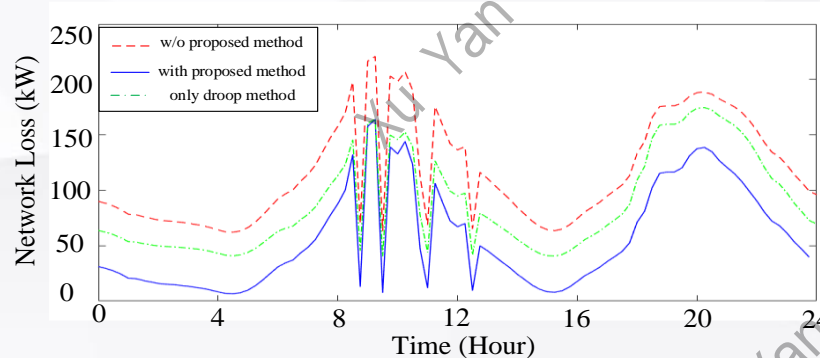
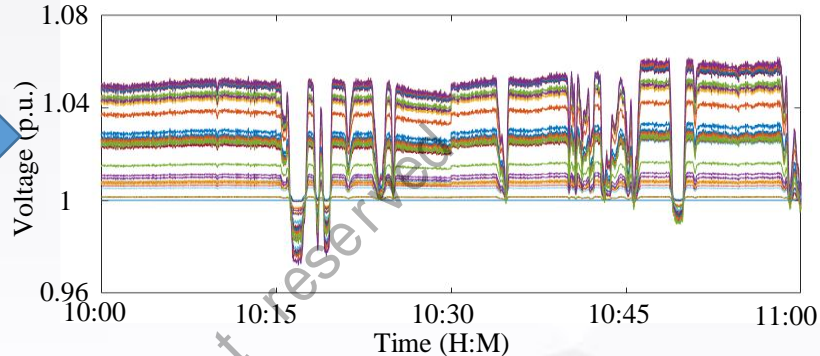
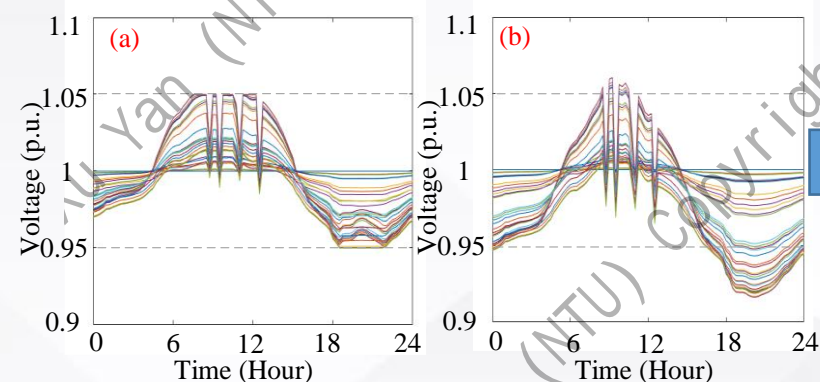
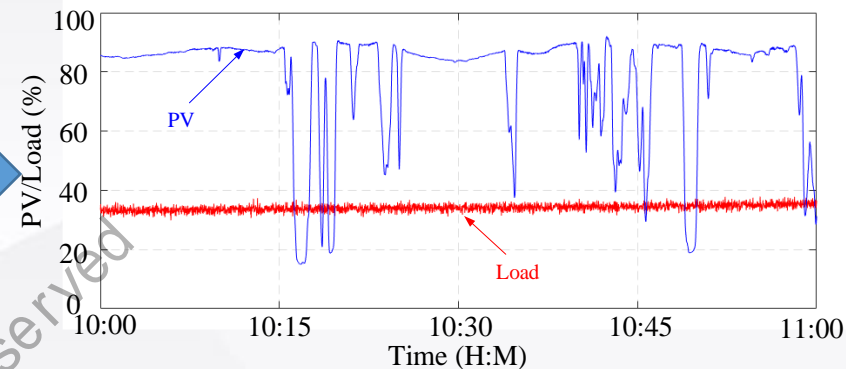
- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Simulation Results

24-hour simulation with 15 minutes sampling



One-hour simulation with 1 second sampling



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

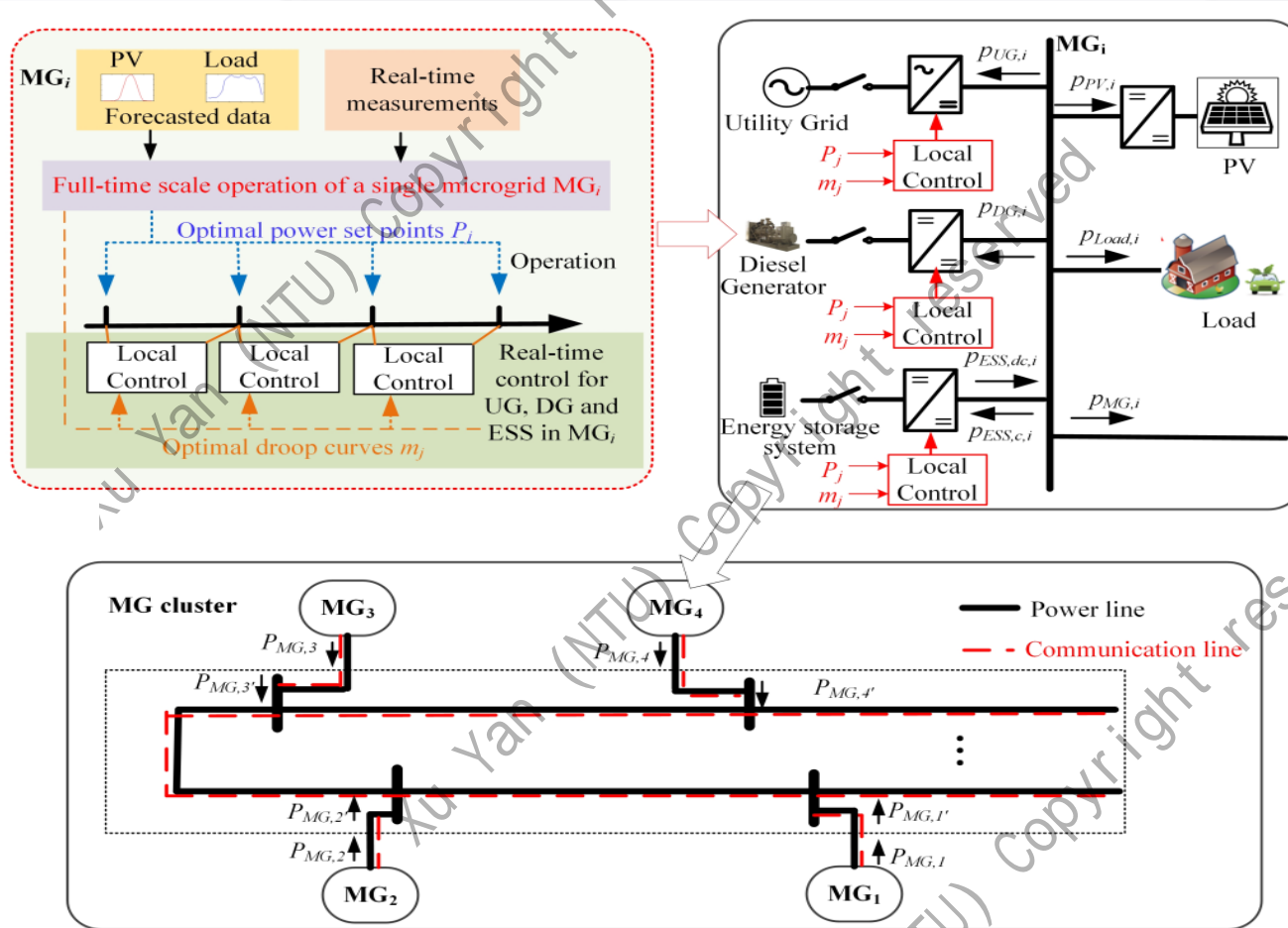
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Hierarchically Coordinated Operation and Control for DC microgrid clusters



$$\min_{\mathbf{P}_j(t), \beta_j(t), P_{jk}(t), l_{jk}(t), v_j(t)} \mathbb{E} \sum_{t \in \mathcal{T}} \{f(\mathbf{P}_i(t), \beta_i(t)) + \sum_{j:j \rightarrow k} l_{jk}(t) r_{jk}\} \quad \forall j \in \mathcal{N}, j \rightarrow k \in \mathcal{E}, t \in \mathcal{T}$$

$$p_{UG,i} - P_{UG,i} = \beta_{UG,i} \xi_i$$

$$p_{DG,i} - P_{DG,i} = \beta_{DG,i} \xi_i$$

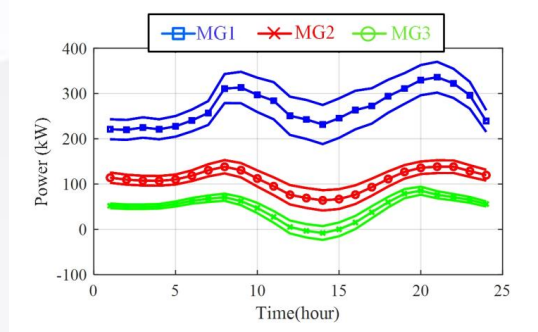
$$p_{ESS,i} - P_{ESS,dc,i} + P_{ESS,c,i} = \beta_{ESS,i} \xi_i$$

$$\beta_{UG,i} + \beta_{DG,i} + \beta_{ESS,i} = 1$$

$$m_{UG,i} = \frac{k_i}{\beta_{UG,i}}, m_{UG,i} \in \left(0, \frac{\Delta V_{\max}}{P_{UG,\max}}\right)$$

$$m_{DG,i} = \frac{k_i}{\beta_{DG,i}}, m_{DG,i} \in \left(0, \frac{\Delta V_{\max}}{P_{DG,\max}}\right)$$

$$m_{ESS,i} = \frac{k_i}{\beta_{ESS,i}}, m_{ESS,i} \in \left(0, \frac{\Delta V_{\max}}{P_{ESS,\max}}\right)$$



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

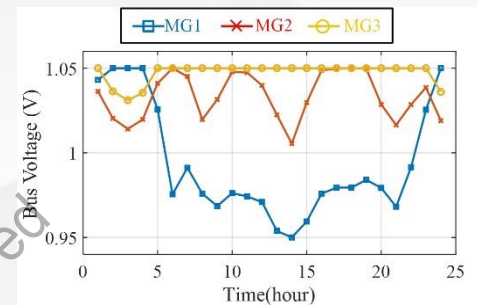
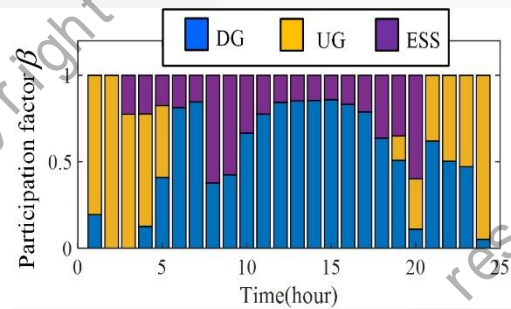
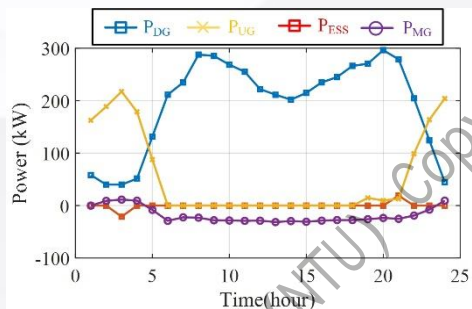
4. Hierarchy coordination

5. Planning

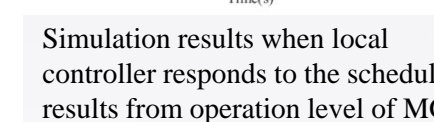
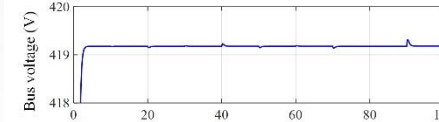
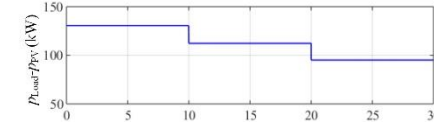
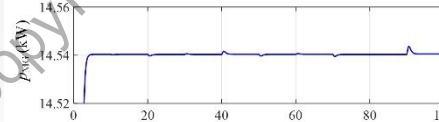
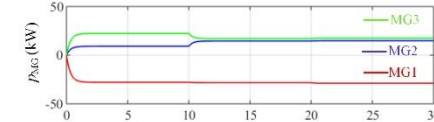
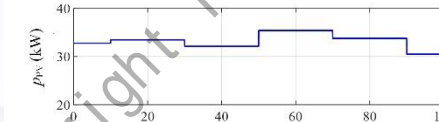
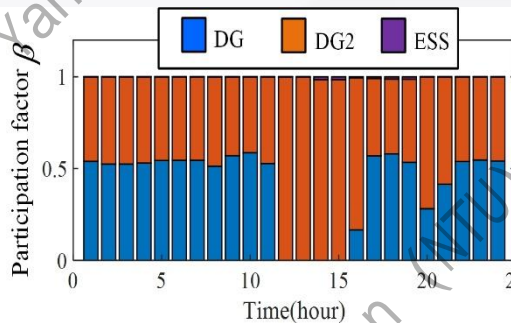
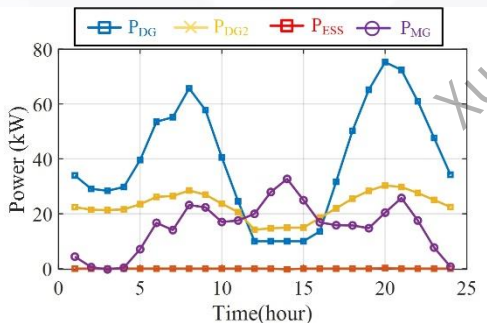
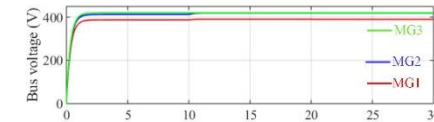
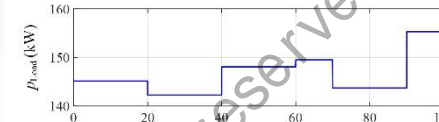
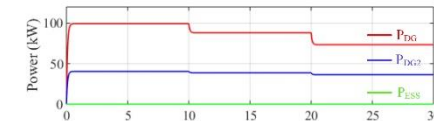
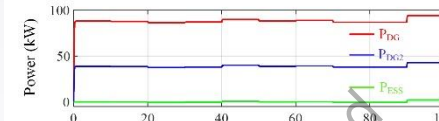
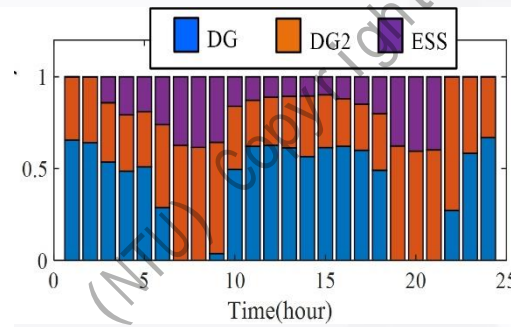
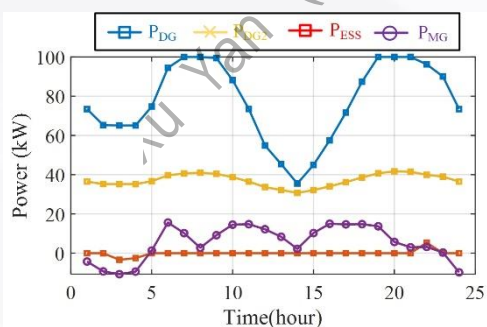
- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

- Hierarchically Coordinated Operation and Control for DC microgrid clusters

Dispatch results



Real-time control results



Q. Xu, Y. Xu*, et al, " A Hierarchically Coordinated Operation and Control Scheme for DC Microgrid Clusters under Uncertainty," *IEEE Transactions on Sustainable Energy*, 2020.

Simulation results of MG2 during 9h-10h with PV and load fluctuations in Matlab/Simulink.

Simulation results when local controller responds to the scheduling results from operation level of MG2 at 9h, 10h and 11h (which is at 10s, 20s and 30s in the simulation)



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

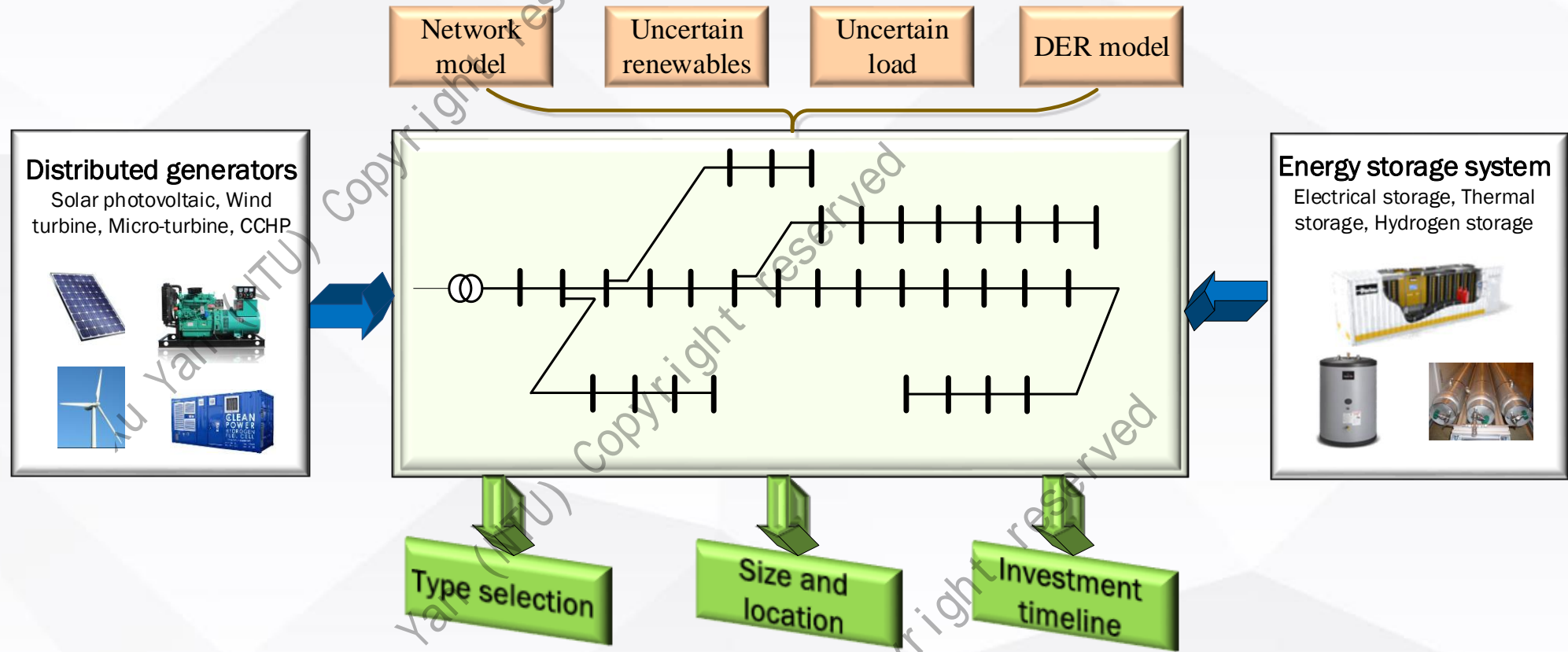
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Optimal Planning of DERs in Microgrid



Objective: Minimize total investment costs

Constraints: operational limits
network constraints
component constraints, etc.

Variables: size, site, type, installation year, etc.

Stochastic programming

Robust optimization

Probability-weighted robust optimization

...

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

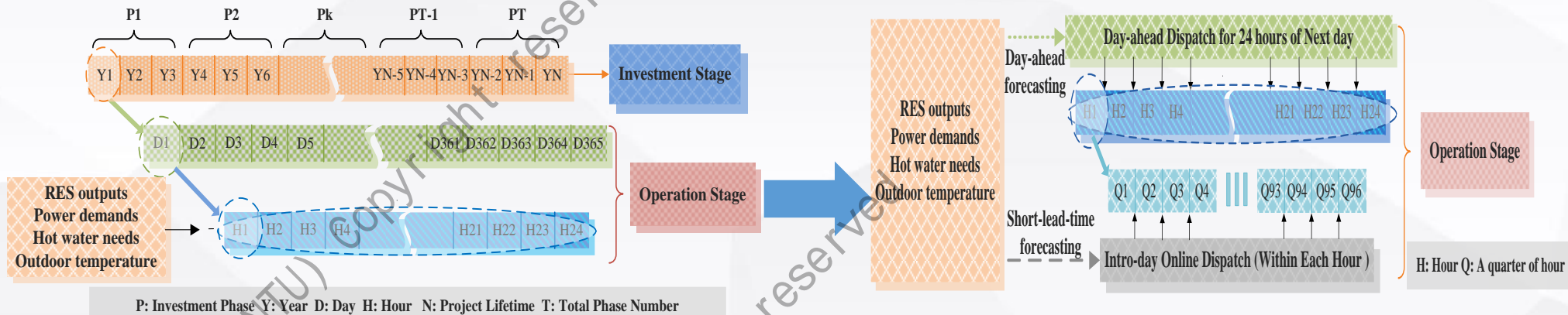
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Optimal Placement of Heterogeneous Distributed Generators



Proposed two-stage DG placement method

$$NPV_s = \underset{z \in CF_z, x \in CG_x}{\text{Max}} \left\{ \underbrace{-F(z)}_{\text{Investment Stage}} + \underbrace{G(x)}_{\text{Operation Stage}} \right\}$$

$$\begin{aligned} \text{Min } G(x|c) &= \text{Min}_w \{ S(w|c) + E[Q(w|c, \omega)] \} \\ \text{s.t. } & w \in CS_w \mid z \\ & Q(w|c, \omega) = \text{Min}_y L(y|c) \\ & y \in CL(w, \omega) \end{aligned}$$

System multi-stage operation model

Sub-stages for system operation

Year/Bus	3	6	9	12	18	22	25	27	30	33
CCHP unit: Cap-65										
1-4	65	195	65	130	0	0	130	65	0	65
5-8	65	195	65	195	0	65	130	65	65	65
9-12	65	195	65	195	65	65	130	65	65	130
Electric boiler: A										
1-4	123.2	96	90.7	0	146.8	41.5	167.8	92.9	0	0
5-8	123.2	96	128.1	0	146.8	88.5	214.8	92.9	0	0
9-12	138.5	96	129.6	0	146.8	120.4	216.2	92.9	0	0
Electric boiler: B										
9-12	0	0	0.0	57.1	0	66.7	74.1	0	0	0
Electric chiller: A										
1-4	200.2	0	68.4	0	105.8	0.0	141.3	0	0	48.25
Electric chiller: B										
1-4	0	0	25.0	0	0	50.7	74.3	0	0	0
5-8	0	0	50.3	0	0	103.8	115.2	0	0	0
9-12	0	0	90.9	0	0	143.0	115.2	0	0	0
Photovoltaics: B										
1-12	137.6	137.6	136.2	122.2	118.9	137.7	181.6	181.6	177.8	169
Wind turbine: A										
1-12	80	0	0	0	0	80	80	0	80	0
Wind turbine: B										
1-12	0	240	120	0	240	0	240	0	120	0

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

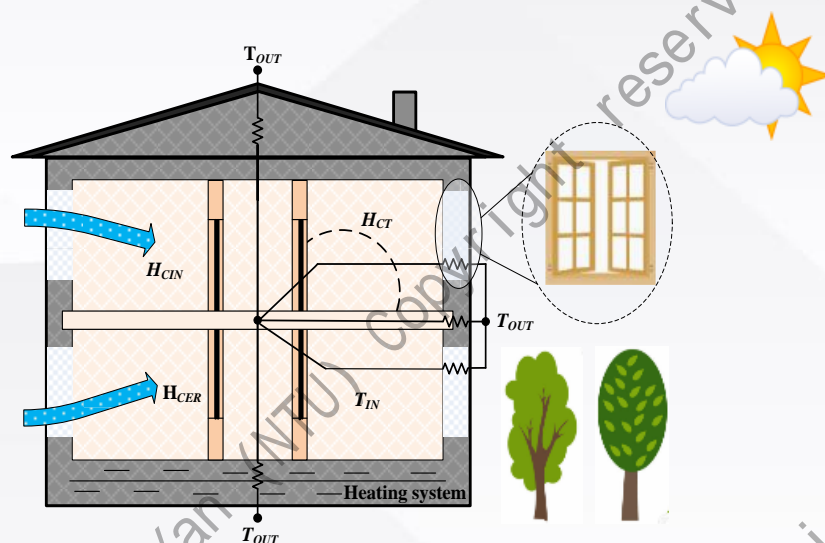
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

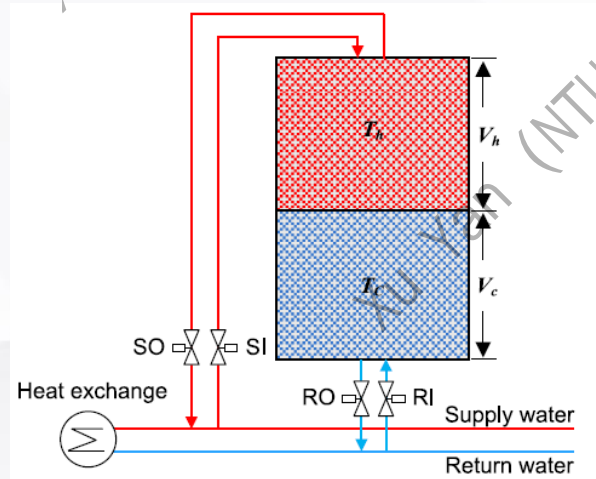
5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Optimal Deployment of Heterogeneous Energy Storage



Typical structure of a room in a residential building



Structure of the thermal storage

$$\max_{z \in Z, x \in X, \eta_{VaR} \in \mathfrak{R}} [C_{EDP} - \rho_{RK} CVaR_{\alpha}(C_{EDP})]$$

$$\text{s.t.}, C_{EDP} = \frac{1}{365 \times N_P} \cdot \frac{dr(1+dr)^{N_P}}{(1+dr)^{N_P} - 1}$$

$$\cdot \left[\underbrace{-F(z)}_{\text{Investment Stage}} + \underbrace{G(x)}_{\text{Operation Stage}} \right]$$

$$CVaR_{\alpha}(C_{EDP}) = \eta_{VaR} + \frac{1}{1 - \alpha_{CL}} E$$

$$\times [\max(C_{EDP} - \eta_{VaR}, 0)]$$

Risk-averse objective function

$$\text{Min}_x G(x) = \text{Min}_{w, y_1, y_2, \dots, y_q} [S(w) + \sum_{q \in N_Q} c_q L(y_q)]$$

$$\text{s.t.} \quad w \in CS_w | z$$

$$y_q \in CL(w, \omega_q), \forall q$$

Proposed multi-stage stochastic deployment model

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

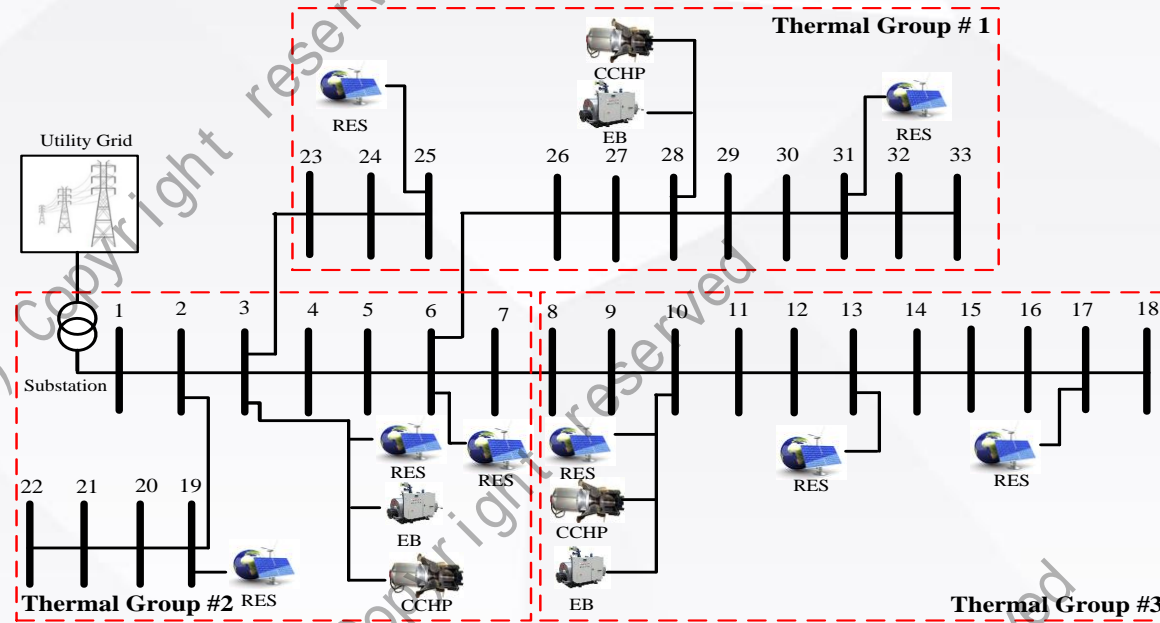
- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

■ Planning results



Deployment Results For Battery Storage (kWh)

Year/Bus	3	6	18	22	25	27	30	33
1-3	1500	0	0	1500	1500	0	0	0
4-6	1500	466.0	101.7	1500	1500	0	0	473.2
7-9	1500	466.0	101.7	1500	1500	378.0	81.19	473.2

Deployment Results For Thermal Storage (kWh)

Year 1-9	Group 1	Group2	Group3
Cooling storage tank	0	0	0
Heat storage tank	1800	1800	1800

0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Probability-Weighted Robust Optimization (PRO) for DG Planning

Problems identification: Robust optimization only considers the worst case under a single day profile, while stochastic programming cannot cover full spectrum of uncertainties and thus full operational robustness.

Our aims: to ensure a full robustness for the short-term operation under the uncertainties over the long-term planning horizon.

Probability-Weighted Uncertainty Sets

$$U_v^D = \{ \underline{\mu}_{y,v}^D \leq \sum_{t \in T} \sum_{i \in I} h \times P_{i,t,y,v}^D \leq \bar{\mu}_{y,v}^D, \forall y, \\ \underline{P}_{i,t,y,v}^D \leq P_{i,t,y,v}^D \leq \bar{P}_{i,t,y,v}^D, \forall i, t, y \} \text{ with } \rho_v, \forall v = 1, 2, \dots, n_v$$

PRO Formulation

$$\min_x a^T x + \sum_{n \in N} \rho_n (\max_{u_n \in U_n} \min_{y_n} b^T y_n + c^T u_n) \\ \text{s.t.} \quad Dx \geq e \\ Fx + Gy_n + Hu_n \leq i, \forall n \\ Jx + Ky_n + Lu_n = m, \forall n$$

Solution Algorithm

Initialize the lower bound LB as $-\infty$, the upper bound UB as $+\infty$, $u_{n,0} = u_{n,mean}, \forall n \in N$ and the iteration number $q = 0$

Solve the master problem:
$$\min_x a^T x + \delta$$

s.t.
$$Dx \geq e$$

$$Fx + Gy_{n,p} + Hu_{n,p}^* \leq i, \forall p \leq q, n \in N$$

$$Jx + Ky_{n,p} + Lu_{n,p}^* = m, \forall p \leq q, n \in N$$

$$\delta \geq \sum_{n \in N} \rho_n (b^T y_{n,p} + c^T u_{n,p}^*), \forall p \leq q$$

Obtain the current optimal solution x_q^*, δ_q^* and update LB by $\max\{LB, a^T x_q^* + \delta_q^*\}$

Solve the slave problem:
 $r = 1$, infinite solution number: $v = 0$

Solve $S_{r,q} = \max_{u_{r,q} \in U_r} \min_{y_{r,q}} b^T y_{r,q} + c^T u_{r,q}$
s.t.
$$Fx_q^* + Gy_{r,q} + Hu_{r,q} \leq i$$

$$Jx_q^* + Ky_{r,q} + Lu_{r,q} = m$$

Decision: A finite $S_{r,q}$?
- Yes: Non-Optimal Cut: Obtain the worst case $u_{r,q}^*$ for $S_{r,q}$
- No: Infeasible Cut: Identify the certain $u_{r,q}^*$ for the infeasible $S_{r,q}, v = v + 1$

Add $Fx + Gy_{r,q} + Hu_{r,q}^* \leq i$ and $Jx + Ky_{r,q} + Lu_{r,q}^* = m$ to the master problem

$r = r + 1$

Decision: $r \in N$?
- Yes: Add $u_{n,q}^*, \forall n \in N$ to the master problem as the parameter
Add $\delta \geq \sum_{n \in N} \rho_n (b^T y_{n,q} + c^T u_{n,q}^*)$ to the master problem

Decision: $v = 0$?
- Yes: Update UB by $\min\{UB, a^T x_q^* + \sum_{n \in N} \rho_n (b^T y_{n,q} + c^T u_{n,q}^*)\}$

Decision: $\frac{UB-LB}{|LB|} \leq gap$?
- Yes: Final Optimal Solution x_q^*
- No: $q = q + 1$



0. Outline

1. REIDS Project

2. Control

- 1) Islanded mode
- 2) Grid-tied mode

3. Operation

- 1) Energy dispatch
- 2) Volt/Var regulation

4. Hierarchy coordination

5. Planning

- 1) DG planning
- 2) ESS planning
- 3) PRO algorithm

Probability-Weighted Robust Optimization (PRO) for DG Planning

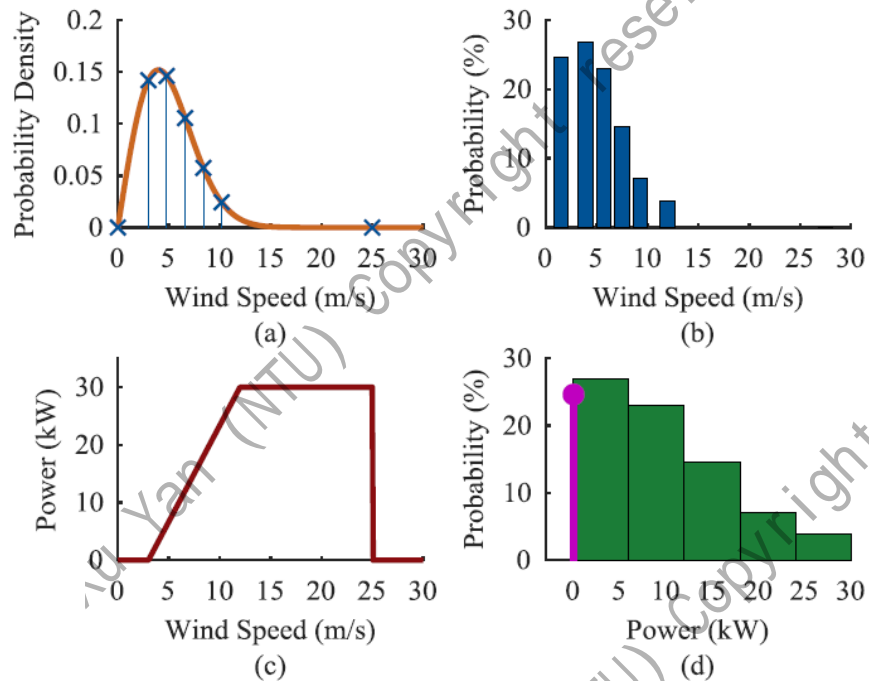


Fig. 3 (a) Wind speed probability density; (b) Wind speed probability; (c) Wind power generation function; (d) Wind power probability.

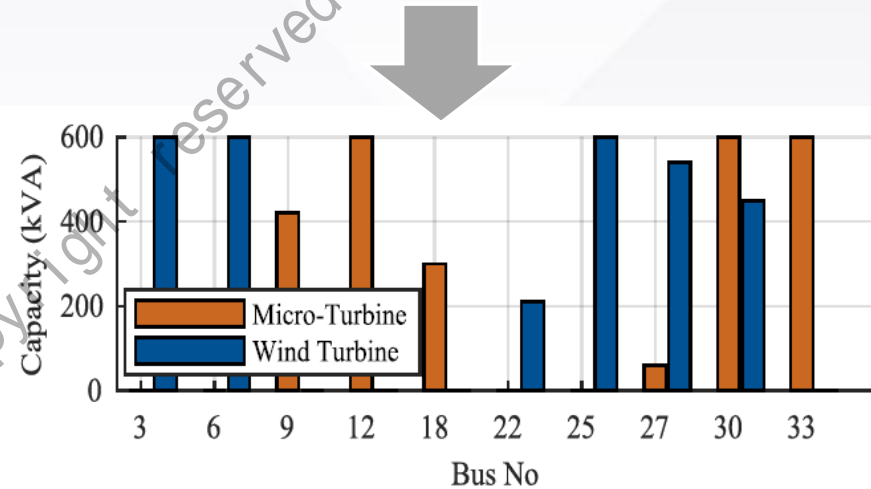
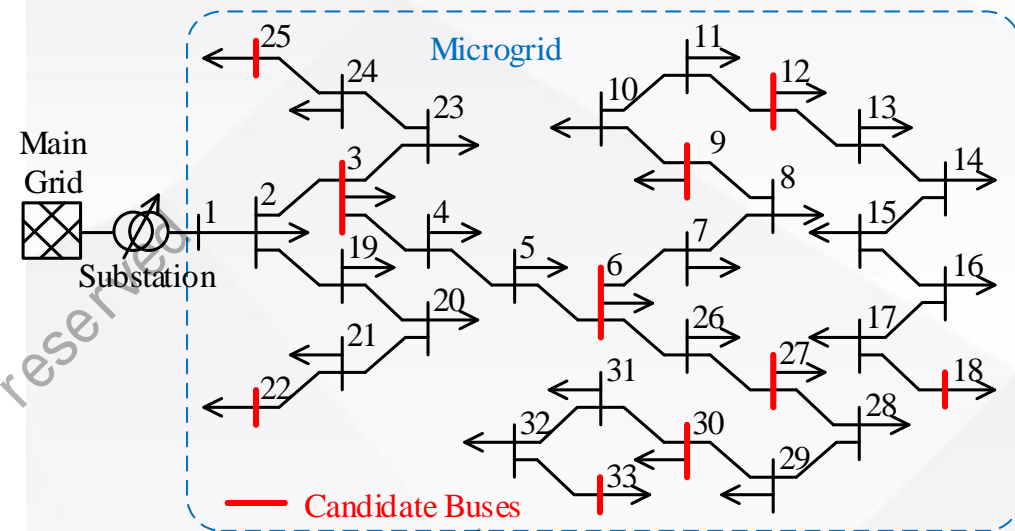


Fig. 4 DG planning decisions.

COMPARISON BETWEEN DIFFERENT METHODS

DG Planning Method	PRO	RO			
		1	2	3	4
Uncertainty Profile Case	N/A	1	2	3	4
Voltage Violation Rate	0%	8.12%	0%	3.12%	11.44%
Profit in NPV (M\$)	23.51	24.71	23.43	24.50	24.74

C. Zhang, Y. Xu*, Z.Y. Dong, "Probability-Weighted Robust Optimization for Distributed Generation Planning in Microgrids," *IEEE Trans. Power Syst.*, 2018.

■ Publication list in DER and Microgrid

1. C. Zhang and **Y. Xu***, “Hierarchically-Coordinated Voltage/VAR Control of Distribution Networks using PV Inverters,” *IEEE Trans. Smart Grid*, 2020.
2. C. Zhang, **Y. Xu***, Z.Y. Dong, and R. Zhang, “Multi-Objective Adaptive Robust Voltage/VAR Control for High-PV Penetrated Distribution Networks,” *IEEE Trans. Smart Grid*, 2020.
3. Z. Li, **Y. Xu***, et al, “Optimal Deployment of Heterogeneous Energy Storage System in a Residential Multi-Energy Microgrid with Demand Side Management,” *IEEE Trans. Industrial Informatics*, 2020.
4. Q. Xu, **Y. Xu***, Z. Xu, L. Xie, F. Blaabjerg, “A Hierarchically Coordinated Operation and Control Scheme for DC Microgrid Clusters under Uncertainty,” *IEEE Trans. Sustainable Energy*, 2020.
5. Q. Xu, T. Zhao, **Y. Xu***, Z. Xu, P. Wang, and F. Blaabjerg, “A Distributed and Robust Energy Management System for Networked Hybrid AC/DC Microgrids,” *IEEE Trans. Smart Grid*, 2020.
6. C. Zhang, **Y. Xu***, and Z.Y. Dong, “Robustly Coordinated Operation of a Multi-Energy Micro-Grid in Grid-Connected and Islanded Modes under Uncertainties,” *IEEE Trans. Sustainable Energy*, 2020.
7. Y. Wang, T.L. Nguyen, M. Syed, **Y. Xu***, E. Guillo-Sansano, V.H. Nguye, G. Burt, and Q.T. Tran, “A Distributed Control Scheme of Microgrids in Energy Internet Paradigm and Its Multisite Implementation,” *IEEE Trans. Industrial Informatics*, 2020.
8. Y. Wang, M.H. Syed, E. Guillo-Sansano, **Y. Xu***, and G.M. Burt, “Inverter-based Voltage Control of Distribution Networks: A Three-Level Coordinated Method and Power Hardware-in-the-Loop Validation,” *IEEE Trans. Sustainable Energy*, 2020.
9. Y. Wang, T. L. Nguyen, **Y. Xu***, and D. Shi, “Distributed Control of Heterogeneous Energy Storage Systems in Islanded Microgrids: Finite-Time Approach and Cyber-Physical Implementation,” *Int. J. Electrical Power and Energy Systems*, 2020.
10. Q. Xu, **Y. Xu***, C. Zhang, and P. Wang, “A Robust Droop-based Autonomous Controller for Decentralized Power Sharing in DC Microgrid Considering Large Signal Stability,” *IEEE Trans. Industrial Informatics*, 2020.

■ Publication list in DER and Microgrid

11. Z. Li and **Y. Xu***, “Temporally-Coordinated Optimal Operation of a Multi-energy Microgrid under Diverse Uncertainties,” *Applied Energy*, 2019.
12. C. Zhang, **Y. Xu***, Z.Y. Dong, “Robustly Coordinated Operation of a Multi-Energy Micro-Grid in Grid-Connected and Islanded Modes under Uncertainties,” *IEEE Trans. Sustainable Energy*, 2019.
13. Y. Wang, T. Zhao, C. Ju, **Y. Xu***, P. Wang “Two-Level Distributed Voltage/Var Control of Aggregated PV Inverters in Distribution Networks,” *IEEE Trans. Power Delivery*, 2019.
14. Y. Wang, **Y. Xu**, and Y. Tang, “Distributed Aggregation Control of Grid-Interactive Smart Buildings for Power System Frequency Support,” *Applied Energy*, 2019.
15. S. Sharma, **Y. Xu***, A. Verma, et al, “Time-Coordinated Multi-Energy Management of Smart Buildings under Uncertainties,” *IEEE Trans. Industrial Informatics*, 2019.
16. Y. Wang, T.L. Nguyen, **Y. Xu***, et al, “Cyber-Physical Design and Implementation of Distributed Event-Triggered Secondary Control in Islanded Microgrids,” *IEEE Trans. Industry Applications*, 2019.
17. Z. Li, **Y. Xu***, et al, “Optimal Placement of Heterogeneous Distributed Generators in a Grid-Connected Multi-Energy Microgrid under Uncertainties,” *IET Renewable Power Generation*, 2019.
18. Y. Wang, Y. Tang, **Y. Xu***, et al, “A Distributed Control Scheme of Thermostatically Controlled Loads for Building-Microgrid Community,” *IEEE Trans. Sust. Energy*, 2019. – **Web-of-Science Highly Cited Paper**
19. Y. Chen, **Y. Xu***, et al, “Optimally Coordinated Dispatch of Combined-Heat-and-Electrical Network,” *IET Gen. Trans. & Dist.*, 2019.
20. R. Xu, C. Zhang, **Y. Xu***, Z.Y. Dong, “Rolling Horizon Based Multi-Objective Robust Voltage/VAR Regulation with Conservation Voltage Reduction in High PV-Penetrated Distribution Networks,” *IET Gen. Trans. & Dist.*, 2019.
21. **Y. Xu***, Z.Y. Dong, et al, “Multi-timescale coordinated voltage/var control of high renewable-penetrated distribution networks,” *IEEE Trans. Power Syst.*, 2018.
22. Z. Li and **Y. Xu***, “Optimal coordinated energy dispatch for a multi-energy microgrid in grid-connected and islanded modes,” *Applied Energy*, 2018. – **Web-of-Science Highly Cited Paper**

■ Publication list in DER and Microgrid

23. Y. Wang, **Y. Xu**, Y. Tang, et al “Aggregated Energy Storage for Power System Frequency Control: A Finite-Time Consensus Approach,” *IEEE Trans. Smart Grid*, 2018.
24. Y. Wang, **Y. Xu***, Y. Tang, et al, “Decentralized-Distributed Hybrid Voltage Regulation of Power Distribution Networks Based on Power Inverters,” *IET Gen. Trans. & Dist.*, 2018.
25. C. Zhang, **Y. Xu***, Z.Y. Dong, et al, “Probability-Weighted Robust Optimization for Distributed Generation Planning in Microgrids,” *IEEE Trans. Power Syst.*, 2018.
26. C. Zhang, **Y. Xu***, Z.Y. Dong, et al, “Robustly Coordinated Operation of A Multi-Energy Microgrid with Flexible Electric and Thermal Loads,” *IEEE Trans. Smart Grid*, 2018.
27. C. Zhang, **Y. Xu***, Z.Y. Dong, “Three-Stage Robust Inverter-Based Voltage/Var Control for Distribution Networks with High PV,” *IEEE Trans. Smart Grid*, 2017. – **Web-of-Science Highly Cited Paper**
28. C. Zhang, **Y. Xu***, Z.Y. Dong, et al, “Robust operation of Microgrids via two-stage coordinated energy storage and direct load control,” *IEEE Trans. Power Syst.*, 2017.
29. C. Zhang, **Y. Xu**, Z.Y. Dong, “Robust Coordination of Distributed Generation and Price-Based Demand Response in Microgrids,” *IEEE Trans. Smart Grid*, 2017. – **Web-of-Science Highly Cited Paper**
30. W. Zhang, **Y. Xu***, Z.Y. Dong, “Robust SCOPF using multiple microgrids for corrective control under uncertainty,” *IEEE Trans. Industrial Informatics*, 2017.
31. C. Ju, P. Wang, L. Goel, and **Y. Xu***, “A two-layer energy management system for microgrids with hybrid energy storage considering degradation costs,” *IEEE Trans. Smart Grid*, 2017.
32. **Y. Xu**, Z.Y. Dong, K.P. Wong, et al, “Optimal capacitor placement to distribution transformers for power loss reduction in radial distribution systems,” *IEEE Trans. Power Systems*, 2013.

***Corresponding author**

To appear in 2021: Y. Xu, Y. Wang, C. Zhang, and Z. Li, “Coordination and optimization of distributed energy resources in microgrids,” IET Book Press.



**NANYANG
TECHNOLOGICAL
UNIVERSITY**
SINGAPORE

Thank You!